

## INTRODUCTION

This paper contains the computation of the motive of the irreducible  $\mathrm{SL}_4(k)$ -character variety of torus knots for any algebraically closed field  $k$  of zero characteristic. The calculation is based on the methods introduced in the paper [1].

The notations used in this paper are the following:

- $R_4^{\mathrm{irr}}$  is the irreducible  $\mathrm{SL}_4(k)$ -representation variety of torus knots, that is, the variety of irreducible representations  $\rho : \Gamma \rightarrow \mathrm{SL}_4(k)$  where  $\Gamma = \Gamma_{n,m}$  is the fundamental group of the complement of the  $(n,m)$ -torus knot (see section 4 of [1]).
- $\mathfrak{M}_4^{\mathrm{irr}} = R_4^{\mathrm{irr}} // \mathrm{SL}_4(k)$  is the irreducible  $\mathrm{SL}_4(k)$ -character variety of torus knots, that is, the moduli space of representations (see section 4 of [1]).
- $\kappa = (\epsilon, \varepsilon)$  is a configuration of eigenvalues, that is a collection of possible eigenvalues for the matrices  $A$  and  $B$  of a torus knot representation  $\rho = (A, B)$  (see section 4 of [1]).
- $\tau$  is the type of a semi-simple filtration of a torus knot representation (see section 2.1 of [1]).
- $\xi$  is the shape of the type  $\tau$ , that is the collection of dimensions and multiplicities of each isotypic component (see section 2.1 of [1]).
- $\sigma_A$  are the collections of eigenvalues of  $A$  for each isotypic component of a torus knot representation  $\rho = (A, B)$  (see section 7.1 of [1]).
- $\sigma_B$  are the collections of eigenvalues of  $B$  for each isotypic component of a torus knot representation  $\rho = (A, B)$  (see section 7.1 of [1]).
- $\mathcal{M}_\tau$  is the space parametrizing possible completions of a semi-simple representation to a general representation of type  $\tau$  (see section 4 of [1])
- $\mathcal{G}_\tau$  is the gauge group acting on  $\mathcal{M}_\tau \times \mathrm{SL}_4(k)$  that identifies isomorphic completions (see section 4 of [1]).
- $\mathfrak{M}_\tau^{\mathrm{irr}}$  is the variety of possible semi-simplifications of a representation of type  $\tau$  (see section 4 of [1]).
- $R(\tau)$  is the variety of representations of type  $\tau$ .
- $m_\kappa(\tau)$  is the multiplicity of the type  $\tau$ , that is the number of isomorphic components  $R(\tau')$  of types  $\tau'$  with the same shape as  $\tau$  but whose eigenvalues are given by a permutation of the ones of  $\tau$  that preserves their multiplicity (see section 5 of [1]).
- $C_{\pi, \pi'}$  are the number of isomorphic components given by configurations of eigenvalues with the same structure of repeated eigenvalues (see Section 6 of [1]). Here,  $\pi, \pi'$  are two partitions of 4 that determine the number of repeated eigenvalues of the matrices  $A$  and  $B$  of a representation  $\rho = (A, B)$ . If  $\pi = \{1^{e_1}, \dots, 4^{e_4}\}$  and  $\pi' = \{1^{e'_1}, \dots, 4^{e'_4}\}$  we have the following characterization in terms of multinomial numbers (Theorem 6.8 of [1])

$$C_{\pi, \pi'} = \frac{4}{nm} \binom{n}{e_1, \dots, e_4} \binom{m}{e'_1, \dots, e'_4}.$$

Combinatorial formulas for the motives  $[\mathcal{M}_\tau]$ ,  $[\mathcal{G}_\tau]$  and  $[\mathfrak{M}_\tau^{\mathrm{irr}}]$  are described in section 5 of [1] in terms of the structure of the type  $\tau$ .

The structure of the paper is as follows. Each section describes the count of the motive  $[\mathfrak{M}_\kappa]$  for a possible configuration of eigenvalues  $\kappa$ . For that purpose, we analyze all the types  $\tau$  compatible with  $\kappa$  and compute the motives  $[R(\tau)]$ . A configuration of eigenvalues  $\kappa$  not appearing as a section of the paper means that  $R_\kappa^{\mathrm{irr}} = \emptyset$  (see Remark 4.5 and Proposition 8.1 of [1]). In the final section of this paper, we summarize the results for each configuration  $\kappa$  and we provide the final result depending on the combinatorial coefficients  $C_{\pi, \pi'}$ .

**Warning:** The script generating this paper is only valid for rank  $\leq 4$ . The result for higher rank may not be correct.

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 1. CONFIGURATION  $\epsilon = (\epsilon_1, \epsilon_1, \epsilon_1, \epsilon_2)$  AND  $\varepsilon = (\varepsilon_1, \varepsilon_2, \varepsilon_3, \varepsilon_4)$ 


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$$\xi = ((3, 1), (1, 1)), \quad \sigma_A = (\epsilon_1, \epsilon_1, \epsilon_2, \epsilon_1), \quad \sigma_B = (\epsilon_1, \epsilon_2, \epsilon_4, \epsilon_3).$$

- $[\mathcal{M}_\tau] = 1.$
  - $[\mathcal{G}_\tau] = (q - 1)^2.$
  - $[\mathfrak{M}_\tau^{\text{irr}}] = q^2 - 3q + 3.$
  - $[R(\tau)] = q^{16} - 2q^{15} + 2q^{13} + q^{12} + 2q^{11} - 3q^{10} - 2q^9 - 2q^8 + 3q^6$
  - $m_\kappa(\tau) = 4.$
- 

$$\xi = ((2, 1), (1, 1), (1, 1)), \quad \sigma_A = (\epsilon_1, \epsilon_2, \epsilon_1, \epsilon_1), \quad \sigma_B = (\epsilon_1, \epsilon_4, \epsilon_2, \epsilon_3).$$

- $[\mathcal{M}_\tau] = 1.$
  - $[\mathcal{G}_\tau] = (q - 1)^3.$
  - $[\mathfrak{M}_\tau^{\text{irr}}] = q - 2.$
  - $[R(\tau)] = q^{14} - 2q^{12} - 3q^{11} - 3q^{10} + 2q^8 + 3q^7 + 2q^6$
  - $m_\kappa(\tau) = 6.$
- 

$$\xi = ((1, 1), (1, 1), (1, 1), (1, 1)), \quad \sigma_A = (\epsilon_1, \epsilon_1, \epsilon_1, \epsilon_2), \quad \sigma_B = (\epsilon_1, \epsilon_2, \epsilon_3, \epsilon_4).$$

- $[\mathcal{M}_\tau] = 1.$
  - $[\mathcal{G}_\tau] = (q - 1)^4.$
  - $[\mathfrak{M}_\tau^{\text{irr}}] = 1.$
  - $[R(\tau)] = q^{12} + 3q^{11} + 5q^{10} + 6q^9 + 5q^8 + 3q^7 + q^6$
  - $m_\kappa(\tau) = 4.$
- 

$$\xi = ((1, 1), (1, 1), (1, 1), (1, 1)), \quad \sigma_A = (\epsilon_1, \epsilon_1, \epsilon_1, \epsilon_2), \quad \sigma_B = (\epsilon_1, \epsilon_2, \epsilon_3, \epsilon_4).$$

- $[\mathcal{M}_\tau] = q^3 - 1.$
  - $[\mathcal{G}_\tau] = (q - 1)^4.$
  - $[\mathfrak{M}_\tau^{\text{irr}}] = 1.$
  - $[R(\tau)] = q^{15} + 3q^{14} + 5q^{13} + 5q^{12} + 2q^{11} - 2q^{10} - 5q^9 - 5q^8 - 3q^7 - q^6$
  - $m_\kappa(\tau) = 4.$
- 

$$\xi = ((3, 1), (1, 1)), \quad \sigma_A = (\epsilon_1, \epsilon_1, \epsilon_2, \epsilon_1), \quad \sigma_B = (\epsilon_1, \epsilon_2, \epsilon_4, \epsilon_3).$$

- $[\mathcal{M}_\tau] = q^3 - q^2.$
  - $[\mathcal{G}_\tau] = (q - 1)^2 q^2.$
  - $[\mathfrak{M}_\tau^{\text{irr}}] = q^2 - 3q + 3.$
  - $[R(\tau)] = q^{17} - 3q^{16} + 2q^{15} + 2q^{14} - q^{13} + q^{12} - 5q^{11} + q^{10} + 2q^8 + 3q^7 - 3q^6$
  - $m_\kappa(\tau) = 4.$
- 

$$\xi = ((2, 1), (1, 1), (1, 1)), \quad \sigma_A = (\epsilon_1, \epsilon_2, \epsilon_1, \epsilon_1), \quad \sigma_B = (\epsilon_1, \epsilon_4, \epsilon_2, \epsilon_3).$$

- $[\mathcal{M}_\tau] = q^3 - q^2.$
- $[\mathcal{G}_\tau] = (q - 1)^3 q^2.$
- $[\mathfrak{M}_\tau^{\text{irr}}] = q - 2.$
- $[R(\tau)] = q^{15} - q^{14} - 2q^{13} - q^{12} + 3q^{10} + 2q^9 + q^8 - q^7 - 2q^6$
- $m_\kappa(\tau) = 12.$

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$$\xi = ((1,1),(1,1),(1,1),(1,1)), \quad \sigma_A = (\epsilon_1, \epsilon_1, \epsilon_2, \epsilon_1), \quad \sigma_B = (\epsilon_1, \epsilon_2, \epsilon_4, \epsilon_3).$$

- $[\mathcal{M}_\tau] = q^3 - q^2.$
  - $[\mathcal{G}_\tau] = (q-1)^4 q^2.$
  - $[\mathfrak{M}_\tau^{\text{irr}}] = 1.$
  - $[R(\tau)] = q^{13} + 2q^{12} + 2q^{11} + q^{10} - q^9 - 2q^8 - 2q^7 - q^6$
  - $m_\kappa(\tau) = 12.$
- 

$$\xi = ((1,1),(1,1),(2,1)), \quad \sigma_A = (\epsilon_1, \epsilon_1, \epsilon_1, \epsilon_2), \quad \sigma_B = (\epsilon_1, \epsilon_2, \epsilon_3, \epsilon_4).$$

- $[\mathcal{M}_\tau] = q^4 - q^2.$
  - $[\mathcal{G}_\tau] = (q-1)^3 q^2.$
  - $[\mathfrak{M}_\tau^{\text{irr}}] = q - 2.$
  - $[R(\tau)] = q^{16} - 3q^{14} - 3q^{13} - q^{12} + 3q^{11} + 5q^{10} + 3q^9 - 3q^7 - 2q^6$
  - $m_\kappa(\tau) = 6.$
- 

$$\xi = ((2,1),(1,1),(1,1)), \quad \sigma_A = (\epsilon_1, \epsilon_2, \epsilon_1, \epsilon_1), \quad \sigma_B = (\epsilon_1, \epsilon_4, \epsilon_2, \epsilon_3).$$

- $[\mathcal{M}_\tau] = (q^2 - q)^2.$
  - $[\mathcal{G}_\tau] = (q-1)^3 q^2.$
  - $[\mathfrak{M}_\tau^{\text{irr}}] = q - 2.$
  - $[R(\tau)] = q^{16} - 2q^{15} - q^{14} + q^{13} + q^{12} + 3q^{11} - q^{10} - q^9 - 2q^8 - q^7 + 2q^6$
  - $m_\kappa(\tau) = 6.$
- 

$$\xi = ((1,1),(1,1),(1,1),(1,1)), \quad \sigma_A = (\epsilon_1, \epsilon_2, \epsilon_1, \epsilon_1), \quad \sigma_B = (\epsilon_1, \epsilon_4, \epsilon_2, \epsilon_3).$$

- $[\mathcal{M}_\tau] = (q^2 - q)^2.$
  - $[\mathcal{G}_\tau] = (q-1)^4 q^2.$
  - $[\mathfrak{M}_\tau^{\text{irr}}] = 1.$
  - $[R(\tau)] = q^{14} + q^{13} - q^{11} - 2q^{10} - q^9 + q^7 + q^6$
  - $m_\kappa(\tau) = 12.$
- 

$$\xi = ((1,1),(1,1),(1,1),(1,1)), \quad \sigma_A = (\epsilon_1, \epsilon_1, \epsilon_2, \epsilon_1), \quad \sigma_B = (\epsilon_1, \epsilon_2, \epsilon_4, \epsilon_3).$$

- $[\mathcal{M}_\tau] = (q^2 - 1)(q-1)q^2.$
  - $[\mathcal{G}_\tau] = (q-1)^4 q^2.$
  - $[\mathfrak{M}_\tau^{\text{irr}}] = 1.$
  - $[R(\tau)] = q^{15} + 2q^{14} + q^{13} - q^{12} - 3q^{11} - 3q^{10} - q^9 + q^8 + 2q^7 + q^6$
  - $m_\kappa(\tau) = 12.$
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$$\xi = ((1,1),(3,1)), \quad \sigma_A = (\epsilon_1, \epsilon_1, \epsilon_1, \epsilon_2), \quad \sigma_B = (\epsilon_1, \epsilon_2, \epsilon_3, \epsilon_4).$$

- $[\mathcal{M}_\tau] = q^3 - q^2.$
- $[\mathcal{G}_\tau] = (q-1)^2 q^2.$
- $[\mathfrak{M}_\tau^{\text{irr}}] = q^2 - 3q + 3.$
- $[R(\tau)] = q^{17} - 3q^{16} + 2q^{15} + 2q^{14} - q^{13} + q^{12} - 5q^{11} + q^{10} + 2q^8 + 3q^7 - 3q^6$
- $m_\kappa(\tau) = 4.$

$$\xi = ((1,1),(1,1),(1,1),(1,1)), \quad \sigma_A = (\epsilon_2, \epsilon_1, \epsilon_1, \epsilon_1), \quad \sigma_B = (\epsilon_4, \epsilon_1, \epsilon_2, \epsilon_3).$$

- $[\mathcal{M}_\tau] = (q-1)^3.$
- $[\mathcal{G}_\tau] = (q-1)^4.$
- $[\mathfrak{M}_\tau^{\text{irr}}] = 1.$
- $[R(\tau)] = q^{15} - q^{13} - q^{12} - q^{11} + q^{10} + q^9 + q^8 - q^6$
- $m_\kappa(\tau) = 4.$

$$\xi = ((1,1),(2,1),(1,1)), \quad \sigma_A = (\epsilon_1, \epsilon_1, \epsilon_2, \epsilon_1), \quad \sigma_B = (\epsilon_1, \epsilon_2, \epsilon_4, \epsilon_3).$$

- $[\mathcal{M}_\tau] = (q^2 - q)^2 q.$
- $[\mathcal{G}_\tau] = (q-1)^3 q^3.$
- $[\mathfrak{M}_\tau^{\text{irr}}] = q - 2.$
- $[R(\tau)] = q^{16} - 2q^{15} - q^{14} + q^{13} + q^{12} + 3q^{11} - q^{10} - q^9 - 2q^8 - q^7 + 2q^6$
- $m_\kappa(\tau) = 12.$

$$\xi = ((1,1),(1,1),(1,1),(1,1)), \quad \sigma_A = (\epsilon_1, \epsilon_2, \epsilon_1, \epsilon_1), \quad \sigma_B = (\epsilon_1, \epsilon_4, \epsilon_2, \epsilon_3).$$

- $[\mathcal{M}_\tau] = (q-1)^3 q^2.$
- $[\mathcal{G}_\tau] = (q-1)^4 q^2.$
- $[\mathfrak{M}_\tau^{\text{irr}}] = 1.$
- $[R(\tau)] = q^{15} - q^{13} - q^{12} - q^{11} + q^{10} + q^9 + q^8 - q^6$
- $m_\kappa(\tau) = 12.$

**Total count of  $\kappa = ((\epsilon_1, \epsilon_1, \epsilon_1, \epsilon_2), (\varepsilon_1, \varepsilon_2, \varepsilon_3, \varepsilon_4))$**

$$\begin{aligned} [R_\kappa^{\text{red}}] &= 8q^{17} + 4q^{16} + 16q^{15} + 22q^{14} + 16q^{13} + 20q^{12} + 2q^{11} + 6q^{10} + 6q^9 - 4q^8, \\ [R_\kappa^{\text{irr}}] &= q^{18} - 4q^{17} + 5q^{16} - q^{15} - 3q^{14} + 3q^{13} - 5q^{12} + 7q^{11} - 2q^{10} + q^9 - 6q^8 + 4q^7, \\ [R_\kappa] &= q^{18} + 4q^{17} + 9q^{16} + 15q^{15} + 19q^{14} + 19q^{13} + 15q^{12} + 9q^{11} + 4q^{10} + q^9, \\ [\mathfrak{M}_\kappa] &= q^3 - 4q^2 + 6q - 4. \end{aligned}$$

2. CONFIGURATION  $\epsilon = (\epsilon_1, \epsilon_1, \epsilon_2, \epsilon_2)$  AND  $\varepsilon = (\varepsilon_1, \varepsilon_1, \varepsilon_2, \varepsilon_2)$

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**Total count of  $\kappa = ((\epsilon_1, \epsilon_1, \epsilon_2, \epsilon_2), (\varepsilon_1, \varepsilon_1, \varepsilon_2, \varepsilon_2))$**

$$\begin{aligned} [R_\kappa^{\text{red}}] &= q^{16} + 2q^{15} + 5q^{14} + 6q^{13} + 8q^{12} + 6q^{11} + 5q^{10} + 2q^9 + q^8, \\ [R_\kappa^{\text{irr}}] &= 0, \\ [R_\kappa] &= q^{16} + 2q^{15} + 5q^{14} + 6q^{13} + 8q^{12} + 6q^{11} + 5q^{10} + 2q^9 + q^8, \\ [\mathfrak{M}_\kappa] &= 0. \end{aligned}$$

3. CONFIGURATION  $\epsilon = (\epsilon_1, \epsilon_1, \epsilon_2, \epsilon_2)$  AND  $\varepsilon = (\varepsilon_1, \varepsilon_1, \varepsilon_2, \varepsilon_3)$

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$$\xi = ((3, 1), (1, 1)), \quad \sigma_A = (\epsilon_1, \epsilon_1, \epsilon_2, \epsilon_2), \quad \sigma_B = (\epsilon_2, \epsilon_3, \epsilon_1, \epsilon_1).$$

- $[\mathcal{M}_\tau] = 1.$
  - $[\mathcal{G}_\tau] = (q - 1)^2.$
  - $[\mathfrak{M}_\tau^{\text{irr}}] = q^2 - 3q + 3.$
  - $[R(\tau)] = q^{16} - 2q^{15} + 2q^{13} + q^{12} + 2q^{11} - 3q^{10} - 2q^9 - 2q^8 + 3q^6$
  - $m_\kappa(\tau) = 2.$
- 

$$\xi = ((2, 1), (2, 1)), \quad \sigma_A = (\epsilon_1, \epsilon_2, \epsilon_1, \epsilon_2), \quad \sigma_B = (\epsilon_1, \epsilon_2, \epsilon_1, \epsilon_3).$$

- $[\mathcal{M}_\tau] = 1.$
  - $[\mathcal{G}_\tau] = (q - 1)^2.$
  - $[\mathfrak{M}_\tau^{\text{irr}}] = q^2 - 4q + 4.$
  - $[R(\tau)] = q^{16} - 3q^{15} + 3q^{13} + 2q^{12} + 3q^{11} - 4q^{10} - 3q^9 - 3q^8 + 4q^6$
  - $m_\kappa(\tau) = 1.$
- 

$$\xi = ((2, 1), (1, 1), (1, 1)), \quad \sigma_A = (\epsilon_1, \epsilon_2, \epsilon_1, \epsilon_2), \quad \sigma_B = (\epsilon_1, \epsilon_2, \epsilon_1, \epsilon_3).$$

- $[\mathcal{M}_\tau] = 1.$
  - $[\mathcal{G}_\tau] = (q - 1)^3.$
  - $[\mathfrak{M}_\tau^{\text{irr}}] = q - 2.$
  - $[R(\tau)] = q^{14} - 2q^{12} - 3q^{11} - 3q^{10} + 2q^8 + 3q^7 + 2q^6$
  - $m_\kappa(\tau) = 4.$
- 

$$\xi = ((2, 1), (1, 1), (1, 1)), \quad \sigma_A = (\epsilon_1, \epsilon_2, \epsilon_1, \epsilon_2), \quad \sigma_B = (\epsilon_2, \epsilon_3, \epsilon_1, \epsilon_1).$$

- $[\mathcal{M}_\tau] = 1.$
  - $[\mathcal{G}_\tau] = (q - 1)^3.$
  - $[\mathfrak{M}_\tau^{\text{irr}}] = q - 2.$
  - $[R(\tau)] = q^{14} - 2q^{12} - 3q^{11} - 3q^{10} + 2q^8 + 3q^7 + 2q^6$
  - $m_\kappa(\tau) = 1.$
- 

$$\xi = ((1, 2), (1, 1), (1, 1)), \quad \sigma_A = (\epsilon_1, \epsilon_2, \epsilon_2), \quad \sigma_B = (\epsilon_1, \epsilon_2, \epsilon_3).$$

- $[\mathcal{M}_\tau] = 1.$
  - $[\mathcal{G}_\tau] = (q + 1)(q - 1)^4q.$
  - $[\mathfrak{M}_\tau^{\text{irr}}] = 1.$
  - $[R(\tau)] = q^{10} + 2q^9 + 3q^8 + 3q^7 + 2q^6 + q^5$
  - $m_\kappa(\tau) = 2.$
- 

$$\xi = ((1, 1), (1, 1), (1, 1), (1, 1)), \quad \sigma_A = (\epsilon_1, \epsilon_1, \epsilon_2, \epsilon_2), \quad \sigma_B = (\epsilon_1, \epsilon_2, \epsilon_3, \epsilon_1).$$

- $[\mathcal{M}_\tau] = 1.$
- $[\mathcal{G}_\tau] = (q - 1)^4.$
- $[\mathfrak{M}_\tau^{\text{irr}}] = 1.$
- $[R(\tau)] = q^{12} + 3q^{11} + 5q^{10} + 6q^9 + 5q^8 + 3q^7 + q^6$
- $m_\kappa(\tau) = 2.$

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$$\xi = ((3, 1), (1, 1)), \quad \sigma_A = (\epsilon_1, \epsilon_1, \epsilon_2, \epsilon_2), \quad \sigma_B = (\epsilon_2, \epsilon_3, \epsilon_1, \epsilon_1).$$

- $[\mathcal{M}_\tau] = q^2 - q.$
  - $[\mathcal{G}_\tau] = (q - 1)^2 q.$
  - $[\mathfrak{M}_\tau^{\text{irr}}] = q^2 - 3q + 3.$
  - $[R(\tau)] = q^{17} - 3q^{16} + 2q^{15} + 2q^{14} - q^{13} + q^{12} - 5q^{11} + q^{10} + 2q^8 + 3q^7 - 3q^6$
  - $m_\kappa(\tau) = 2.$
- 

$$\xi = ((2, 1), (1, 1), (1, 1)), \quad \sigma_A = (\epsilon_1, \epsilon_2, \epsilon_1, \epsilon_2), \quad \sigma_B = (\epsilon_1, \epsilon_2, \epsilon_1, \epsilon_3).$$

- $[\mathcal{M}_\tau] = q^3 - q.$
  - $[\mathcal{G}_\tau] = (q - 1)^3 q.$
  - $[\mathfrak{M}_\tau^{\text{irr}}] = q - 2.$
  - $[R(\tau)] = q^{16} - 3q^{14} - 3q^{13} - q^{12} + 3q^{11} + 5q^{10} + 3q^9 - 3q^7 - 2q^6$
  - $m_\kappa(\tau) = 4.$
- 

$$\xi = ((2, 1), (1, 1), (1, 1)), \quad \sigma_A = (\epsilon_1, \epsilon_2, \epsilon_1, \epsilon_2), \quad \sigma_B = (\epsilon_2, \epsilon_1, \epsilon_3, \epsilon_1).$$

- $[\mathcal{M}_\tau] = q^2 - q.$
  - $[\mathcal{G}_\tau] = (q - 1)^3 q.$
  - $[\mathfrak{M}_\tau^{\text{irr}}] = q - 2.$
  - $[R(\tau)] = q^{15} - q^{14} - 2q^{13} - q^{12} + 3q^{10} + 2q^9 + q^8 - q^7 - 2q^6$
  - $m_\kappa(\tau) = 4.$
- 

$$\xi = ((2, 1), (1, 1), (1, 1)), \quad \sigma_A = (\epsilon_1, \epsilon_2, \epsilon_1, \epsilon_2), \quad \sigma_B = (\epsilon_2, \epsilon_3, \epsilon_1, \epsilon_1).$$

- $[\mathcal{M}_\tau] = q^2 - q.$
  - $[\mathcal{G}_\tau] = (q - 1)^3 q.$
  - $[\mathfrak{M}_\tau^{\text{irr}}] = q - 2.$
  - $[R(\tau)] = q^{15} - q^{14} - 2q^{13} - q^{12} + 3q^{10} + 2q^9 + q^8 - q^7 - 2q^6$
  - $m_\kappa(\tau) = 2.$
- 

$$\xi = ((1, 2), (1, 1), (1, 1)), \quad \sigma_A = (\epsilon_1, \epsilon_2, \epsilon_2), \quad \sigma_B = (\epsilon_1, \epsilon_2, \epsilon_3).$$

- $[\mathcal{M}_\tau] = q^3 - q.$
  - $[\mathcal{G}_\tau] = (q + 1)(q - 1)^4 q^2.$
  - $[\mathfrak{M}_\tau^{\text{irr}}] = 1.$
  - $[R(\tau)] = q^{12} + 2q^{11} + 2q^{10} + q^9 - q^8 - 2q^7 - 2q^6 - q^5$
  - $m_\kappa(\tau) = 4.$
- 

$$\xi = ((1, 1), (1, 1), (1, 1), (1, 1)), \quad \sigma_A = (\epsilon_1, \epsilon_1, \epsilon_2, \epsilon_2), \quad \sigma_B = (\epsilon_2, \epsilon_3, \epsilon_1, \epsilon_1).$$

- $[\mathcal{M}_\tau] = q^2 - 1.$
- $[\mathcal{G}_\tau] = (q - 1)^4 q.$
- $[\mathfrak{M}_\tau^{\text{irr}}] = 1.$
- $[R(\tau)] = q^{13} + 3q^{12} + 4q^{11} + 3q^{10} - 3q^8 - 4q^7 - 3q^6 - q^5$
- $m_\kappa(\tau) = 2.$

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$$\xi = ((1,1),(1,1),(1,1),(1,1)), \quad \sigma_A = (\epsilon_1, \epsilon_1, \epsilon_2, \epsilon_2), \quad \sigma_B = (\epsilon_1, \epsilon_2, \epsilon_3, \epsilon_1).$$

- $[\mathcal{M}_\tau] = q^2 - q.$
  - $[\mathcal{G}_\tau] = (q-1)^4 q.$
  - $[\mathfrak{M}_\tau^{\text{irr}}] = 1.$
  - $[R(\tau)] = q^{13} + 2q^{12} + 2q^{11} + q^{10} - q^9 - 2q^8 - 2q^7 - q^6$
  - $m_\kappa(\tau) = 4.$
- 

$$\xi = ((1,1),(1,1),(1,1),(1,1)), \quad \sigma_A = (\epsilon_1, \epsilon_1, \epsilon_2, \epsilon_2), \quad \sigma_B = (\epsilon_2, \epsilon_1, \epsilon_1, \epsilon_3).$$

- $[\mathcal{M}_\tau] = q^3 - q.$
  - $[\mathcal{G}_\tau] = (q-1)^4 q.$
  - $[\mathfrak{M}_\tau^{\text{irr}}] = 1.$
  - $[R(\tau)] = q^{14} + 3q^{13} + 4q^{12} + 3q^{11} - 3q^9 - 4q^8 - 3q^7 - q^6$
  - $m_\kappa(\tau) = 4.$
- 

$$\xi = ((1,2),(1,1),(1,1)), \quad \sigma_A = (\epsilon_1, \epsilon_2, \epsilon_2), \quad \sigma_B = (\epsilon_1, \epsilon_2, \epsilon_3).$$

- $[\mathcal{M}_\tau] = (q^2 - 1)^2.$
  - $[\mathcal{G}_\tau] = (q+1)(q-1)^4 q.$
  - $[\mathfrak{M}_\tau^{\text{irr}}] = 1.$
  - $[R(\tau)] = q^{14} + 2q^{13} + q^{12} - q^{11} - 3q^{10} - 3q^9 - q^8 + q^7 + 2q^6 + q^5$
  - $m_\kappa(\tau) = 2.$
- 

$$\xi = ((1,1),(1,1),(1,2)), \quad \sigma_A = (\epsilon_1, \epsilon_1, \epsilon_2), \quad \sigma_B = (\epsilon_2, \epsilon_3, \epsilon_1).$$

- $[\mathcal{M}_\tau] = q^4 - q^3 - q^2 + q.$
  - $[\mathcal{G}_\tau] = (q+1)(q-1)^4 q.$
  - $[\mathfrak{M}_\tau^{\text{irr}}] = 1.$
  - $[R(\tau)] = q^{14} + q^{13} - q^{11} - 2q^{10} - q^9 + q^7 + q^6$
  - $m_\kappa(\tau) = 2.$
- 

$$\xi = ((1,1),(1,1),(1,1),(1,1)), \quad \sigma_A = (\epsilon_1, \epsilon_1, \epsilon_2, \epsilon_2), \quad \sigma_B = (\epsilon_1, \epsilon_2, \epsilon_3, \epsilon_1).$$

- $[\mathcal{M}_\tau] = (q^2 - 1)(q - 1).$
  - $[\mathcal{G}_\tau] = (q - 1)^4.$
  - $[\mathfrak{M}_\tau^{\text{irr}}] = 1.$
  - $[R(\tau)] = q^{15} + 2q^{14} + q^{13} - q^{12} - 3q^{11} - 3q^{10} - q^9 + q^8 + 2q^7 + q^6$
  - $m_\kappa(\tau) = 4.$
- 

$$\xi = ((2,1),(2,1)), \quad \sigma_A = (\epsilon_1, \epsilon_2, \epsilon_1, \epsilon_2), \quad \sigma_B = (\epsilon_1, \epsilon_2, \epsilon_1, \epsilon_3).$$

- $[\mathcal{M}_\tau] = q^3 - q^2.$
- $[\mathcal{G}_\tau] = (q - 1)^2 q^2.$
- $[\mathfrak{M}_\tau^{\text{irr}}] = q^2 - 4q + 4.$
- $[R(\tau)] = q^{17} - 4q^{16} + 3q^{15} + 3q^{14} - q^{13} + q^{12} - 7q^{11} + q^{10} + 3q^8 + 4q^7 - 4q^6$
- $m_\kappa(\tau) = 2.$

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$$\xi = ((2, 1), (1, 1), (1, 1)), \quad \sigma_A = (\epsilon_1, \epsilon_2, \epsilon_1, \epsilon_2), \quad \sigma_B = (\epsilon_2, \epsilon_3, \epsilon_1, \epsilon_1).$$

- $[\mathcal{M}_\tau] = (q^2 - q)^2.$
  - $[\mathcal{G}_\tau] = (q - 1)^3 q^2.$
  - $[\mathfrak{M}_\tau^{\text{irr}}] = q - 2.$
  - $[R(\tau)] = q^{16} - 2q^{15} - q^{14} + q^{13} + q^{12} + 3q^{11} - q^{10} - q^9 - 2q^8 - q^7 + 2q^6$
  - $m_\kappa(\tau) = 1.$
- 

$$\xi = ((1, 1), (1, 1), (2, 1)), \quad \sigma_A = (\epsilon_1, \epsilon_2, \epsilon_1, \epsilon_2), \quad \sigma_B = (\epsilon_1, \epsilon_2, \epsilon_1, \epsilon_3).$$

- $[\mathcal{M}_\tau] = q^3 - q^2.$
  - $[\mathcal{G}_\tau] = (q - 1)^3 q^2.$
  - $[\mathfrak{M}_\tau^{\text{irr}}] = q - 2.$
  - $[R(\tau)] = q^{15} - q^{14} - 2q^{13} - q^{12} + 3q^{10} + 2q^9 + q^8 - q^7 - 2q^6$
  - $m_\kappa(\tau) = 4.$
- 

$$\xi = ((1, 1), (1, 1), (2, 1)), \quad \sigma_A = (\epsilon_1, \epsilon_2, \epsilon_1, \epsilon_2), \quad \sigma_B = (\epsilon_1, \epsilon_1, \epsilon_3, \epsilon_2).$$

- $[\mathcal{M}_\tau] = q^4 - q^2.$
  - $[\mathcal{G}_\tau] = (q - 1)^3 q^2.$
  - $[\mathfrak{M}_\tau^{\text{irr}}] = q - 2.$
  - $[R(\tau)] = q^{16} - 3q^{14} - 3q^{13} - q^{12} + 3q^{11} + 5q^{10} + 3q^9 - 3q^7 - 2q^6$
  - $m_\kappa(\tau) = 1.$
- 

$$\xi = ((1, 1), (1, 1), (1, 1), (1, 1)), \quad \sigma_A = (\epsilon_1, \epsilon_2, \epsilon_1, \epsilon_2), \quad \sigma_B = (\epsilon_1, \epsilon_2, \epsilon_1, \epsilon_3).$$

- $[\mathcal{M}_\tau] = (q^2 - q)(q - 1).$
  - $[\mathcal{G}_\tau] = (q - 1)^4 q^2.$
  - $[\mathfrak{M}_\tau^{\text{irr}}] = 1.$
  - $[R(\tau)] = q^{13} + q^{12} - q^{10} - 2q^9 - q^8 + q^6 + q^5$
  - $m_\kappa(\tau) = 4.$
- 

$$\xi = ((1, 1), (1, 1), (1, 1), (1, 1)), \quad \sigma_A = (\epsilon_1, \epsilon_2, \epsilon_1, \epsilon_2), \quad \sigma_B = (\epsilon_1, \epsilon_1, \epsilon_3, \epsilon_2).$$

- $[\mathcal{M}_\tau] = (q^2 - q)^2.$
  - $[\mathcal{G}_\tau] = (q - 1)^4 q^2.$
  - $[\mathfrak{M}_\tau^{\text{irr}}] = 1.$
  - $[R(\tau)] = q^{14} + q^{13} - q^{11} - 2q^{10} - q^9 + q^7 + q^6$
  - $m_\kappa(\tau) = 2.$
- 

$$\xi = ((1, 1), (1, 1), (1, 1), (1, 1)), \quad \sigma_A = (\epsilon_1, \epsilon_2, \epsilon_1, \epsilon_2), \quad \sigma_B = (\epsilon_2, \epsilon_3, \epsilon_1, \epsilon_1).$$

- $[\mathcal{M}_\tau] = (q^2 - q)^2.$
- $[\mathcal{G}_\tau] = (q - 1)^4 q^2.$
- $[\mathfrak{M}_\tau^{\text{irr}}] = 1.$
- $[R(\tau)] = q^{14} + q^{13} - q^{11} - 2q^{10} - q^9 + q^7 + q^6$
- $m_\kappa(\tau) = 2.$

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$$\xi = ((2, 1), (1, 1), (1, 1)), \quad \sigma_A = (\epsilon_1, \epsilon_2, \epsilon_1, \epsilon_2), \quad \sigma_B = (\epsilon_2, \epsilon_1, \epsilon_3, \epsilon_1).$$

- $[\mathcal{M}_\tau] = (q^2 - q)(q - 1)q.$
  - $[\mathcal{G}_\tau] = (q - 1)^3 q^2.$
  - $[\mathfrak{M}_\tau^{\text{irr}}] = q - 2.$
  - $[R(\tau)] = q^{16} - 2q^{15} - q^{14} + q^{13} + q^{12} + 3q^{11} - q^{10} - q^9 - 2q^8 - q^7 + 2q^6$
  - $m_\kappa(\tau) = 4.$
- 

$$\xi = ((1, 1), (1, 1), (1, 1), (1, 1)), \quad \sigma_A = (\epsilon_1, \epsilon_2, \epsilon_1, \epsilon_2), \quad \sigma_B = (\epsilon_1, \epsilon_2, \epsilon_1, \epsilon_3).$$

- $[\mathcal{M}_\tau] = (q - 1)^2 q^2.$
  - $[\mathcal{G}_\tau] = (q - 1)^4 q^2.$
  - $[\mathfrak{M}_\tau^{\text{irr}}] = 1.$
  - $[R(\tau)] = q^{14} + q^{13} - q^{11} - 2q^{10} - q^9 + q^7 + q^6$
  - $m_\kappa(\tau) = 4.$
- 

$$\xi = ((1, 1), (1, 1), (1, 1), (1, 1)), \quad \sigma_A = (\epsilon_1, \epsilon_2, \epsilon_1, \epsilon_2), \quad \sigma_B = (\epsilon_2, \epsilon_1, \epsilon_3, \epsilon_1).$$

- $[\mathcal{M}_\tau] = (q^2 - q)(q - 1)q.$
  - $[\mathcal{G}_\tau] = (q - 1)^4 q^2.$
  - $[\mathfrak{M}_\tau^{\text{irr}}] = 1.$
  - $[R(\tau)] = q^{14} + q^{13} - q^{11} - 2q^{10} - q^9 + q^7 + q^6$
  - $m_\kappa(\tau) = 4.$
- 

$$\xi = ((1, 1), (1, 1), (1, 1), (1, 1)), \quad \sigma_A = (\epsilon_1, \epsilon_2, \epsilon_1, \epsilon_2), \quad \sigma_B = (\epsilon_1, \epsilon_3, \epsilon_2, \epsilon_1).$$

- $[\mathcal{M}_\tau] = (q^2 - q)(q - 1)q.$
  - $[\mathcal{G}_\tau] = (q - 1)^4 q^2.$
  - $[\mathfrak{M}_\tau^{\text{irr}}] = 1.$
  - $[R(\tau)] = q^{14} + q^{13} - q^{11} - 2q^{10} - q^9 + q^7 + q^6$
  - $m_\kappa(\tau) = 4.$
- 

$$\xi = ((1, 1), (1, 1), (1, 1), (1, 1)), \quad \sigma_A = (\epsilon_1, \epsilon_2, \epsilon_1, \epsilon_2), \quad \sigma_B = (\epsilon_1, \epsilon_1, \epsilon_3, \epsilon_2).$$

- $[\mathcal{M}_\tau] = (q^2 - q)(q - 1)q^2.$
  - $[\mathcal{G}_\tau] = (q - 1)^4 q^2.$
  - $[\mathfrak{M}_\tau^{\text{irr}}] = 1.$
  - $[R(\tau)] = q^{15} + q^{14} - q^{12} - 2q^{11} - q^{10} + q^8 + q^7$
  - $m_\kappa(\tau) = 4.$
- 

$$\xi = ((1, 1), (3, 1)), \quad \sigma_A = (\epsilon_1, \epsilon_1, \epsilon_2, \epsilon_2), \quad \sigma_B = (\epsilon_1, \epsilon_1, \epsilon_2, \epsilon_3).$$

- $[\mathcal{M}_\tau] = q^2 - q.$
- $[\mathcal{G}_\tau] = (q - 1)^2 q.$
- $[\mathfrak{M}_\tau^{\text{irr}}] = q^2 - 3q + 3.$
- $[R(\tau)] = q^{17} - 3q^{16} + 2q^{15} + 2q^{14} - q^{13} + q^{12} - 5q^{11} + q^{10} + 2q^8 + 3q^7 - 3q^6$
- $m_\kappa(\tau) = 2.$

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$$\xi = ((1,1),(2,1),(1,1)), \quad \sigma_A = (\epsilon_1, \epsilon_1, \epsilon_2, \epsilon_2), \quad \sigma_B = (\epsilon_2, \epsilon_3, \epsilon_1, \epsilon_1).$$

- $[\mathcal{M}_\tau] = (q^2 - q)(q - 1)$ .
  - $[\mathcal{G}_\tau] = (q - 1)^3 q$ .
  - $[\mathfrak{M}_\tau^{\text{irr}}] = q - 2$ .
  - $[R(\tau)] = q^{16} - 2q^{15} - q^{14} + q^{13} + q^{12} + 3q^{11} - q^{10} - q^9 - 2q^8 - q^7 + 2q^6$
  - $m_\kappa(\tau) = 4$ .
- 

$$\xi = ((1,1),(2,1),(1,1)), \quad \sigma_A = (\epsilon_1, \epsilon_1, \epsilon_2, \epsilon_2), \quad \sigma_B = (\epsilon_1, \epsilon_2, \epsilon_3, \epsilon_1).$$

- $[\mathcal{M}_\tau] = (q^2 - q)^2$ .
  - $[\mathcal{G}_\tau] = (q - 1)^3 q^2$ .
  - $[\mathfrak{M}_\tau^{\text{irr}}] = q - 2$ .
  - $[R(\tau)] = q^{16} - 2q^{15} - q^{14} + q^{13} + q^{12} + 3q^{11} - q^{10} - q^9 - 2q^8 - q^7 + 2q^6$
  - $m_\kappa(\tau) = 2$ .
- 

$$\xi = ((1,1),(1,1),(1,1),(1,1)), \quad \sigma_A = (\epsilon_1, \epsilon_2, \epsilon_2, \epsilon_1), \quad \sigma_B = (\epsilon_1, \epsilon_2, \epsilon_3, \epsilon_1).$$

- $[\mathcal{M}_\tau] = (q^2 - 1)(q - 1)^2$ .
  - $[\mathcal{G}_\tau] = (q - 1)^4 q$ .
  - $[\mathfrak{M}_\tau^{\text{irr}}] = 1$ .
  - $[R(\tau)] = q^{15} + q^{14} - q^{13} - 2q^{12} - 2q^{11} + 2q^9 + 2q^8 + q^7 - q^6 - q^5$
  - $m_\kappa(\tau) = 2$ .
- 

$$\xi = ((1,1),(1,1),(1,1),(1,1)), \quad \sigma_A = (\epsilon_1, \epsilon_2, \epsilon_2, \epsilon_1), \quad \sigma_B = (\epsilon_2, \epsilon_1, \epsilon_3, \epsilon_1).$$

- $[\mathcal{M}_\tau] = (q - 1)^3 q$ .
  - $[\mathcal{G}_\tau] = (q - 1)^4 q$ .
  - $[\mathfrak{M}_\tau^{\text{irr}}] = 1$ .
  - $[R(\tau)] = q^{15} - q^{13} - q^{12} - q^{11} + q^{10} + q^9 + q^8 - q^6$
  - $m_\kappa(\tau) = 4$ .
- 

$$\xi = ((1,1),(1,1),(2,1)), \quad \sigma_A = (\epsilon_1, \epsilon_2, \epsilon_1, \epsilon_2), \quad \sigma_B = (\epsilon_1, \epsilon_2, \epsilon_1, \epsilon_3).$$

- $[\mathcal{M}_\tau] = (q^2 - q)(q - 1)q$ .
  - $[\mathcal{G}_\tau] = (q - 1)^3 q^2$ .
  - $[\mathfrak{M}_\tau^{\text{irr}}] = q - 2$ .
  - $[R(\tau)] = q^{16} - 2q^{15} - q^{14} + q^{13} + q^{12} + 3q^{11} - q^{10} - q^9 - 2q^8 - q^7 + 2q^6$
  - $m_\kappa(\tau) = 4$ .
- 

$$\xi = ((1,1),(1,1),(1,1),(1,1)), \quad \sigma_A = (\epsilon_1, \epsilon_2, \epsilon_1, \epsilon_2), \quad \sigma_B = (\epsilon_1, \epsilon_2, \epsilon_1, \epsilon_3).$$

- $[\mathcal{M}_\tau] = (q - 1)^3 q^2$ .
- $[\mathcal{G}_\tau] = (q - 1)^4 q^2$ .
- $[\mathfrak{M}_\tau^{\text{irr}}] = 1$ .
- $[R(\tau)] = q^{15} - q^{13} - q^{12} - q^{11} + q^{10} + q^9 + q^8 - q^6$
- $m_\kappa(\tau) = 4$ .

---


$$\xi = ((1,1),(1,1),(1,1),(1,1)), \quad \sigma_A = (\epsilon_1, \epsilon_2, \epsilon_1, \epsilon_2), \quad \sigma_B = (\epsilon_2, \epsilon_1, \epsilon_3, \epsilon_1).$$

- $[\mathcal{M}_\tau] = (q-1)^3 q^2.$
  - $[\mathcal{G}_\tau] = (q-1)^4 q^2.$
  - $[\mathfrak{M}_\tau^{\text{irr}}] = 1.$
  - $[R(\tau)] = q^{15} - q^{13} - q^{12} - q^{11} + q^{10} + q^9 + q^8 - q^6$
  - $m_\kappa(\tau) = 4.$
- 

$$\xi = ((1,1),(1,1),(1,1),(1,1)), \quad \sigma_A = (\epsilon_1, \epsilon_2, \epsilon_1, \epsilon_2), \quad \sigma_B = (\epsilon_1, \epsilon_3, \epsilon_2, \epsilon_1).$$

- $[\mathcal{M}_\tau] = (q-1)^3 q^2.$
  - $[\mathcal{G}_\tau] = (q-1)^4 q^2.$
  - $[\mathfrak{M}_\tau^{\text{irr}}] = 1.$
  - $[R(\tau)] = q^{15} - q^{13} - q^{12} - q^{11} + q^{10} + q^9 + q^8 - q^6$
  - $m_\kappa(\tau) = 4.$
- 

**Total count of  $\kappa$**  =  $((\epsilon_1, \epsilon_1, \epsilon_2, \epsilon_2), (\varepsilon_1, \varepsilon_1, \varepsilon_2, \varepsilon_3))$

$$\begin{aligned} [R_\kappa^{\text{red}}] &= 6q^{17} + 3q^{16} + 13q^{15} + 17q^{14} + 11q^{13} + 14q^{12} + 5q^{10} + q^9 + q^8 + 5q^7 - 4q^6, \\ [R_\kappa^{\text{irr}}] &= q^{18} - 3q^{17} + 4q^{16} - 2q^{15} - 3q^{14} + 3q^{13} - 3q^{12} + 7q^{11} - 2q^{10} - q^8 - 5q^7 + 4q^6, \\ [R_\kappa] &= q^{18} + 3q^{17} + 7q^{16} + 11q^{15} + 14q^{14} + 14q^{13} + 11q^{12} + 7q^{11} + 3q^{10} + q^9, \\ [\mathfrak{M}_\kappa] &= q^3 - 3q^2 + 5q - 4. \end{aligned}$$

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 4. CONFIGURATION  $\boldsymbol{\epsilon} = (\epsilon_1, \epsilon_1, \epsilon_2, \epsilon_2)$  AND  $\boldsymbol{\varepsilon} = (\varepsilon_1, \varepsilon_2, \varepsilon_3, \varepsilon_4)$ 


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$$\xi = ((3, 1), (1, 1)), \quad \sigma_A = (\epsilon_1, \epsilon_1, \epsilon_2, \epsilon_2), \quad \sigma_B = (\epsilon_1, \epsilon_2, \epsilon_3, \epsilon_4).$$

- $[\mathcal{M}_\tau] = 1$ .
  - $[\mathcal{G}_\tau] = (q - 1)^2$ .
  - $[\mathfrak{M}_\tau^{\text{irr}}] = q^2 - 3q + 3$ .
  - $[R(\tau)] = q^{16} - 2q^{15} + 2q^{13} + q^{12} + 2q^{11} - 3q^{10} - 2q^9 - 2q^8 + 3q^6$
  - $m_\kappa(\tau) = 8$ .
- 

$$\xi = ((2, 1), (2, 1)), \quad \sigma_A = (\epsilon_1, \epsilon_2, \epsilon_1, \epsilon_2), \quad \sigma_B = (\epsilon_1, \epsilon_3, \epsilon_2, \epsilon_4).$$

- $[\mathcal{M}_\tau] = 1$ .
  - $[\mathcal{G}_\tau] = (q - 1)^2$ .
  - $[\mathfrak{M}_\tau^{\text{irr}}] = q^2 - 4q + 4$ .
  - $[R(\tau)] = q^{16} - 3q^{15} + 3q^{13} + 2q^{12} + 3q^{11} - 4q^{10} - 3q^9 - 3q^8 + 4q^6$
  - $m_\kappa(\tau) = 3$ .
- 

$$\xi = ((2, 1), (1, 1), (1, 1)), \quad \sigma_A = (\epsilon_1, \epsilon_2, \epsilon_1, \epsilon_2), \quad \sigma_B = (\epsilon_1, \epsilon_3, \epsilon_2, \epsilon_4).$$

- $[\mathcal{M}_\tau] = 1$ .
  - $[\mathcal{G}_\tau] = (q - 1)^3$ .
  - $[\mathfrak{M}_\tau^{\text{irr}}] = q - 2$ .
  - $[R(\tau)] = q^{14} - 2q^{12} - 3q^{11} - 3q^{10} + 2q^8 + 3q^7 + 2q^6$
  - $m_\kappa(\tau) = 12$ .
- 

$$\xi = ((1, 1), (1, 1), (1, 1), (1, 1)), \quad \sigma_A = (\epsilon_1, \epsilon_1, \epsilon_2, \epsilon_2), \quad \sigma_B = (\epsilon_1, \epsilon_2, \epsilon_3, \epsilon_4).$$

- $[\mathcal{M}_\tau] = 1$ .
  - $[\mathcal{G}_\tau] = (q - 1)^4$ .
  - $[\mathfrak{M}_\tau^{\text{irr}}] = 1$ .
  - $[R(\tau)] = q^{12} + 3q^{11} + 5q^{10} + 6q^9 + 5q^8 + 3q^7 + q^6$
  - $m_\kappa(\tau) = 6$ .
- 

$$\xi = ((3, 1), (1, 1)), \quad \sigma_A = (\epsilon_1, \epsilon_1, \epsilon_2, \epsilon_2), \quad \sigma_B = (\epsilon_1, \epsilon_2, \epsilon_3, \epsilon_4).$$

- $[\mathcal{M}_\tau] = q^3 - q$ .
  - $[\mathcal{G}_\tau] = (q - 1)^2 q$ .
  - $[\mathfrak{M}_\tau^{\text{irr}}] = q^2 - 3q + 3$ .
  - $[R(\tau)] = q^{18} - 2q^{17} - q^{16} + 4q^{15} + q^{14} - 4q^{12} - 4q^{11} + q^{10} + 2q^9 + 5q^8 - 3q^6$
  - $m_\kappa(\tau) = 8$ .
- 

$$\xi = ((2, 1), (1, 1), (1, 1)), \quad \sigma_A = (\epsilon_1, \epsilon_2, \epsilon_1, \epsilon_2), \quad \sigma_B = (\epsilon_1, \epsilon_3, \epsilon_2, \epsilon_4).$$

- $[\mathcal{M}_\tau] = q^3 - q$ .
- $[\mathcal{G}_\tau] = (q - 1)^3 q$ .
- $[\mathfrak{M}_\tau^{\text{irr}}] = q - 2$ .
- $[R(\tau)] = q^{16} - 3q^{14} - 3q^{13} - q^{12} + 3q^{11} + 5q^{10} + 3q^9 - 3q^7 - 2q^6$
- $m_\kappa(\tau) = 24$ .

$$\xi = ((1,1),(1,1),(1,1),(1,1)), \quad \sigma_A = (\epsilon_1, \epsilon_1, \epsilon_2, \epsilon_2), \quad \sigma_B = (\epsilon_1, \epsilon_2, \epsilon_3, \epsilon_4).$$

- $[\mathcal{M}_\tau] = q^3 - q.$
- $[\mathcal{G}_\tau] = (q-1)^4 q.$
- $[\mathfrak{M}_\tau^{\text{irr}}] = 1.$
- $[R(\tau)] = q^{14} + 3q^{13} + 4q^{12} + 3q^{11} - 3q^9 - 4q^8 - 3q^7 - q^6$
- $m_\kappa(\tau) = 24.$

$$\xi = ((1,1),(1,1),(1,1),(1,1)), \quad \sigma_A = (\epsilon_1, \epsilon_1, \epsilon_2, \epsilon_2), \quad \sigma_B = (\epsilon_1, \epsilon_2, \epsilon_3, \epsilon_4).$$

- $[\mathcal{M}_\tau] = (q^2 - 1)^2.$
- $[\mathcal{G}_\tau] = (q-1)^4.$
- $[\mathfrak{M}_\tau^{\text{irr}}] = 1.$
- $[R(\tau)] = q^{16} + 3q^{15} + 3q^{14} - 4q^{12} - 6q^{11} - 4q^{10} + 3q^8 + 3q^7 + q^6$
- $m_\kappa(\tau) = 12.$

$$\xi = ((2,1),(2,1)), \quad \sigma_A = (\epsilon_1, \epsilon_2, \epsilon_1, \epsilon_2), \quad \sigma_B = (\epsilon_1, \epsilon_3, \epsilon_2, \epsilon_4).$$

- $[\mathcal{M}_\tau] = q^4 - q^2.$
- $[\mathcal{G}_\tau] = (q-1)^2 q^2.$
- $[\mathfrak{M}_\tau^{\text{irr}}] = q^2 - 4q + 4.$
- $[R(\tau)] = q^{18} - 3q^{17} - q^{16} + 6q^{15} + 2q^{14} - 6q^{12} - 6q^{11} + q^{10} + 3q^9 + 7q^8 - 4q^6$
- $m_\kappa(\tau) = 6.$

$$\xi = ((2,1),(1,1),(1,1)), \quad \sigma_A = (\epsilon_1, \epsilon_2, \epsilon_1, \epsilon_2), \quad \sigma_B = (\epsilon_1, \epsilon_3, \epsilon_2, \epsilon_4).$$

- $[\mathcal{M}_\tau] = (q^2 - q)^2.$
- $[\mathcal{G}_\tau] = (q-1)^3 q^2.$
- $[\mathfrak{M}_\tau^{\text{irr}}] = q - 2.$
- $[R(\tau)] = q^{16} - 2q^{15} - q^{14} + q^{13} + q^{12} + 3q^{11} - q^{10} - q^9 - 2q^8 - q^7 + 2q^6$
- $m_\kappa(\tau) = 12.$

$$\xi = ((1,1),(1,1),(2,1)), \quad \sigma_A = (\epsilon_1, \epsilon_2, \epsilon_1, \epsilon_2), \quad \sigma_B = (\epsilon_1, \epsilon_3, \epsilon_2, \epsilon_4).$$

- $[\mathcal{M}_\tau] = q^4 - q^2.$
- $[\mathcal{G}_\tau] = (q-1)^3 q^2.$
- $[\mathfrak{M}_\tau^{\text{irr}}] = q - 2.$
- $[R(\tau)] = q^{16} - 3q^{14} - 3q^{13} - q^{12} + 3q^{11} + 5q^{10} + 3q^9 - 3q^7 - 2q^6$
- $m_\kappa(\tau) = 12.$

$$\xi = ((1,1),(1,1),(1,1),(1,1)), \quad \sigma_A = (\epsilon_1, \epsilon_2, \epsilon_1, \epsilon_2), \quad \sigma_B = (\epsilon_1, \epsilon_3, \epsilon_2, \epsilon_4).$$

- $[\mathcal{M}_\tau] = (q^2 - q)^2.$
- $[\mathcal{G}_\tau] = (q-1)^4 q^2.$
- $[\mathfrak{M}_\tau^{\text{irr}}] = 1.$
- $[R(\tau)] = q^{14} + q^{13} - q^{11} - 2q^{10} - q^9 + q^7 + q^6$
- $m_\kappa(\tau) = 24.$

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$$\xi = ((2, 1), (1, 1), (1, 1)), \quad \sigma_A = (\epsilon_1, \epsilon_2, \epsilon_1, \epsilon_2), \quad \sigma_B = (\epsilon_1, \epsilon_3, \epsilon_2, \epsilon_4).$$

- $[\mathcal{M}_\tau] = (q^2 - q)(q - 1)q^2.$
  - $[\mathcal{G}_\tau] = (q - 1)^3 q^2.$
  - $[\mathfrak{M}_\tau^{\text{irr}}] = q - 2.$
  - $[R(\tau)] = q^{17} - 2q^{16} - q^{15} + q^{14} + q^{13} + 3q^{12} - q^{11} - q^{10} - 2q^9 - q^8 + 2q^7$
  - $m_\kappa(\tau) = 24.$
- 

$$\xi = ((1, 1), (1, 1), (1, 1), (1, 1)), \quad \sigma_A = (\epsilon_1, \epsilon_2, \epsilon_1, \epsilon_2), \quad \sigma_B = (\epsilon_1, \epsilon_3, \epsilon_2, \epsilon_4).$$

- $[\mathcal{M}_\tau] = (q^2 - q)(q - 1)q^2.$
  - $[\mathcal{G}_\tau] = (q - 1)^4 q^2.$
  - $[\mathfrak{M}_\tau^{\text{irr}}] = 1.$
  - $[R(\tau)] = q^{15} + q^{14} - q^{12} - 2q^{11} - q^{10} + q^8 + q^7$
  - $m_\kappa(\tau) = 48.$
- 

$$\xi = ((1, 1), (3, 1)), \quad \sigma_A = (\epsilon_1, \epsilon_1, \epsilon_2, \epsilon_2), \quad \sigma_B = (\epsilon_1, \epsilon_2, \epsilon_3, \epsilon_4).$$

- $[\mathcal{M}_\tau] = q^3 - q.$
  - $[\mathcal{G}_\tau] = (q - 1)^2 q.$
  - $[\mathfrak{M}_\tau^{\text{irr}}] = q^2 - 3q + 3.$
  - $[R(\tau)] = q^{18} - 2q^{17} - q^{16} + 4q^{15} + q^{14} - 4q^{12} - 4q^{11} + q^{10} + 2q^9 + 5q^8 - 3q^6$
  - $m_\kappa(\tau) = 8.$
- 

$$\xi = ((1, 1), (2, 1), (1, 1)), \quad \sigma_A = (\epsilon_1, \epsilon_1, \epsilon_2, \epsilon_2), \quad \sigma_B = (\epsilon_1, \epsilon_2, \epsilon_3, \epsilon_4).$$

- $[\mathcal{M}_\tau] = (q^2 - q)(q - 1).$
  - $[\mathcal{G}_\tau] = (q - 1)^3 q.$
  - $[\mathfrak{M}_\tau^{\text{irr}}] = q - 2.$
  - $[R(\tau)] = q^{16} - 2q^{15} - q^{14} + q^{13} + q^{12} + 3q^{11} - q^{10} - q^9 - 2q^8 - q^7 + 2q^6$
  - $m_\kappa(\tau) = 24.$
- 

$$\xi = ((1, 1), (2, 1), (1, 1)), \quad \sigma_A = (\epsilon_1, \epsilon_1, \epsilon_2, \epsilon_2), \quad \sigma_B = (\epsilon_1, \epsilon_2, \epsilon_3, \epsilon_4).$$

- $[\mathcal{M}_\tau] = (q^2 - q)^2 q.$
  - $[\mathcal{G}_\tau] = (q - 1)^3 q^2.$
  - $[\mathfrak{M}_\tau^{\text{irr}}] = q - 2.$
  - $[R(\tau)] = q^{17} - 2q^{16} - q^{15} + q^{14} + q^{13} + 3q^{12} - q^{11} - q^{10} - 2q^9 - q^8 + 2q^7$
  - $m_\kappa(\tau) = 24.$
- 

$$\xi = ((1, 1), (1, 1), (1, 1), (1, 1)), \quad \sigma_A = (\epsilon_1, \epsilon_2, \epsilon_2, \epsilon_1), \quad \sigma_B = (\epsilon_1, \epsilon_3, \epsilon_4, \epsilon_2).$$

- $[\mathcal{M}_\tau] = (q^2 - 1)(q - 1)^2 q.$
- $[\mathcal{G}_\tau] = (q - 1)^4 q.$
- $[\mathfrak{M}_\tau^{\text{irr}}] = 1.$
- $[R(\tau)] = q^{16} + q^{15} - q^{14} - 2q^{13} - 2q^{12} + 2q^{10} + 2q^9 + q^8 - q^7 - q^6$
- $m_\kappa(\tau) = 24.$

---


$$\xi = ((1,1), (1,1), (2,1)), \quad \sigma_A = (\epsilon_1, \epsilon_2, \epsilon_1, \epsilon_2), \quad \sigma_B = (\epsilon_1, \epsilon_3, \epsilon_2, \epsilon_4).$$

- $[\mathcal{M}_\tau] = (q^2 - q)(q - 1)q^2.$
  - $[\mathcal{G}_\tau] = (q - 1)^3 q^2.$
  - $[\mathfrak{M}_\tau^{\text{irr}}] = q - 2.$
  - $[R(\tau)] = q^{17} - 2q^{16} - q^{15} + q^{14} + q^{13} + 3q^{12} - q^{11} - q^{10} - 2q^9 - q^8 + 2q^7$
  - $m_\kappa(\tau) = 24.$
- 

$$\xi = ((1,1), (1,1), (1,1), (1,1)), \quad \sigma_A = (\epsilon_1, \epsilon_2, \epsilon_1, \epsilon_2), \quad \sigma_B = (\epsilon_1, \epsilon_3, \epsilon_2, \epsilon_4).$$

- $[\mathcal{M}_\tau] = (q - 1)^3 q^3.$
  - $[\mathcal{G}_\tau] = (q - 1)^4 q^2.$
  - $[\mathfrak{M}_\tau^{\text{irr}}] = 1.$
  - $[R(\tau)] = q^{16} - q^{14} - q^{13} - q^{12} + q^{11} + q^{10} + q^9 - q^7$
  - $m_\kappa(\tau) = 48.$
- 

**Total count of  $\kappa = ((\epsilon_1, \epsilon_1, \epsilon_2, \epsilon_2), (\varepsilon_1, \varepsilon_2, \varepsilon_3, \varepsilon_4))$**

$$\begin{aligned} [R_\kappa^{\text{red}}] &= 22q^{18} + 22q^{17} + q^{16} + 39q^{15} + 28q^{14} + 25q^{13} + 16q^{12} - 21q^{11} + 4q^{10} - \\ &11q^9 + 19q^8 + 18q^7 - 18q^6, \\ [R_\kappa^{\text{irr}}] &= q^{20} + 4q^{19} - 12q^{18} - 4q^{17} + 24q^{16} - 11q^{15} - 3q^{14} - 7q^{13} - 6q^{12} + 25q^{11} - \\ 3q^{10} + 11q^9 - 19q^8 - 18q^7 + 18q^6, \\ [R_\kappa] &= q^{20} + 4q^{19} + 10q^{18} + 18q^{17} + 25q^{16} + 28q^{15} + 25q^{14} + 18q^{13} + 10q^{12} + \\ 4q^{11} + q^{10}, \\ [\mathfrak{M}_\kappa] &= q^5 + 4q^4 - 11q^3 + q^2 + 18q - 18. \end{aligned}$$

5. CONFIGURATION  $\boldsymbol{\epsilon} = (\epsilon_1, \epsilon_1, \epsilon_2, \epsilon_3)$  AND  $\boldsymbol{\varepsilon} = (\varepsilon_1, \varepsilon_1, \varepsilon_2, \varepsilon_2)$

---

$$\xi = ((3, 1), (1, 1)), \quad \sigma_A = (\epsilon_1, \epsilon_2, \epsilon_3, \epsilon_1), \quad \sigma_B = (\epsilon_1, \epsilon_2, \epsilon_2, \epsilon_1).$$

- $[\mathcal{M}_\tau] = 1.$
  - $[\mathcal{G}_\tau] = (q - 1)^2.$
  - $[\mathfrak{M}_\tau^{\text{irr}}] = q^2 - 3q + 3.$
  - $[R(\tau)] = q^{16} - 2q^{15} + 2q^{13} + q^{12} + 2q^{11} - 3q^{10} - 2q^9 - 2q^8 + 3q^6$
  - $m_\kappa(\tau) = 2.$
- 

$$\xi = ((2, 1), (2, 1)), \quad \sigma_A = (\epsilon_1, \epsilon_2, \epsilon_1, \epsilon_3), \quad \sigma_B = (\epsilon_1, \epsilon_2, \epsilon_1, \epsilon_2).$$

- $[\mathcal{M}_\tau] = 1.$
  - $[\mathcal{G}_\tau] = (q - 1)^2.$
  - $[\mathfrak{M}_\tau^{\text{irr}}] = q^2 - 4q + 4.$
  - $[R(\tau)] = q^{16} - 3q^{15} + 3q^{13} + 2q^{12} + 3q^{11} - 4q^{10} - 3q^9 - 3q^8 + 4q^6$
  - $m_\kappa(\tau) = 1.$
- 

$$\xi = ((2, 1), (1, 1), (1, 1)), \quad \sigma_A = (\epsilon_1, \epsilon_2, \epsilon_1, \epsilon_3), \quad \sigma_B = (\epsilon_1, \epsilon_2, \epsilon_1, \epsilon_2).$$

- $[\mathcal{M}_\tau] = 1.$
  - $[\mathcal{G}_\tau] = (q - 1)^3.$
  - $[\mathfrak{M}_\tau^{\text{irr}}] = q - 2.$
  - $[R(\tau)] = q^{14} - 2q^{12} - 3q^{11} - 3q^{10} + 2q^8 + 3q^7 + 2q^6$
  - $m_\kappa(\tau) = 4.$
- 

$$\xi = ((1, 1), (1, 1), (2, 1)), \quad \sigma_A = (\epsilon_1, \epsilon_1, \epsilon_2, \epsilon_3), \quad \sigma_B = (\epsilon_1, \epsilon_2, \epsilon_2, \epsilon_1).$$

- $[\mathcal{M}_\tau] = 1.$
  - $[\mathcal{G}_\tau] = (q - 1)^3.$
  - $[\mathfrak{M}_\tau^{\text{irr}}] = q - 2.$
  - $[R(\tau)] = q^{14} - 2q^{12} - 3q^{11} - 3q^{10} + 2q^8 + 3q^7 + 2q^6$
  - $m_\kappa(\tau) = 1.$
- 

$$\xi = ((1, 2), (1, 1), (1, 1)), \quad \sigma_A = (\epsilon_1, \epsilon_2, \epsilon_3), \quad \sigma_B = (\epsilon_1, \epsilon_2, \epsilon_2).$$

- $[\mathcal{M}_\tau] = 1.$
  - $[\mathcal{G}_\tau] = (q + 1)(q - 1)^4 q.$
  - $[\mathfrak{M}_\tau^{\text{irr}}] = 1.$
  - $[R(\tau)] = q^{10} + 2q^9 + 3q^8 + 3q^7 + 2q^6 + q^5$
  - $m_\kappa(\tau) = 2.$
- 

$$\xi = ((1, 1), (1, 1), (1, 1), (1, 1)), \quad \sigma_A = (\epsilon_1, \epsilon_1, \epsilon_2, \epsilon_3), \quad \sigma_B = (\epsilon_1, \epsilon_2, \epsilon_2, \epsilon_1).$$

- $[\mathcal{M}_\tau] = 1.$
- $[\mathcal{G}_\tau] = (q - 1)^4.$
- $[\mathfrak{M}_\tau^{\text{irr}}] = 1.$
- $[R(\tau)] = q^{12} + 3q^{11} + 5q^{10} + 6q^9 + 5q^8 + 3q^7 + q^6$
- $m_\kappa(\tau) = 2.$

---


$$\xi = ((2, 1), (1, 1), (1, 1)), \quad \sigma_A = (\epsilon_1, \epsilon_2, \epsilon_1, \epsilon_3), \quad \sigma_B = (\epsilon_1, \epsilon_2, \epsilon_1, \epsilon_2).$$

- $[\mathcal{M}_\tau] = q^2 - 1.$
  - $[\mathcal{G}_\tau] = (q - 1)^3.$
  - $[\mathfrak{M}_\tau^{\text{irr}}] = q - 2.$
  - $[R(\tau)] = q^{16} - 3q^{14} - 3q^{13} - q^{12} + 3q^{11} + 5q^{10} + 3q^9 - 3q^7 - 2q^6$
  - $m_\kappa(\tau) = 4.$
- 

$$\xi = ((1, 2), (1, 1), (1, 1)), \quad \sigma_A = (\epsilon_1, \epsilon_2, \epsilon_3), \quad \sigma_B = (\epsilon_1, \epsilon_2, \epsilon_2).$$

- $[\mathcal{M}_\tau] = q^2 - 1.$
  - $[\mathcal{G}_\tau] = (q + 1)(q - 1)^4 q.$
  - $[\mathfrak{M}_\tau^{\text{irr}}] = 1.$
  - $[R(\tau)] = q^{12} + 2q^{11} + 2q^{10} + q^9 - q^8 - 2q^7 - 2q^6 - q^5$
  - $m_\kappa(\tau) = 4.$
- 

$$\xi = ((1, 1), (1, 1), (1, 1), (1, 1)), \quad \sigma_A = (\epsilon_1, \epsilon_1, \epsilon_2, \epsilon_3), \quad \sigma_B = (\epsilon_1, \epsilon_2, \epsilon_2, \epsilon_1).$$

- $[\mathcal{M}_\tau] = q^2 - 1.$
  - $[\mathcal{G}_\tau] = (q - 1)^4.$
  - $[\mathfrak{M}_\tau^{\text{irr}}] = 1.$
  - $[R(\tau)] = q^{14} + 3q^{13} + 4q^{12} + 3q^{11} - 3q^9 - 4q^8 - 3q^7 - q^6$
  - $m_\kappa(\tau) = 4.$
- 

$$\xi = ((3, 1), (1, 1)), \quad \sigma_A = (\epsilon_1, \epsilon_2, \epsilon_3, \epsilon_1), \quad \sigma_B = (\epsilon_1, \epsilon_2, \epsilon_2, \epsilon_1).$$

- $[\mathcal{M}_\tau] = q^2 - q.$
  - $[\mathcal{G}_\tau] = (q - 1)^2 q.$
  - $[\mathfrak{M}_\tau^{\text{irr}}] = q^2 - 3q + 3.$
  - $[R(\tau)] = q^{17} - 3q^{16} + 2q^{15} + 2q^{14} - q^{13} + q^{12} - 5q^{11} + q^{10} + 2q^8 + 3q^7 - 3q^6$
  - $m_\kappa(\tau) = 2.$
- 

$$\xi = ((2, 1), (1, 1), (1, 1)), \quad \sigma_A = (\epsilon_1, \epsilon_2, \epsilon_3, \epsilon_1), \quad \sigma_B = (\epsilon_1, \epsilon_2, \epsilon_2, \epsilon_1).$$

- $[\mathcal{M}_\tau] = q^2 - q.$
  - $[\mathcal{G}_\tau] = (q - 1)^3 q.$
  - $[\mathfrak{M}_\tau^{\text{irr}}] = q - 2.$
  - $[R(\tau)] = q^{15} - q^{14} - 2q^{13} - q^{12} + 3q^{10} + 2q^9 + q^8 - q^7 - 2q^6$
  - $m_\kappa(\tau) = 4.$
- 

$$\xi = ((1, 1), (2, 1), (1, 1)), \quad \sigma_A = (\epsilon_1, \epsilon_2, \epsilon_3, \epsilon_1), \quad \sigma_B = (\epsilon_1, \epsilon_2, \epsilon_1, \epsilon_2).$$

- $[\mathcal{M}_\tau] = q^2 - q.$
- $[\mathcal{G}_\tau] = (q - 1)^3 q.$
- $[\mathfrak{M}_\tau^{\text{irr}}] = q - 2.$
- $[R(\tau)] = q^{15} - q^{14} - 2q^{13} - q^{12} + 3q^{10} + 2q^9 + q^8 - q^7 - 2q^6$
- $m_\kappa(\tau) = 2.$

---


$$\xi = ((1,1),(1,1),(1,1),(1,1)), \quad \sigma_A = (\epsilon_1, \epsilon_2, \epsilon_3, \epsilon_1), \quad \sigma_B = (\epsilon_1, \epsilon_2, \epsilon_2, \epsilon_1).$$

- $[\mathcal{M}_\tau] = q^2 - 1.$
  - $[\mathcal{G}_\tau] = (q-1)^4 q.$
  - $[\mathfrak{M}_\tau^{\text{irr}}] = 1.$
  - $[R(\tau)] = q^{13} + 3q^{12} + 4q^{11} + 3q^{10} - 3q^8 - 4q^7 - 3q^6 - q^5$
  - $m_\kappa(\tau) = 2.$
- 

$$\xi = ((1,1),(1,1),(1,1),(1,1)), \quad \sigma_A = (\epsilon_1, \epsilon_2, \epsilon_3, \epsilon_1), \quad \sigma_B = (\epsilon_1, \epsilon_2, \epsilon_1, \epsilon_2).$$

- $[\mathcal{M}_\tau] = q^2 - q.$
  - $[\mathcal{G}_\tau] = (q-1)^4 q.$
  - $[\mathfrak{M}_\tau^{\text{irr}}] = 1.$
  - $[R(\tau)] = q^{13} + 2q^{12} + 2q^{11} + q^{10} - q^9 - 2q^8 - 2q^7 - q^6$
  - $m_\kappa(\tau) = 4.$
- 

$$\xi = ((1,1),(1,1),(2,1)), \quad \sigma_A = (\epsilon_1, \epsilon_1, \epsilon_2, \epsilon_3), \quad \sigma_B = (\epsilon_1, \epsilon_2, \epsilon_2, \epsilon_1).$$

- $[\mathcal{M}_\tau] = q^2 - 1.$
  - $[\mathcal{G}_\tau] = (q-1)^3.$
  - $[\mathfrak{M}_\tau^{\text{irr}}] = q - 2.$
  - $[R(\tau)] = q^{16} - 3q^{14} - 3q^{13} - q^{12} + 3q^{11} + 5q^{10} + 3q^9 - 3q^7 - 2q^6$
  - $m_\kappa(\tau) = 1.$
- 

$$\xi = ((1,2),(1,1),(1,1)), \quad \sigma_A = (\epsilon_1, \epsilon_2, \epsilon_3), \quad \sigma_B = (\epsilon_1, \epsilon_2, \epsilon_2).$$

- $[\mathcal{M}_\tau] = (q^2 - 1)^2.$
  - $[\mathcal{G}_\tau] = (q+1)(q-1)^4 q.$
  - $[\mathfrak{M}_\tau^{\text{irr}}] = 1.$
  - $[R(\tau)] = q^{14} + 2q^{13} + q^{12} - q^{11} - 3q^{10} - 3q^9 - q^8 + q^7 + 2q^6 + q^5$
  - $m_\kappa(\tau) = 2.$
- 

$$\xi = ((1,1),(1,1),(1,1),(1,1)), \quad \sigma_A = (\epsilon_1, \epsilon_1, \epsilon_2, \epsilon_3), \quad \sigma_B = (\epsilon_1, \epsilon_2, \epsilon_2, \epsilon_1).$$

- $[\mathcal{M}_\tau] = (q-1)^2.$
  - $[\mathcal{G}_\tau] = (q-1)^4.$
  - $[\mathfrak{M}_\tau^{\text{irr}}] = 1.$
  - $[R(\tau)] = q^{14} + q^{13} - q^{11} - 2q^{10} - q^9 + q^7 + q^6$
  - $m_\kappa(\tau) = 2.$
- 

$$\xi = ((2,1),(2,1)), \quad \sigma_A = (\epsilon_1, \epsilon_2, \epsilon_1, \epsilon_3), \quad \sigma_B = (\epsilon_1, \epsilon_2, \epsilon_1, \epsilon_2).$$

- $[\mathcal{M}_\tau] = q^2 - q.$
- $[\mathcal{G}_\tau] = (q-1)^2 q.$
- $[\mathfrak{M}_\tau^{\text{irr}}] = q^2 - 4q + 4.$
- $[R(\tau)] = q^{17} - 4q^{16} + 3q^{15} + 3q^{14} - q^{13} + q^{12} - 7q^{11} + q^{10} + 3q^8 + 4q^7 - 4q^6$
- $m_\kappa(\tau) = 2.$

$$\xi = ((1, 1), (1, 1), (2, 1)), \quad \sigma_A = (\epsilon_1, \epsilon_2, \epsilon_1, \epsilon_3), \quad \sigma_B = (\epsilon_1, \epsilon_2, \epsilon_1, \epsilon_2).$$

- $[\mathcal{M}_\tau] = q^2 - q.$
  - $[\mathcal{G}_\tau] = (q - 1)^3 q.$
  - $[\mathfrak{M}_\tau^{\text{irr}}] = q - 2.$
  - $[R(\tau)] = q^{15} - q^{14} - 2q^{13} - q^{12} + 3q^{10} + 2q^9 + q^8 - q^7 - 2q^6$
  - $m_\kappa(\tau) = 4.$
- 

$$\xi = ((1, 1), (1, 1), (1, 1), (1, 1)), \quad \sigma_A = (\epsilon_1, \epsilon_2, \epsilon_1, \epsilon_3), \quad \sigma_B = (\epsilon_1, \epsilon_2, \epsilon_1, \epsilon_2).$$

- $[\mathcal{M}_\tau] = (q - 1)^2.$
  - $[\mathcal{G}_\tau] = (q - 1)^4 q.$
  - $[\mathfrak{M}_\tau^{\text{irr}}] = 1.$
  - $[R(\tau)] = q^{13} + q^{12} - q^{10} - 2q^9 - q^8 + q^6 + q^5$
  - $m_\kappa(\tau) = 4.$
- 

$$\xi = ((1, 1), (1, 1), (1, 1), (1, 1)), \quad \sigma_A = (\epsilon_1, \epsilon_2, \epsilon_1, \epsilon_3), \quad \sigma_B = (\epsilon_1, \epsilon_1, \epsilon_2, \epsilon_2).$$

- $[\mathcal{M}_\tau] = (q^2 - q)(q^2 - 1).$
  - $[\mathcal{G}_\tau] = (q - 1)^4 q.$
  - $[\mathfrak{M}_\tau^{\text{irr}}] = 1.$
  - $[R(\tau)] = q^{15} + 2q^{14} + q^{13} - q^{12} - 3q^{11} - 3q^{10} - q^9 + q^8 + 2q^7 + q^6$
  - $m_\kappa(\tau) = 4.$
- 

$$\xi = ((2, 1), (1, 1), (1, 1)), \quad \sigma_A = (\epsilon_2, \epsilon_3, \epsilon_1, \epsilon_1), \quad \sigma_B = (\epsilon_2, \epsilon_1, \epsilon_1, \epsilon_2).$$

- $[\mathcal{M}_\tau] = (q - 1)^2.$
  - $[\mathcal{G}_\tau] = (q - 1)^3.$
  - $[\mathfrak{M}_\tau^{\text{irr}}] = q - 2.$
  - $[R(\tau)] = q^{16} - 2q^{15} - q^{14} + q^{13} + q^{12} + 3q^{11} - q^{10} - q^9 - 2q^8 - q^7 + 2q^6$
  - $m_\kappa(\tau) = 1.$
- 

$$\xi = ((1, 1), (1, 1), (1, 2)), \quad \sigma_A = (\epsilon_2, \epsilon_3, \epsilon_1), \quad \sigma_B = (\epsilon_2, \epsilon_2, \epsilon_1).$$

- $[\mathcal{M}_\tau] = q^4 - q^3 - q^2 + q.$
  - $[\mathcal{G}_\tau] = (q + 1)(q - 1)^4 q.$
  - $[\mathfrak{M}_\tau^{\text{irr}}] = 1.$
  - $[R(\tau)] = q^{14} + q^{13} - q^{11} - 2q^{10} - q^9 + q^7 + q^6$
  - $m_\kappa(\tau) = 2.$
- 

$$\xi = ((1, 1), (1, 1), (1, 1), (1, 1)), \quad \sigma_A = (\epsilon_2, \epsilon_3, \epsilon_1, \epsilon_1), \quad \sigma_B = (\epsilon_2, \epsilon_1, \epsilon_1, \epsilon_2).$$

- $[\mathcal{M}_\tau] = (q - 1)^2.$
- $[\mathcal{G}_\tau] = (q - 1)^4.$
- $[\mathfrak{M}_\tau^{\text{irr}}] = 1.$
- $[R(\tau)] = q^{14} + q^{13} - q^{11} - 2q^{10} - q^9 + q^7 + q^6$
- $m_\kappa(\tau) = 2.$

---


$$\xi = ((1, 1), (1, 1), (1, 1), (1, 1)), \quad \sigma_A = (\epsilon_1, \epsilon_1, \epsilon_2, \epsilon_3), \quad \sigma_B = (\epsilon_1, \epsilon_2, \epsilon_2, \epsilon_1).$$

- $[\mathcal{M}_\tau] = (q - 1)^2 q.$
  - $[\mathcal{G}_\tau] = (q - 1)^4.$
  - $[\mathfrak{M}_\tau^{\text{irr}}] = 1.$
  - $[R(\tau)] = q^{15} + q^{14} - q^{12} - 2q^{11} - q^{10} + q^8 + q^7$
  - $m_\kappa(\tau) = 4.$
- 

$$\xi = ((1, 1), (1, 1), (1, 1), (1, 1)), \quad \sigma_A = (\epsilon_1, \epsilon_2, \epsilon_1, \epsilon_3), \quad \sigma_B = (\epsilon_1, \epsilon_2, \epsilon_1, \epsilon_2).$$

- $[\mathcal{M}_\tau] = (q - 1)^2 q.$
  - $[\mathcal{G}_\tau] = (q - 1)^4 q.$
  - $[\mathfrak{M}_\tau^{\text{irr}}] = 1.$
  - $[R(\tau)] = q^{14} + q^{13} - q^{11} - 2q^{10} - q^9 + q^7 + q^6$
  - $m_\kappa(\tau) = 4.$
- 

$$\xi = ((2, 1), (1, 1), (1, 1)), \quad \sigma_A = (\epsilon_1, \epsilon_2, \epsilon_3, \epsilon_1), \quad \sigma_B = (\epsilon_1, \epsilon_2, \epsilon_2, \epsilon_1).$$

- $[\mathcal{M}_\tau] = (q - 1)^2 q.$
  - $[\mathcal{G}_\tau] = (q - 1)^3 q.$
  - $[\mathfrak{M}_\tau^{\text{irr}}] = q - 2.$
  - $[R(\tau)] = q^{16} - 2q^{15} - q^{14} + q^{13} + q^{12} + 3q^{11} - q^{10} - q^9 - 2q^8 - q^7 + 2q^6$
  - $m_\kappa(\tau) = 4.$
- 

$$\xi = ((1, 1), (1, 1), (1, 1), (1, 1)), \quad \sigma_A = (\epsilon_1, \epsilon_2, \epsilon_3, \epsilon_1), \quad \sigma_B = (\epsilon_1, \epsilon_2, \epsilon_2, \epsilon_1).$$

- $[\mathcal{M}_\tau] = (q - 1)^2 q.$
  - $[\mathcal{G}_\tau] = (q - 1)^4 q.$
  - $[\mathfrak{M}_\tau^{\text{irr}}] = 1.$
  - $[R(\tau)] = q^{14} + q^{13} - q^{11} - 2q^{10} - q^9 + q^7 + q^6$
  - $m_\kappa(\tau) = 4.$
- 

$$\xi = ((1, 1), (1, 1), (1, 1), (1, 1)), \quad \sigma_A = (\epsilon_1, \epsilon_2, \epsilon_3, \epsilon_1), \quad \sigma_B = (\epsilon_1, \epsilon_2, \epsilon_1, \epsilon_2).$$

- $[\mathcal{M}_\tau] = (q - 1)^2 q.$
  - $[\mathcal{G}_\tau] = (q - 1)^4 q.$
  - $[\mathfrak{M}_\tau^{\text{irr}}] = 1.$
  - $[R(\tau)] = q^{14} + q^{13} - q^{11} - 2q^{10} - q^9 + q^7 + q^6$
  - $m_\kappa(\tau) = 4.$
- 

$$\xi = ((1, 1), (3, 1)), \quad \sigma_A = (\epsilon_1, \epsilon_1, \epsilon_2, \epsilon_3), \quad \sigma_B = (\epsilon_1, \epsilon_1, \epsilon_2, \epsilon_2).$$

- $[\mathcal{M}_\tau] = q^2 - q.$
- $[\mathcal{G}_\tau] = (q - 1)^2 q.$
- $[\mathfrak{M}_\tau^{\text{irr}}] = q^2 - 3q + 3.$
- $[R(\tau)] = q^{17} - 3q^{16} + 2q^{15} + 2q^{14} - q^{13} + q^{12} - 5q^{11} + q^{10} + 2q^8 + 3q^7 - 3q^6$
- $m_\kappa(\tau) = 2.$

---


$$\xi = ((1, 1), (2, 1), (1, 1)), \quad \sigma_A = (\epsilon_2, \epsilon_1, \epsilon_3, \epsilon_1), \quad \sigma_B = (\epsilon_2, \epsilon_1, \epsilon_2, \epsilon_1).$$

- $[\mathcal{M}_\tau] = (q - 1)^2$ .
  - $[\mathcal{G}_\tau] = (q - 1)^3$ .
  - $[\mathfrak{M}_\tau^{\text{irr}}] = q - 2$ .
  - $[R(\tau)] = q^{16} - 2q^{15} - q^{14} + q^{13} + q^{12} + 3q^{11} - q^{10} - q^9 - 2q^8 - q^7 + 2q^6$
  - $m_\kappa(\tau) = 4$ .
- 

$$\xi = ((1, 1), (2, 1), (1, 1)), \quad \sigma_A = (\epsilon_1, \epsilon_2, \epsilon_3, \epsilon_1), \quad \sigma_B = (\epsilon_1, \epsilon_2, \epsilon_1, \epsilon_2).$$

- $[\mathcal{M}_\tau] = (q - 1)^2 q$ .
  - $[\mathcal{G}_\tau] = (q - 1)^3 q$ .
  - $[\mathfrak{M}_\tau^{\text{irr}}] = q - 2$ .
  - $[R(\tau)] = q^{16} - 2q^{15} - q^{14} + q^{13} + q^{12} + 3q^{11} - q^{10} - q^9 - 2q^8 - q^7 + 2q^6$
  - $m_\kappa(\tau) = 2$ .
- 

$$\xi = ((1, 1), (1, 1), (1, 1), (1, 1)), \quad \sigma_A = (\epsilon_1, \epsilon_2, \epsilon_3, \epsilon_1), \quad \sigma_B = (\epsilon_1, \epsilon_2, \epsilon_2, \epsilon_1).$$

- $[\mathcal{M}_\tau] = (q^2 - 1)(q - 1)^2$ .
  - $[\mathcal{G}_\tau] = (q - 1)^4 q$ .
  - $[\mathfrak{M}_\tau^{\text{irr}}] = 1$ .
  - $[R(\tau)] = q^{15} + q^{14} - q^{13} - 2q^{12} - 2q^{11} + 2q^9 + 2q^8 + q^7 - q^6 - q^5$
  - $m_\kappa(\tau) = 2$ .
- 

$$\xi = ((1, 1), (1, 1), (1, 1), (1, 1)), \quad \sigma_A = (\epsilon_2, \epsilon_1, \epsilon_3, \epsilon_1), \quad \sigma_B = (\epsilon_2, \epsilon_1, \epsilon_1, \epsilon_2).$$

- $[\mathcal{M}_\tau] = (q^2 - q)(q - 1)^2$ .
  - $[\mathcal{G}_\tau] = (q - 1)^4 q$ .
  - $[\mathfrak{M}_\tau^{\text{irr}}] = 1$ .
  - $[R(\tau)] = q^{15} - q^{13} - q^{12} - q^{11} + q^{10} + q^9 + q^8 - q^6$
  - $m_\kappa(\tau) = 4$ .
- 

$$\xi = ((1, 1), (1, 1), (2, 1)), \quad \sigma_A = (\epsilon_1, \epsilon_2, \epsilon_1, \epsilon_3), \quad \sigma_B = (\epsilon_1, \epsilon_2, \epsilon_1, \epsilon_2).$$

- $[\mathcal{M}_\tau] = (q - 1)^2 q$ .
  - $[\mathcal{G}_\tau] = (q - 1)^3 q$ .
  - $[\mathfrak{M}_\tau^{\text{irr}}] = q - 2$ .
  - $[R(\tau)] = q^{16} - 2q^{15} - q^{14} + q^{13} + q^{12} + 3q^{11} - q^{10} - q^9 - 2q^8 - q^7 + 2q^6$
  - $m_\kappa(\tau) = 4$ .
- 

$$\xi = ((1, 1), (1, 1), (1, 1), (1, 1)), \quad \sigma_A = (\epsilon_1, \epsilon_2, \epsilon_1, \epsilon_3), \quad \sigma_B = (\epsilon_1, \epsilon_2, \epsilon_1, \epsilon_2).$$

- $[\mathcal{M}_\tau] = (q - 1)^3 q$ .
- $[\mathcal{G}_\tau] = (q - 1)^4 q$ .
- $[\mathfrak{M}_\tau^{\text{irr}}] = 1$ .
- $[R(\tau)] = q^{15} - q^{13} - q^{12} - q^{11} + q^{10} + q^9 + q^8 - q^6$
- $m_\kappa(\tau) = 4$ .

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$$\xi = ((1,1),(1,1),(1,1),(1,1)), \quad \sigma_A = (\epsilon_1, \epsilon_2, \epsilon_3, \epsilon_1), \quad \sigma_B = (\epsilon_1, \epsilon_2, \epsilon_1, \epsilon_2).$$

- $[\mathcal{M}_\tau] = (q-1)^3 q.$
  - $[\mathcal{G}_\tau] = (q-1)^4 q.$
  - $[\mathfrak{M}_\tau^{\text{irr}}] = 1.$
  - $[R(\tau)] = q^{15} - q^{13} - q^{12} - q^{11} + q^{10} + q^9 + q^8 - q^6$
  - $m_\kappa(\tau) = 4.$
- 

$$\xi = ((1,1),(1,1),(1,1),(1,1)), \quad \sigma_A = (\epsilon_2, \epsilon_1, \epsilon_3, \epsilon_1), \quad \sigma_B = (\epsilon_2, \epsilon_1, \epsilon_2, \epsilon_1).$$

- $[\mathcal{M}_\tau] = (q-1)^3 q.$
  - $[\mathcal{G}_\tau] = (q-1)^4 q.$
  - $[\mathfrak{M}_\tau^{\text{irr}}] = 1.$
  - $[R(\tau)] = q^{15} - q^{13} - q^{12} - q^{11} + q^{10} + q^9 + q^8 - q^6$
  - $m_\kappa(\tau) = 4.$
- 

**Total count of  $\kappa$**  =  $((\epsilon_1, \epsilon_1, \epsilon_2, \epsilon_3), (\varepsilon_1, \varepsilon_1, \varepsilon_2, \varepsilon_2))$

$$\begin{aligned} [R_\kappa^{\text{red}}] &= 6q^{17} + 3q^{16} + 13q^{15} + 17q^{14} + 11q^{13} + 14q^{12} + 5q^{10} + q^9 + q^8 + 5q^7 - 4q^6, \\ [R_\kappa^{\text{irr}}] &= q^{18} - 3q^{17} + 4q^{16} - 2q^{15} - 3q^{14} + 3q^{13} - 3q^{12} + 7q^{11} - 2q^{10} - q^8 - 5q^7 + 4q^6, \\ [R_\kappa] &= q^{18} + 3q^{17} + 7q^{16} + 11q^{15} + 14q^{14} + 14q^{13} + 11q^{12} + 7q^{11} + 3q^{10} + q^9, \\ [\mathfrak{M}_\kappa] &= q^3 - 3q^2 + 5q - 4. \end{aligned}$$

6. CONFIGURATION  $\epsilon = (\epsilon_1, \epsilon_1, \epsilon_2, \epsilon_3)$  AND  $\varepsilon = (\varepsilon_1, \varepsilon_1, \varepsilon_2, \varepsilon_3)$ 

$$\xi = ((3, 1), (1, 1)), \quad \sigma_A = (\epsilon_1, \epsilon_1, \epsilon_2, \epsilon_3), \quad \sigma_B = (\epsilon_2, \epsilon_3, \epsilon_1, \epsilon_1).$$

- $[\mathcal{M}_\tau] = 1$ .
- $[\mathcal{G}_\tau] = (q - 1)^2$ .
- $[\mathfrak{M}_\tau^{\text{irr}}] = q^2 - 3q + 3$ .
- $[R(\tau)] = q^{16} - 2q^{15} + 2q^{13} + q^{12} + 2q^{11} - 3q^{10} - 2q^9 - 2q^8 + 3q^6$
- $m_\kappa(\tau) = 2$ .

$$\xi = ((3, 1), (1, 1)), \quad \sigma_A = (\epsilon_1, \epsilon_2, \epsilon_3, \epsilon_1), \quad \sigma_B = (\epsilon_1, \epsilon_2, \epsilon_3, \epsilon_1).$$

- $[\mathcal{M}_\tau] = 1$ .
- $[\mathcal{G}_\tau] = (q - 1)^2$ .
- $[\mathfrak{M}_\tau^{\text{irr}}] = q^4 + 4q^3 - 9q^2 - 3q + 12$ .
- $[R(\tau)] = q^{18} + 5q^{17} - 5q^{16} - 13q^{15} + 3q^{14} + 12q^{13} + 17q^{12} + 4q^{11} - 16q^{10} - 17q^9 - 12q^8 + 9q^7 + 12q^6$
- $m_\kappa(\tau) = 1$ .

$$\xi = ((3, 1), (1, 1)), \quad \sigma_A = (\epsilon_1, \epsilon_2, \epsilon_3, \epsilon_1), \quad \sigma_B = (\epsilon_2, \epsilon_1, \epsilon_1, \epsilon_3).$$

- $[\mathcal{M}_\tau] = 1$ .
- $[\mathcal{G}_\tau] = (q - 1)^2$ .
- $[\mathfrak{M}_\tau^{\text{irr}}] = q^2 - 3q + 3$ .
- $[R(\tau)] = q^{16} - 2q^{15} + 2q^{13} + q^{12} + 2q^{11} - 3q^{10} - 2q^9 - 2q^8 + 3q^6$
- $m_\kappa(\tau) = 2$ .

$$\xi = ((2, 1), (2, 1)), \quad \sigma_A = (\epsilon_1, \epsilon_2, \epsilon_1, \epsilon_3), \quad \sigma_B = (\epsilon_1, \epsilon_2, \epsilon_1, \epsilon_3).$$

- $[\mathcal{M}_\tau] = 1$ .
- $[\mathcal{G}_\tau] = (q - 1)^2$ .
- $[\mathfrak{M}_\tau^{\text{irr}}] = q^2 - 4q + 4$ .
- $[R(\tau)] = q^{16} - 3q^{15} + 3q^{13} + 2q^{12} + 3q^{11} - 4q^{10} - 3q^9 - 3q^8 + 4q^6$
- $m_\kappa(\tau) = 2$ .

$$\xi = ((2, 1), (1, 1), (1, 1)), \quad \sigma_A = (\epsilon_1, \epsilon_2, \epsilon_1, \epsilon_3), \quad \sigma_B = (\epsilon_1, \epsilon_2, \epsilon_1, \epsilon_3).$$

- $[\mathcal{M}_\tau] = 1$ .
- $[\mathcal{G}_\tau] = (q - 1)^3$ .
- $[\mathfrak{M}_\tau^{\text{irr}}] = q - 2$ .
- $[R(\tau)] = q^{14} - 2q^{12} - 3q^{11} - 3q^{10} + 2q^8 + 3q^7 + 2q^6$
- $m_\kappa(\tau) = 4$ .

$$\xi = ((2, 1), (1, 1), (1, 1)), \quad \sigma_A = (\epsilon_1, \epsilon_2, \epsilon_1, \epsilon_3), \quad \sigma_B = (\epsilon_2, \epsilon_1, \epsilon_3, \epsilon_1).$$

- $[\mathcal{M}_\tau] = 1$ .
- $[\mathcal{G}_\tau] = (q - 1)^3$ .
- $[\mathfrak{M}_\tau^{\text{irr}}] = q - 2$ .
- $[R(\tau)] = q^{14} - 2q^{12} - 3q^{11} - 3q^{10} + 2q^8 + 3q^7 + 2q^6$
- $m_\kappa(\tau) = 4$ .

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$$\xi = ((2, 1), (1, 1), (1, 1)), \quad \sigma_A = (\epsilon_1, \epsilon_2, \epsilon_1, \epsilon_3), \quad \sigma_B = (\epsilon_2, \epsilon_3, \epsilon_1, \epsilon_1).$$

- $[\mathcal{M}_\tau] = 1.$
  - $[\mathcal{G}_\tau] = (q - 1)^3.$
  - $[\mathfrak{M}_\tau^{\text{irr}}] = q - 2.$
  - $[R(\tau)] = q^{14} - 2q^{12} - 3q^{11} - 3q^{10} + 2q^8 + 3q^7 + 2q^6$
  - $m_\kappa(\tau) = 2.$
- 

$$\xi = ((1, 2), (2, 1)), \quad \sigma_A = (\epsilon_1, \epsilon_2, \epsilon_3), \quad \sigma_B = (\epsilon_1, \epsilon_2, \epsilon_3).$$

- $[\mathcal{M}_\tau] = 1.$
  - $[\mathcal{G}_\tau] = (q + 1)(q - 1)^3 q.$
  - $[\mathfrak{M}_\tau^{\text{irr}}] = q - 2.$
  - $[R(\tau)] = q^{12} - q^{11} - q^{10} - 2q^9 - q^8 + q^7 + q^6 + 2q^5$
  - $m_\kappa(\tau) = 1.$
- 

$$\xi = ((1, 1), (1, 1), (2, 1)), \quad \sigma_A = (\epsilon_1, \epsilon_1, \epsilon_2, \epsilon_3), \quad \sigma_B = (\epsilon_1, \epsilon_2, \epsilon_3, \epsilon_1).$$

- $[\mathcal{M}_\tau] = 1.$
  - $[\mathcal{G}_\tau] = (q - 1)^3.$
  - $[\mathfrak{M}_\tau^{\text{irr}}] = q - 2.$
  - $[R(\tau)] = q^{14} - 2q^{12} - 3q^{11} - 3q^{10} + 2q^8 + 3q^7 + 2q^6$
  - $m_\kappa(\tau) = 2.$
- 

$$\xi = ((1, 2), (1, 1), (1, 1)), \quad \sigma_A = (\epsilon_1, \epsilon_2, \epsilon_3), \quad \sigma_B = (\epsilon_1, \epsilon_2, \epsilon_3).$$

- $[\mathcal{M}_\tau] = 1.$
  - $[\mathcal{G}_\tau] = (q + 1)(q - 1)^4 q.$
  - $[\mathfrak{M}_\tau^{\text{irr}}] = 1.$
  - $[R(\tau)] = q^{10} + 2q^9 + 3q^8 + 3q^7 + 2q^6 + q^5$
  - $m_\kappa(\tau) = 2.$
- 

$$\xi = ((1, 1), (1, 1), (1, 1), (1, 1)), \quad \sigma_A = (\epsilon_1, \epsilon_1, \epsilon_2, \epsilon_3), \quad \sigma_B = (\epsilon_2, \epsilon_3, \epsilon_1, \epsilon_1).$$

- $[\mathcal{M}_\tau] = 1.$
  - $[\mathcal{G}_\tau] = (q - 1)^4.$
  - $[\mathfrak{M}_\tau^{\text{irr}}] = 1.$
  - $[R(\tau)] = q^{12} + 3q^{11} + 5q^{10} + 6q^9 + 5q^8 + 3q^7 + q^6$
  - $m_\kappa(\tau) = 1.$
- 

$$\xi = ((1, 1), (1, 1), (1, 1), (1, 1)), \quad \sigma_A = (\epsilon_1, \epsilon_1, \epsilon_2, \epsilon_3), \quad \sigma_B = (\epsilon_1, \epsilon_2, \epsilon_3, \epsilon_1).$$

- $[\mathcal{M}_\tau] = 1.$
- $[\mathcal{G}_\tau] = (q - 1)^4.$
- $[\mathfrak{M}_\tau^{\text{irr}}] = 1.$
- $[R(\tau)] = q^{12} + 3q^{11} + 5q^{10} + 6q^9 + 5q^8 + 3q^7 + q^6$
- $m_\kappa(\tau) = 4.$

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$$\xi = ((3, 1), (1, 1)), \quad \sigma_A = (\epsilon_1, \epsilon_1, \epsilon_2, \epsilon_3), \quad \sigma_B = (\epsilon_2, \epsilon_3, \epsilon_1, \epsilon_1).$$

- $[\mathcal{M}_\tau] = q^2 - 1.$
  - $[\mathcal{G}_\tau] = (q - 1)^2.$
  - $[\mathfrak{M}_\tau^{\text{irr}}] = q^2 - 3q + 3.$
  - $[R(\tau)] = q^{18} - 2q^{17} - q^{16} + 4q^{15} + q^{14} - 4q^{12} - 4q^{11} + q^{10} + 2q^9 + 5q^8 - 3q^6$
  - $m_\kappa(\tau) = 2.$
- 

$$\xi = ((2, 1), (1, 1), (1, 1)), \quad \sigma_A = (\epsilon_1, \epsilon_2, \epsilon_1, \epsilon_3), \quad \sigma_B = (\epsilon_1, \epsilon_2, \epsilon_1, \epsilon_3).$$

- $[\mathcal{M}_\tau] = q^3 - 1.$
  - $[\mathcal{G}_\tau] = (q - 1)^3.$
  - $[\mathfrak{M}_\tau^{\text{irr}}] = q - 2.$
  - $[R(\tau)] = q^{17} - 2q^{15} - 4q^{14} - 3q^{13} + 2q^{12} + 5q^{11} + 6q^{10} + 2q^9 - 2q^8 - 3q^7 - 2q^6$
  - $m_\kappa(\tau) = 4.$
- 

$$\xi = ((2, 1), (1, 1), (1, 1)), \quad \sigma_A = (\epsilon_1, \epsilon_2, \epsilon_1, \epsilon_3), \quad \sigma_B = (\epsilon_2, \epsilon_1, \epsilon_3, \epsilon_1).$$

- $[\mathcal{M}_\tau] = q^2 - 1.$
  - $[\mathcal{G}_\tau] = (q - 1)^3.$
  - $[\mathfrak{M}_\tau^{\text{irr}}] = q - 2.$
  - $[R(\tau)] = q^{16} - 3q^{14} - 3q^{13} - q^{12} + 3q^{11} + 5q^{10} + 3q^9 - 3q^7 - 2q^6$
  - $m_\kappa(\tau) = 4.$
- 

$$\xi = ((2, 1), (1, 1), (1, 1)), \quad \sigma_A = (\epsilon_1, \epsilon_2, \epsilon_1, \epsilon_3), \quad \sigma_B = (\epsilon_2, \epsilon_3, \epsilon_1, \epsilon_1).$$

- $[\mathcal{M}_\tau] = q^2 - 1.$
  - $[\mathcal{G}_\tau] = (q - 1)^3.$
  - $[\mathfrak{M}_\tau^{\text{irr}}] = q - 2.$
  - $[R(\tau)] = q^{16} - 3q^{14} - 3q^{13} - q^{12} + 3q^{11} + 5q^{10} + 3q^9 - 3q^7 - 2q^6$
  - $m_\kappa(\tau) = 2.$
- 

$$\xi = ((1, 2), (1, 1), (1, 1)), \quad \sigma_A = (\epsilon_1, \epsilon_2, \epsilon_3), \quad \sigma_B = (\epsilon_1, \epsilon_2, \epsilon_3).$$

- $[\mathcal{M}_\tau] = q^3 - 1.$
  - $[\mathcal{G}_\tau] = (q + 1)(q - 1)^4 q.$
  - $[\mathfrak{M}_\tau^{\text{irr}}] = 1.$
  - $[R(\tau)] = q^{13} + 2q^{12} + 3q^{11} + 2q^{10} - 2q^8 - 3q^7 - 2q^6 - q^5$
  - $m_\kappa(\tau) = 4.$
- 

$$\xi = ((1, 1), (1, 1), (1, 1), (1, 1)), \quad \sigma_A = (\epsilon_1, \epsilon_1, \epsilon_2, \epsilon_3), \quad \sigma_B = (\epsilon_2, \epsilon_3, \epsilon_1, \epsilon_1).$$

- $[\mathcal{M}_\tau] = q^2 - 1.$
- $[\mathcal{G}_\tau] = (q - 1)^4.$
- $[\mathfrak{M}_\tau^{\text{irr}}] = 1.$
- $[R(\tau)] = q^{14} + 3q^{13} + 4q^{12} + 3q^{11} - 3q^9 - 4q^8 - 3q^7 - q^6$
- $m_\kappa(\tau) = 2.$

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$$\xi = ((1,1),(1,1),(1,1),(1,1)), \quad \sigma_A = (\epsilon_1, \epsilon_1, \epsilon_2, \epsilon_3), \quad \sigma_B = (\epsilon_1, \epsilon_2, \epsilon_3, \epsilon_1).$$

- $[\mathcal{M}_\tau] = q^2 - 1.$
  - $[\mathcal{G}_\tau] = (q-1)^4.$
  - $[\mathfrak{M}_\tau^{\text{irr}}] = 1.$
  - $[R(\tau)] = q^{14} + 3q^{13} + 4q^{12} + 3q^{11} - 3q^9 - 4q^8 - 3q^7 - q^6$
  - $m_\kappa(\tau) = 4.$
- 

$$\xi = ((1,1),(1,1),(1,1),(1,1)), \quad \sigma_A = (\epsilon_1, \epsilon_1, \epsilon_2, \epsilon_3), \quad \sigma_B = (\epsilon_2, \epsilon_1, \epsilon_1, \epsilon_3).$$

- $[\mathcal{M}_\tau] = q^3 - 1.$
  - $[\mathcal{G}_\tau] = (q-1)^4.$
  - $[\mathfrak{M}_\tau^{\text{irr}}] = 1.$
  - $[R(\tau)] = q^{15} + 3q^{14} + 5q^{13} + 5q^{12} + 2q^{11} - 2q^{10} - 5q^9 - 5q^8 - 3q^7 - q^6$
  - $m_\kappa(\tau) = 4.$
- 

$$\xi = ((3,1),(1,1)), \quad \sigma_A = (\epsilon_1, \epsilon_2, \epsilon_3, \epsilon_1), \quad \sigma_B = (\epsilon_1, \epsilon_2, \epsilon_3, \epsilon_1).$$

- $[\mathcal{M}_\tau] = q^2 - q.$
  - $[\mathcal{G}_\tau] = (q-1)^2 q.$
  - $[\mathfrak{M}_\tau^{\text{irr}}] = q^4 + 4q^3 - 9q^2 - 3q + 12.$
  - $[R(\tau)] = q^{19} + 4q^{18} - 10q^{17} - 8q^{16} + 16q^{15} + 9q^{14} + 5q^{13} - 13q^{12} - 20q^{11} - q^{10} + 5q^9 + 21q^8 + 3q^7 - 12q^6$
  - $m_\kappa(\tau) = 1.$
- 

$$\xi = ((3,1),(1,1)), \quad \sigma_A = (\epsilon_1, \epsilon_2, \epsilon_3, \epsilon_1), \quad \sigma_B = (\epsilon_2, \epsilon_1, \epsilon_1, \epsilon_3).$$

- $[\mathcal{M}_\tau] = q^3 - q.$
  - $[\mathcal{G}_\tau] = (q-1)^2 q.$
  - $[\mathfrak{M}_\tau^{\text{irr}}] = q^2 - 3q + 3.$
  - $[R(\tau)] = q^{18} - 2q^{17} - q^{16} + 4q^{15} + q^{14} - 4q^{12} - 4q^{11} + q^{10} + 2q^9 + 5q^8 - 3q^6$
  - $m_\kappa(\tau) = 2.$
- 

$$\xi = ((2,1),(1,1),(1,1)), \quad \sigma_A = (\epsilon_1, \epsilon_2, \epsilon_3, \epsilon_1), \quad \sigma_B = (\epsilon_1, \epsilon_2, \epsilon_3, \epsilon_1).$$

- $[\mathcal{M}_\tau] = q^2 - q.$
  - $[\mathcal{G}_\tau] = (q-1)^3 q.$
  - $[\mathfrak{M}_\tau^{\text{irr}}] = q - 2.$
  - $[R(\tau)] = q^{15} - q^{14} - 2q^{13} - q^{12} + 3q^{10} + 2q^9 + q^8 - q^7 - 2q^6$
  - $m_\kappa(\tau) = 4.$
- 

$$\xi = ((2,1),(1,1),(1,1)), \quad \sigma_A = (\epsilon_1, \epsilon_2, \epsilon_3, \epsilon_1), \quad \sigma_B = (\epsilon_2, \epsilon_1, \epsilon_1, \epsilon_3).$$

- $[\mathcal{M}_\tau] = q^3 - q.$
- $[\mathcal{G}_\tau] = (q-1)^3 q.$
- $[\mathfrak{M}_\tau^{\text{irr}}] = q - 2.$
- $[R(\tau)] = q^{16} - 3q^{14} - 3q^{13} - q^{12} + 3q^{11} + 5q^{10} + 3q^9 - 3q^7 - 2q^6$
- $m_\kappa(\tau) = 4.$

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$$\xi = ((2, 1), (1, 1), (1, 1)), \quad \sigma_A = (\epsilon_1, \epsilon_2, \epsilon_3, \epsilon_1), \quad \sigma_B = (\epsilon_2, \epsilon_3, \epsilon_1, \epsilon_1).$$

- $[\mathcal{M}_\tau] = q^2 - q.$
  - $[\mathcal{G}_\tau] = (q - 1)^3 q.$
  - $[\mathfrak{M}_\tau^{\text{irr}}] = q - 2.$
  - $[R(\tau)] = q^{15} - q^{14} - 2q^{13} - q^{12} + 3q^{10} + 2q^9 + q^8 - q^7 - 2q^6$
  - $m_\kappa(\tau) = 2.$
- 

$$\xi = ((1, 1), (2, 1), (1, 1)), \quad \sigma_A = (\epsilon_1, \epsilon_2, \epsilon_3, \epsilon_1), \quad \sigma_B = (\epsilon_1, \epsilon_2, \epsilon_3, \epsilon_1).$$

- $[\mathcal{M}_\tau] = q^2 - 1.$
  - $[\mathcal{G}_\tau] = (q - 1)^3 q.$
  - $[\mathfrak{M}_\tau^{\text{irr}}] = q - 2.$
  - $[R(\tau)] = q^{15} - 3q^{13} - 3q^{12} - q^{11} + 3q^{10} + 5q^9 + 3q^8 - 3q^6 - 2q^5$
  - $m_\kappa(\tau) = 1.$
- 

$$\xi = ((1, 1), (2, 1), (1, 1)), \quad \sigma_A = (\epsilon_1, \epsilon_2, \epsilon_3, \epsilon_1), \quad \sigma_B = (\epsilon_1, \epsilon_3, \epsilon_1, \epsilon_2).$$

- $[\mathcal{M}_\tau] = q^3 - q.$
  - $[\mathcal{G}_\tau] = (q - 1)^3 q.$
  - $[\mathfrak{M}_\tau^{\text{irr}}] = q - 2.$
  - $[R(\tau)] = q^{16} - 3q^{14} - 3q^{13} - q^{12} + 3q^{11} + 5q^{10} + 3q^9 - 3q^7 - 2q^6$
  - $m_\kappa(\tau) = 2.$
- 

$$\xi = ((1, 1), (2, 1), (1, 1)), \quad \sigma_A = (\epsilon_1, \epsilon_2, \epsilon_3, \epsilon_1), \quad \sigma_B = (\epsilon_2, \epsilon_1, \epsilon_3, \epsilon_1).$$

- $[\mathcal{M}_\tau] = q^2 - q.$
  - $[\mathcal{G}_\tau] = (q - 1)^4 q.$
  - $[\mathfrak{M}_\tau^{\text{irr}}] = 1.$
  - $[R(\tau)] = q^{15} - q^{14} - 2q^{13} - q^{12} + 3q^{10} + 2q^9 + q^8 - q^7 - 2q^6$
  - $m_\kappa(\tau) = 2.$
- 

$$\xi = ((1, 1), (1, 1), (1, 1), (1, 1)), \quad \sigma_A = (\epsilon_1, \epsilon_2, \epsilon_3, \epsilon_1), \quad \sigma_B = (\epsilon_1, \epsilon_2, \epsilon_3, \epsilon_1).$$

- $[\mathcal{M}_\tau] = q^2 - 1.$
  - $[\mathcal{G}_\tau] = (q - 1)^4 q.$
  - $[\mathfrak{M}_\tau^{\text{irr}}] = 1.$
  - $[R(\tau)] = q^{13} + 3q^{12} + 4q^{11} + 3q^{10} - 3q^8 - 4q^7 - 3q^6 - q^5$
  - $m_\kappa(\tau) = 2.$
- 

$$\xi = ((1, 1), (1, 1), (1, 1), (1, 1)), \quad \sigma_A = (\epsilon_1, \epsilon_2, \epsilon_3, \epsilon_1), \quad \sigma_B = (\epsilon_2, \epsilon_1, \epsilon_1, \epsilon_3).$$

- $[\mathcal{M}_\tau] = q^3 - q.$
- $[\mathcal{G}_\tau] = (q - 1)^4 q.$
- $[\mathfrak{M}_\tau^{\text{irr}}] = 1.$
- $[R(\tau)] = q^{14} + 3q^{13} + 4q^{12} + 3q^{11} - 3q^9 - 4q^8 - 3q^7 - q^6$
- $m_\kappa(\tau) = 2.$

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$$\xi = ((1,1),(1,1),(1,1),(1,1)), \quad \sigma_A = (\epsilon_1, \epsilon_2, \epsilon_3, \epsilon_1), \quad \sigma_B = (\epsilon_1, \epsilon_3, \epsilon_1, \epsilon_2).$$

- $[\mathcal{M}_\tau] = q^3 - q.$
  - $[\mathcal{G}_\tau] = (q-1)^4 q.$
  - $[\mathfrak{M}_\tau^{\text{irr}}] = 1.$
  - $[R(\tau)] = q^{14} + 3q^{13} + 4q^{12} + 3q^{11} - 3q^9 - 4q^8 - 3q^7 - q^6$
  - $m_\kappa(\tau) = 4.$
- 

$$\xi = ((1,1),(1,1),(1,1),(1,1)), \quad \sigma_A = (\epsilon_1, \epsilon_2, \epsilon_3, \epsilon_1), \quad \sigma_B = (\epsilon_2, \epsilon_1, \epsilon_3, \epsilon_1).$$

- $[\mathcal{M}_\tau] = q^2 - q.$
  - $[\mathcal{G}_\tau] = (q-1)^4 q.$
  - $[\mathfrak{M}_\tau^{\text{irr}}] = 1.$
  - $[R(\tau)] = q^{13} + 2q^{12} + 2q^{11} + q^{10} - q^9 - 2q^8 - 2q^7 - q^6$
  - $m_\kappa(\tau) = 4.$
- 

$$\xi = ((1,2),(2,1)), \quad \sigma_A = (\epsilon_1, \epsilon_2, \epsilon_3), \quad \sigma_B = (\epsilon_1, \epsilon_2, \epsilon_3).$$

- $[\mathcal{M}_\tau] = q^4 - 1.$
  - $[\mathcal{G}_\tau] = (q+1)(q-1)^3 q.$
  - $[\mathfrak{M}_\tau^{\text{irr}}] = q - 2.$
  - $[R(\tau)] = q^{16} - q^{15} - q^{14} - 2q^{13} - 2q^{12} + 2q^{11} + 2q^{10} + 4q^9 + q^8 - q^7 - q^6 - 2q^5$
  - $m_\kappa(\tau) = 1.$
- 

$$\xi = ((1,1),(1,1),(2,1)), \quad \sigma_A = (\epsilon_1, \epsilon_1, \epsilon_2, \epsilon_3), \quad \sigma_B = (\epsilon_1, \epsilon_2, \epsilon_3, \epsilon_1).$$

- $[\mathcal{M}_\tau] = q^3 - 1.$
  - $[\mathcal{G}_\tau] = (q-1)^3.$
  - $[\mathfrak{M}_\tau^{\text{irr}}] = q - 2.$
  - $[R(\tau)] = q^{17} - 2q^{15} - 4q^{14} - 3q^{13} + 2q^{12} + 5q^{11} + 6q^{10} + 2q^9 - 2q^8 - 3q^7 - 2q^6$
  - $m_\kappa(\tau) = 2.$
- 

$$\xi = ((1,2),(1,1),(1,1)), \quad \sigma_A = (\epsilon_1, \epsilon_2, \epsilon_3), \quad \sigma_B = (\epsilon_1, \epsilon_2, \epsilon_3).$$

- $[\mathcal{M}_\tau] = (q^2 - 1)^2.$
  - $[\mathcal{G}_\tau] = (q+1)(q-1)^4 q.$
  - $[\mathfrak{M}_\tau^{\text{irr}}] = 1.$
  - $[R(\tau)] = q^{14} + 2q^{13} + q^{12} - q^{11} - 3q^{10} - 3q^9 - q^8 + q^7 + 2q^6 + q^5$
  - $m_\kappa(\tau) = 2.$
- 

$$\xi = ((1,1),(1,1),(1,1),(1,1)), \quad \sigma_A = (\epsilon_1, \epsilon_1, \epsilon_2, \epsilon_3), \quad \sigma_B = (\epsilon_2, \epsilon_3, \epsilon_1, \epsilon_1).$$

- $[\mathcal{M}_\tau] = (q^2 - 1)^2.$
- $[\mathcal{G}_\tau] = (q-1)^4.$
- $[\mathfrak{M}_\tau^{\text{irr}}] = 1.$
- $[R(\tau)] = q^{16} + 3q^{15} + 3q^{14} - 4q^{12} - 6q^{11} - 4q^{10} + 3q^8 + 3q^7 + q^6$
- $m_\kappa(\tau) = 1.$

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$$\xi = ((1,1),(1,1),(1,1),(1,1)), \quad \sigma_A = (\epsilon_1, \epsilon_1, \epsilon_2, \epsilon_3), \quad \sigma_B = (\epsilon_1, \epsilon_2, \epsilon_3, \epsilon_1).$$

- $[\mathcal{M}_\tau] = (q^2 - 1)(q - 1)$ .
  - $[\mathcal{G}_\tau] = (q - 1)^4$ .
  - $[\mathfrak{M}_\tau^{\text{irr}}] = 1$ .
  - $[R(\tau)] = q^{15} + 2q^{14} + q^{13} - q^{12} - 3q^{11} - 3q^{10} - q^9 + q^8 + 2q^7 + q^6$
  - $m_\kappa(\tau) = 4$ .
- 

$$\xi = ((2,1),(2,1)), \quad \sigma_A = (\epsilon_1, \epsilon_2, \epsilon_1, \epsilon_3), \quad \sigma_B = (\epsilon_1, \epsilon_2, \epsilon_1, \epsilon_3).$$

- $[\mathcal{M}_\tau] = q^3 - q$ .
  - $[\mathcal{G}_\tau] = (q - 1)^2 q$ .
  - $[\mathfrak{M}_\tau^{\text{irr}}] = q^2 - 4q + 4$ .
  - $[R(\tau)] = q^{18} - 3q^{17} - q^{16} + 6q^{15} + 2q^{14} - 6q^{12} - 6q^{11} + q^{10} + 3q^9 + 7q^8 - 4q^6$
  - $m_\kappa(\tau) = 4$ .
- 

$$\xi = ((2,1),(1,1),(1,1)), \quad \sigma_A = (\epsilon_1, \epsilon_2, \epsilon_1, \epsilon_3), \quad \sigma_B = (\epsilon_2, \epsilon_1, \epsilon_3, \epsilon_1).$$

- $[\mathcal{M}_\tau] = (q^2 - q)(q - 1)$ .
  - $[\mathcal{G}_\tau] = (q - 1)^3 q$ .
  - $[\mathfrak{M}_\tau^{\text{irr}}] = q - 2$ .
  - $[R(\tau)] = q^{16} - 2q^{15} - q^{14} + q^{13} + q^{12} + 3q^{11} - q^{10} - q^9 - 2q^8 - q^7 + 2q^6$
  - $m_\kappa(\tau) = 4$ .
- 

$$\xi = ((2,1),(1,1),(1,1)), \quad \sigma_A = (\epsilon_1, \epsilon_2, \epsilon_1, \epsilon_3), \quad \sigma_B = (\epsilon_2, \epsilon_3, \epsilon_1, \epsilon_1).$$

- $[\mathcal{M}_\tau] = (q^2 - q)(q^2 - 1)$ .
  - $[\mathcal{G}_\tau] = (q - 1)^3 q$ .
  - $[\mathfrak{M}_\tau^{\text{irr}}] = q - 2$ .
  - $[R(\tau)] = q^{17} - q^{16} - 3q^{15} + 2q^{13} + 4q^{12} + 2q^{11} - 2q^{10} - 3q^9 - 3q^8 + q^7 + 2q^6$
  - $m_\kappa(\tau) = 2$ .
- 

$$\xi = ((1,1),(1,1),(2,1)), \quad \sigma_A = (\epsilon_1, \epsilon_2, \epsilon_1, \epsilon_3), \quad \sigma_B = (\epsilon_1, \epsilon_2, \epsilon_1, \epsilon_3).$$

- $[\mathcal{M}_\tau] = q^3 - q$ .
  - $[\mathcal{G}_\tau] = (q - 1)^3 q$ .
  - $[\mathfrak{M}_\tau^{\text{irr}}] = q - 2$ .
  - $[R(\tau)] = q^{16} - 3q^{14} - 3q^{13} - q^{12} + 3q^{11} + 5q^{10} + 3q^9 - 3q^7 - 2q^6$
  - $m_\kappa(\tau) = 4$ .
- 

$$\xi = ((1,1),(1,1),(2,1)), \quad \sigma_A = (\epsilon_1, \epsilon_2, \epsilon_1, \epsilon_3), \quad \sigma_B = (\epsilon_2, \epsilon_1, \epsilon_3, \epsilon_1).$$

- $[\mathcal{M}_\tau] = q^3 - q$ .
- $[\mathcal{G}_\tau] = (q - 1)^3 q$ .
- $[\mathfrak{M}_\tau^{\text{irr}}] = q - 2$ .
- $[R(\tau)] = q^{16} - 3q^{14} - 3q^{13} - q^{12} + 3q^{11} + 5q^{10} + 3q^9 - 3q^7 - 2q^6$
- $m_\kappa(\tau) = 4$ .

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$$\xi = ((1,1), (1,1), (2,1)), \quad \sigma_A = (\epsilon_1, \epsilon_2, \epsilon_1, \epsilon_3), \quad \sigma_B = (\epsilon_1, \epsilon_1, \epsilon_3, \epsilon_2).$$

- $[\mathcal{M}_\tau] = q^4 - q.$
  - $[\mathcal{G}_\tau] = (q-1)^3 q.$
  - $[\mathfrak{M}_\tau^{\text{irr}}] = q - 2.$
  - $[R(\tau)] = q^{17} - 2q^{15} - 4q^{14} - 3q^{13} + 2q^{12} + 5q^{11} + 6q^{10} + 2q^9 - 2q^8 - 3q^7 - 2q^6$
  - $m_\kappa(\tau) = 2.$
- 

$$\xi = ((1,1), (1,1), (1,1), (1,1)), \quad \sigma_A = (\epsilon_1, \epsilon_2, \epsilon_1, \epsilon_3), \quad \sigma_B = (\epsilon_1, \epsilon_2, \epsilon_1, \epsilon_3).$$

- $[\mathcal{M}_\tau] = (q^2 - 1)(q - 1).$
  - $[\mathcal{G}_\tau] = (q-1)^4 q.$
  - $[\mathfrak{M}_\tau^{\text{irr}}] = 1.$
  - $[R(\tau)] = q^{14} + 2q^{13} + q^{12} - q^{11} - 3q^{10} - 3q^9 - q^8 + q^7 + 2q^6 + q^5$
  - $m_\kappa(\tau) = 4.$
- 

$$\xi = ((1,1), (1,1), (1,1), (1,1)), \quad \sigma_A = (\epsilon_1, \epsilon_2, \epsilon_1, \epsilon_3), \quad \sigma_B = (\epsilon_2, \epsilon_1, \epsilon_3, \epsilon_1).$$

- $[\mathcal{M}_\tau] = (q^2 - q)(q - 1).$
  - $[\mathcal{G}_\tau] = (q-1)^4 q.$
  - $[\mathfrak{M}_\tau^{\text{irr}}] = 1.$
  - $[R(\tau)] = q^{14} + q^{13} - q^{11} - 2q^{10} - q^9 + q^7 + q^6$
  - $m_\kappa(\tau) = 4.$
- 

$$\xi = ((1,1), (1,1), (1,1), (1,1)), \quad \sigma_A = (\epsilon_1, \epsilon_2, \epsilon_1, \epsilon_3), \quad \sigma_B = (\epsilon_1, \epsilon_3, \epsilon_2, \epsilon_1).$$

- $[\mathcal{M}_\tau] = (q^2 - q)(q - 1).$
  - $[\mathcal{G}_\tau] = (q-1)^4 q.$
  - $[\mathfrak{M}_\tau^{\text{irr}}] = 1.$
  - $[R(\tau)] = q^{14} + q^{13} - q^{11} - 2q^{10} - q^9 + q^7 + q^6$
  - $m_\kappa(\tau) = 4.$
- 

$$\xi = ((1,1), (1,1), (1,1), (1,1)), \quad \sigma_A = (\epsilon_1, \epsilon_2, \epsilon_1, \epsilon_3), \quad \sigma_B = (\epsilon_1, \epsilon_1, \epsilon_3, \epsilon_2).$$

- $[\mathcal{M}_\tau] = (q^2 - q)(q^2 - 1).$
  - $[\mathcal{G}_\tau] = (q-1)^4 q.$
  - $[\mathfrak{M}_\tau^{\text{irr}}] = 1.$
  - $[R(\tau)] = q^{15} + 2q^{14} + q^{13} - q^{12} - 3q^{11} - 3q^{10} - q^9 + q^8 + 2q^7 + q^6$
  - $m_\kappa(\tau) = 4.$
- 

$$\xi = ((1,1), (1,1), (1,1), (1,1)), \quad \sigma_A = (\epsilon_1, \epsilon_2, \epsilon_1, \epsilon_3), \quad \sigma_B = (\epsilon_2, \epsilon_3, \epsilon_1, \epsilon_1).$$

- $[\mathcal{M}_\tau] = (q^2 - q)(q^2 - 1).$
- $[\mathcal{G}_\tau] = (q-1)^4 q.$
- $[\mathfrak{M}_\tau^{\text{irr}}] = 1.$
- $[R(\tau)] = q^{15} + 2q^{14} + q^{13} - q^{12} - 3q^{11} - 3q^{10} - q^9 + q^8 + 2q^7 + q^6$
- $m_\kappa(\tau) = 4.$

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$$\xi = ((2, 1), (1, 1), (1, 1)), \quad \sigma_A = (\epsilon_2, \epsilon_3, \epsilon_1, \epsilon_1), \quad \sigma_B = (\epsilon_3, \epsilon_1, \epsilon_1, \epsilon_2).$$

- $[\mathcal{M}_\tau] = (q^2 - 1)(q - 1)$ .
  - $[\mathcal{G}_\tau] = (q - 1)^3$ .
  - $[\mathfrak{M}_\tau^{\text{irr}}] = q - 2$ .
  - $[R(\tau)] = q^{17} - q^{16} - 3q^{15} + 2q^{13} + 4q^{12} + 2q^{11} - 2q^{10} - 3q^9 - 3q^8 + q^7 + 2q^6$
  - $m_\kappa(\tau) = 2$ .
- 

$$\xi = ((1, 1), (1, 1), (1, 2)), \quad \sigma_A = (\epsilon_2, \epsilon_3, \epsilon_1), \quad \sigma_B = (\epsilon_2, \epsilon_3, \epsilon_1).$$

- $[\mathcal{M}_\tau] = q^4 - q^3 - q^2 + q$ .
  - $[\mathcal{G}_\tau] = (q + 1)(q - 1)^4 q$ .
  - $[\mathfrak{M}_\tau^{\text{irr}}] = 1$ .
  - $[R(\tau)] = q^{14} + q^{13} - q^{11} - 2q^{10} - q^9 + q^7 + q^6$
  - $m_\kappa(\tau) = 2$ .
- 

$$\xi = ((1, 1), (1, 1), (1, 1), (1, 1)), \quad \sigma_A = (\epsilon_2, \epsilon_3, \epsilon_1, \epsilon_1), \quad \sigma_B = (\epsilon_1, \epsilon_1, \epsilon_2, \epsilon_3).$$

- $[\mathcal{M}_\tau] = (q^2 - 1)^2$ .
  - $[\mathcal{G}_\tau] = (q - 1)^4$ .
  - $[\mathfrak{M}_\tau^{\text{irr}}] = 1$ .
  - $[R(\tau)] = q^{16} + 3q^{15} + 3q^{14} - 4q^{12} - 6q^{11} - 4q^{10} + 3q^8 + 3q^7 + q^6$
  - $m_\kappa(\tau) = 1$ .
- 

$$\xi = ((1, 1), (1, 1), (1, 1), (1, 1)), \quad \sigma_A = (\epsilon_2, \epsilon_3, \epsilon_1, \epsilon_1), \quad \sigma_B = (\epsilon_3, \epsilon_1, \epsilon_1, \epsilon_2).$$

- $[\mathcal{M}_\tau] = (q^2 - 1)(q - 1)$ .
  - $[\mathcal{G}_\tau] = (q - 1)^4$ .
  - $[\mathfrak{M}_\tau^{\text{irr}}] = 1$ .
  - $[R(\tau)] = q^{15} + 2q^{14} + q^{13} - q^{12} - 3q^{11} - 3q^{10} - q^9 + q^8 + 2q^7 + q^6$
  - $m_\kappa(\tau) = 4$ .
- 

$$\xi = ((1, 2), (1, 1), (1, 1)), \quad \sigma_A = (\epsilon_1, \epsilon_2, \epsilon_3), \quad \sigma_B = (\epsilon_1, \epsilon_2, \epsilon_3).$$

- $[\mathcal{M}_\tau] = (q^2 - 1)(q - 1)q^2$ .
  - $[\mathcal{G}_\tau] = (q + 1)(q - 1)^4 q$ .
  - $[\mathfrak{M}_\tau^{\text{irr}}] = 1$ .
  - $[R(\tau)] = q^{15} + q^{14} - q^{12} - 2q^{11} - q^{10} + q^8 + q^7$
  - $m_\kappa(\tau) = 4$ .
- 

$$\xi = ((1, 1), (1, 1), (1, 1), (1, 1)), \quad \sigma_A = (\epsilon_1, \epsilon_1, \epsilon_2, \epsilon_3), \quad \sigma_B = (\epsilon_1, \epsilon_2, \epsilon_3, \epsilon_1).$$

- $[\mathcal{M}_\tau] = (q^2 - 1)(q - 1)q$ .
- $[\mathcal{G}_\tau] = (q - 1)^4$ .
- $[\mathfrak{M}_\tau^{\text{irr}}] = 1$ .
- $[R(\tau)] = q^{16} + 2q^{15} + q^{14} - q^{13} - 3q^{12} - 3q^{11} - q^{10} + q^9 + 2q^8 + q^7$
- $m_\kappa(\tau) = 4$ .

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$$\xi = ((1,1),(1,1),(1,1),(1,1)), \quad \sigma_A = (\epsilon_1, \epsilon_1, \epsilon_2, \epsilon_3), \quad \sigma_B = (\epsilon_2, \epsilon_1, \epsilon_1, \epsilon_3).$$

- $[\mathcal{M}_\tau] = (q-1)^2 q^2.$
  - $[\mathcal{G}_\tau] = (q-1)^4.$
  - $[\mathfrak{M}_\tau^{\text{irr}}] = 1.$
  - $[R(\tau)] = q^{16} + q^{15} - q^{13} - 2q^{12} - q^{11} + q^9 + q^8$
  - $m_\kappa(\tau) = 4.$
- 

$$\xi = ((2,1),(1,1),(1,1)), \quad \sigma_A = (\epsilon_1, \epsilon_2, \epsilon_1, \epsilon_3), \quad \sigma_B = (\epsilon_2, \epsilon_1, \epsilon_3, \epsilon_1).$$

- $[\mathcal{M}_\tau] = (q^2 - q)(q-1)q.$
  - $[\mathcal{G}_\tau] = (q-1)^3 q.$
  - $[\mathfrak{M}_\tau^{\text{irr}}] = q - 2.$
  - $[R(\tau)] = q^{17} - 2q^{16} - q^{15} + q^{14} + q^{13} + 3q^{12} - q^{11} - q^{10} - 2q^9 - q^8 + 2q^7$
  - $m_\kappa(\tau) = 4.$
- 

$$\xi = ((1,1),(1,1),(1,1),(1,1)), \quad \sigma_A = (\epsilon_1, \epsilon_2, \epsilon_1, \epsilon_3), \quad \sigma_B = (\epsilon_1, \epsilon_2, \epsilon_1, \epsilon_3).$$

- $[\mathcal{M}_\tau] = (q-1)^2 q^2.$
  - $[\mathcal{G}_\tau] = (q-1)^4 q.$
  - $[\mathfrak{M}_\tau^{\text{irr}}] = 1.$
  - $[R(\tau)] = q^{15} + q^{14} - q^{12} - 2q^{11} - q^{10} + q^8 + q^7$
  - $m_\kappa(\tau) = 4.$
- 

$$\xi = ((1,1),(1,1),(1,1),(1,1)), \quad \sigma_A = (\epsilon_1, \epsilon_2, \epsilon_1, \epsilon_3), \quad \sigma_B = (\epsilon_2, \epsilon_1, \epsilon_3, \epsilon_1).$$

- $[\mathcal{M}_\tau] = (q^2 - q)(q-1)q.$
  - $[\mathcal{G}_\tau] = (q-1)^4 q.$
  - $[\mathfrak{M}_\tau^{\text{irr}}] = 1.$
  - $[R(\tau)] = q^{15} + q^{14} - q^{12} - 2q^{11} - q^{10} + q^8 + q^7$
  - $m_\kappa(\tau) = 4.$
- 

$$\xi = ((1,1),(1,1),(1,1),(1,1)), \quad \sigma_A = (\epsilon_1, \epsilon_2, \epsilon_1, \epsilon_3), \quad \sigma_B = (\epsilon_1, \epsilon_3, \epsilon_2, \epsilon_1).$$

- $[\mathcal{M}_\tau] = (q^2 - q)(q-1)q.$
  - $[\mathcal{G}_\tau] = (q-1)^4 q.$
  - $[\mathfrak{M}_\tau^{\text{irr}}] = 1.$
  - $[R(\tau)] = q^{15} + q^{14} - q^{12} - 2q^{11} - q^{10} + q^8 + q^7$
  - $m_\kappa(\tau) = 4.$
- 

$$\xi = ((1,1),(1,1),(1,1),(1,1)), \quad \sigma_A = (\epsilon_1, \epsilon_2, \epsilon_1, \epsilon_3), \quad \sigma_B = (\epsilon_1, \epsilon_1, \epsilon_3, \epsilon_2).$$

- $[\mathcal{M}_\tau] = (q^2 - q)(q-1)q^2.$
- $[\mathcal{G}_\tau] = (q-1)^4 q.$
- $[\mathfrak{M}_\tau^{\text{irr}}] = 1.$
- $[R(\tau)] = q^{16} + q^{15} - q^{13} - 2q^{12} - q^{11} + q^9 + q^8$
- $m_\kappa(\tau) = 4.$

$$\xi = ((2, 1), (1, 1), (1, 1)), \quad \sigma_A = (\epsilon_1, \epsilon_2, \epsilon_3, \epsilon_1), \quad \sigma_B = (\epsilon_1, \epsilon_2, \epsilon_3, \epsilon_1).$$

- $[\mathcal{M}_\tau] = (q^2 - 1)(q - 1)q.$
- $[\mathcal{G}_\tau] = (q - 1)^3 q.$
- $[\mathfrak{M}_\tau^{\text{irr}}] = q - 2.$
- $[R(\tau)] = q^{17} - q^{16} - 3q^{15} + 2q^{13} + 4q^{12} + 2q^{11} - 2q^{10} - 3q^9 - 3q^8 + q^7 + 2q^6$
- $m_\kappa(\tau) = 4.$

$$\xi = ((2, 1), (1, 1), (1, 1)), \quad \sigma_A = (\epsilon_1, \epsilon_2, \epsilon_3, \epsilon_1), \quad \sigma_B = (\epsilon_2, \epsilon_1, \epsilon_1, \epsilon_3).$$

- $[\mathcal{M}_\tau] = (q - 1)^2 q^2.$
- $[\mathcal{G}_\tau] = (q - 1)^3 q.$
- $[\mathfrak{M}_\tau^{\text{irr}}] = q - 2.$
- $[R(\tau)] = q^{17} - 2q^{16} - q^{15} + q^{14} + q^{13} + 3q^{12} - q^{11} - q^{10} - 2q^9 - q^8 + 2q^7$
- $m_\kappa(\tau) = 4.$

$$\xi = ((1, 1), (1, 1), (1, 1), (1, 1)), \quad \sigma_A = (\epsilon_1, \epsilon_2, \epsilon_3, \epsilon_1), \quad \sigma_B = (\epsilon_1, \epsilon_2, \epsilon_3, \epsilon_1).$$

- $[\mathcal{M}_\tau] = (q^2 - 1)(q - 1)q.$
- $[\mathcal{G}_\tau] = (q - 1)^4 q.$
- $[\mathfrak{M}_\tau^{\text{irr}}] = 1.$
- $[R(\tau)] = q^{15} + 2q^{14} + q^{13} - q^{12} - 3q^{11} - 3q^{10} - q^9 + q^8 + 2q^7 + q^6$
- $m_\kappa(\tau) = 4.$

$$\xi = ((1, 1), (1, 1), (1, 1), (1, 1)), \quad \sigma_A = (\epsilon_1, \epsilon_2, \epsilon_3, \epsilon_1), \quad \sigma_B = (\epsilon_2, \epsilon_1, \epsilon_1, \epsilon_3).$$

- $[\mathcal{M}_\tau] = (q - 1)^2 q^2.$
- $[\mathcal{G}_\tau] = (q - 1)^4 q.$
- $[\mathfrak{M}_\tau^{\text{irr}}] = 1.$
- $[R(\tau)] = q^{15} + q^{14} - q^{12} - 2q^{11} - q^{10} + q^8 + q^7$
- $m_\kappa(\tau) = 4.$

$$\xi = ((1, 1), (1, 1), (1, 1), (1, 1)), \quad \sigma_A = (\epsilon_1, \epsilon_2, \epsilon_3, \epsilon_1), \quad \sigma_B = (\epsilon_1, \epsilon_3, \epsilon_1, \epsilon_2).$$

- $[\mathcal{M}_\tau] = (q - 1)^2 q^2.$
- $[\mathcal{G}_\tau] = (q - 1)^4 q.$
- $[\mathfrak{M}_\tau^{\text{irr}}] = 1.$
- $[R(\tau)] = q^{15} + q^{14} - q^{12} - 2q^{11} - q^{10} + q^8 + q^7$
- $m_\kappa(\tau) = 4.$

$$\xi = ((1, 1), (1, 1), (1, 1), (1, 1)), \quad \sigma_A = (\epsilon_1, \epsilon_2, \epsilon_3, \epsilon_1), \quad \sigma_B = (\epsilon_2, \epsilon_1, \epsilon_3, \epsilon_1).$$

- $[\mathcal{M}_\tau] = (q^2 - 1)(q - 1)q.$
- $[\mathcal{G}_\tau] = (q - 1)^4 q.$
- $[\mathfrak{M}_\tau^{\text{irr}}] = 1.$
- $[R(\tau)] = q^{15} + 2q^{14} + q^{13} - q^{12} - 3q^{11} - 3q^{10} - q^9 + q^8 + 2q^7 + q^6$
- $m_\kappa(\tau) = 4.$

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$$\xi = ((1,1),(1,1),(1,1),(1,1)), \quad \sigma_A = (\epsilon_1, \epsilon_2, \epsilon_3, \epsilon_1), \quad \sigma_B = (\epsilon_1, \epsilon_1, \epsilon_2, \epsilon_3).$$

- $[\mathcal{M}_\tau] = (q^2 - 1)(q - 1)q^2.$
  - $[\mathcal{G}_\tau] = (q - 1)^4 q.$
  - $[\mathfrak{M}_\tau^{\text{irr}}] = 1.$
  - $[R(\tau)] = q^{16} + 2q^{15} + q^{14} - q^{13} - 3q^{12} - 3q^{11} - q^{10} + q^9 + 2q^8 + q^7$
  - $m_\kappa(\tau) = 4.$
- 

$$\xi = ((1,1),(3,1)), \quad \sigma_A = (\epsilon_1, \epsilon_1, \epsilon_2, \epsilon_3), \quad \sigma_B = (\epsilon_1, \epsilon_1, \epsilon_2, \epsilon_3).$$

- $[\mathcal{M}_\tau] = q^2 - q.$
  - $[\mathcal{G}_\tau] = (q - 1)^2 q.$
  - $[\mathfrak{M}_\tau^{\text{irr}}] = q^4 + 4q^3 - 9q^2 - 3q + 12.$
  - $[R(\tau)] = q^{19} + 4q^{18} - 10q^{17} - 8q^{16} + 16q^{15} + 9q^{14} + 5q^{13} - 13q^{12} - 20q^{11} - q^{10} + 5q^9 + 21q^8 + 3q^7 - 12q^6$
  - $m_\kappa(\tau) = 1.$
- 

$$\xi = ((1,1),(3,1)), \quad \sigma_A = (\epsilon_1, \epsilon_1, \epsilon_2, \epsilon_3), \quad \sigma_B = (\epsilon_2, \epsilon_3, \epsilon_1, \epsilon_1).$$

- $[\mathcal{M}_\tau] = q^3 - q.$
  - $[\mathcal{G}_\tau] = (q - 1)^2 q.$
  - $[\mathfrak{M}_\tau^{\text{irr}}] = q^2 - 3q + 3.$
  - $[R(\tau)] = q^{18} - 2q^{17} - q^{16} + 4q^{15} + q^{14} - 4q^{12} - 4q^{11} + q^{10} + 2q^9 + 5q^8 - 3q^6$
  - $m_\kappa(\tau) = 2.$
- 

$$\xi = ((1,1),(2,1),(1,1)), \quad \sigma_A = (\epsilon_1, \epsilon_1, \epsilon_2, \epsilon_3), \quad \sigma_B = (\epsilon_2, \epsilon_3, \epsilon_1, \epsilon_1).$$

- $[\mathcal{M}_\tau] = (q^2 - q)(q - 1).$
  - $[\mathcal{G}_\tau] = (q - 1)^3 q.$
  - $[\mathfrak{M}_\tau^{\text{irr}}] = q - 2.$
  - $[R(\tau)] = q^{16} - 2q^{15} - q^{14} + q^{13} + q^{12} + 3q^{11} - q^{10} - q^9 - 2q^8 - q^7 + 2q^6$
  - $m_\kappa(\tau) = 4.$
- 

$$\xi = ((1,1),(3,1)), \quad \sigma_A = (\epsilon_2, \epsilon_1, \epsilon_1, \epsilon_3), \quad \sigma_B = (\epsilon_1, \epsilon_2, \epsilon_3, \epsilon_1).$$

- $[\mathcal{M}_\tau] = q^2 - 1.$
  - $[\mathcal{G}_\tau] = (q - 1)^2.$
  - $[\mathfrak{M}_\tau^{\text{irr}}] = q^2 - 3q + 3.$
  - $[R(\tau)] = q^{18} - 2q^{17} - q^{16} + 4q^{15} + q^{14} - 4q^{12} - 4q^{11} + q^{10} + 2q^9 + 5q^8 - 3q^6$
  - $m_\kappa(\tau) = 2.$
- 

$$\xi = ((1,1),(2,1),(1,1)), \quad \sigma_A = (\epsilon_2, \epsilon_1, \epsilon_3, \epsilon_1), \quad \sigma_B = (\epsilon_2, \epsilon_1, \epsilon_3, \epsilon_1).$$

- $[\mathcal{M}_\tau] = (q^2 - 1)(q - 1).$
- $[\mathcal{G}_\tau] = (q - 1)^3.$
- $[\mathfrak{M}_\tau^{\text{irr}}] = q - 2.$
- $[R(\tau)] = q^{17} - q^{16} - 3q^{15} + 2q^{13} + 4q^{12} + 2q^{11} - 2q^{10} - 3q^9 - 3q^8 + q^7 + 2q^6$
- $m_\kappa(\tau) = 4.$

$$\xi = ((1, 1), (2, 1), (1, 1)), \quad \sigma_A = (\epsilon_2, \epsilon_1, \epsilon_3, \epsilon_1), \quad \sigma_B = (\epsilon_1, \epsilon_2, \epsilon_1, \epsilon_3).$$

- $[\mathcal{M}_\tau] = (q - 1)^2$ .
  - $[\mathcal{G}_\tau] = (q - 1)^3$ .
  - $[\mathfrak{M}_\tau^{\text{irr}}] = q - 2$ .
  - $[R(\tau)] = q^{16} - 2q^{15} - q^{14} + q^{13} + q^{12} + 3q^{11} - q^{10} - q^9 - 2q^8 - q^7 + 2q^6$
  - $m_\kappa(\tau) = 4$ .
- 

$$\xi = ((1, 1), (1, 1), (1, 1), (1, 1)), \quad \sigma_A = (\epsilon_2, \epsilon_1, \epsilon_1, \epsilon_3), \quad \sigma_B = (\epsilon_3, \epsilon_1, \epsilon_2, \epsilon_1).$$

- $[\mathcal{M}_\tau] = (q - 1)^3$ .
  - $[\mathcal{G}_\tau] = (q - 1)^4$ .
  - $[\mathfrak{M}_\tau^{\text{irr}}] = 1$ .
  - $[R(\tau)] = q^{15} - q^{13} - q^{12} - q^{11} + q^{10} + q^9 + q^8 - q^6$
  - $m_\kappa(\tau) = 4$ .
- 

$$\xi = ((1, 1), (2, 1), (1, 1)), \quad \sigma_A = (\epsilon_1, \epsilon_1, \epsilon_2, \epsilon_3), \quad \sigma_B = (\epsilon_2, \epsilon_3, \epsilon_1, \epsilon_1).$$

- $[\mathcal{M}_\tau] = (q^2 - q)(q - 1)q$ .
  - $[\mathcal{G}_\tau] = (q - 1)^3q$ .
  - $[\mathfrak{M}_\tau^{\text{irr}}] = q - 2$ .
  - $[R(\tau)] = q^{17} - 2q^{16} - q^{15} + q^{14} + q^{13} + 3q^{12} - q^{11} - q^{10} - 2q^9 - q^8 + 2q^7$
  - $m_\kappa(\tau) = 4$ .
- 

$$\xi = ((1, 1), (2, 1), (1, 1)), \quad \sigma_A = (\epsilon_1, \epsilon_1, \epsilon_2, \epsilon_3), \quad \sigma_B = (\epsilon_1, \epsilon_2, \epsilon_3, \epsilon_1).$$

- $[\mathcal{M}_\tau] = (q^2 - q)(q^2 - 1)$ .
  - $[\mathcal{G}_\tau] = (q - 1)^3q$ .
  - $[\mathfrak{M}_\tau^{\text{irr}}] = q - 2$ .
  - $[R(\tau)] = q^{17} - q^{16} - 3q^{15} + 2q^{13} + 4q^{12} + 2q^{11} - 2q^{10} - 3q^9 - 3q^8 + q^7 + 2q^6$
  - $m_\kappa(\tau) = 2$ .
- 

$$\xi = ((1, 1), (2, 1), (1, 1)), \quad \sigma_A = (\epsilon_1, \epsilon_2, \epsilon_3, \epsilon_1), \quad \sigma_B = (\epsilon_1, \epsilon_2, \epsilon_3, \epsilon_1).$$

- $[\mathcal{M}_\tau] = (q^2 - 1)^2$ .
  - $[\mathcal{G}_\tau] = (q - 1)^3q$ .
  - $[\mathfrak{M}_\tau^{\text{irr}}] = q - 2$ .
  - $[R(\tau)] = q^{17} - 4q^{15} - 3q^{14} + 2q^{13} + 6q^{12} + 6q^{11} - 5q^9 - 6q^8 - 2q^7 + 3q^6 + 2q^5$
  - $m_\kappa(\tau) = 1$ .
- 

$$\xi = ((1, 1), (2, 1), (1, 1)), \quad \sigma_A = (\epsilon_1, \epsilon_2, \epsilon_3, \epsilon_1), \quad \sigma_B = (\epsilon_1, \epsilon_3, \epsilon_1, \epsilon_2).$$

- $[\mathcal{M}_\tau] = (q^2 - 1)(q - 1)q$ .
- $[\mathcal{G}_\tau] = (q - 1)^3q$ .
- $[\mathfrak{M}_\tau^{\text{irr}}] = q - 2$ .
- $[R(\tau)] = q^{17} - q^{16} - 3q^{15} + 2q^{13} + 4q^{12} + 2q^{11} - 2q^{10} - 3q^9 - 3q^8 + q^7 + 2q^6$
- $m_\kappa(\tau) = 2$ .

$$\xi = ((1,1),(2,1),(1,1)), \quad \sigma_A = (\epsilon_1, \epsilon_2, \epsilon_3, \epsilon_1), \quad \sigma_B = (\epsilon_2, \epsilon_1, \epsilon_3, \epsilon_1).$$

- $[\mathcal{M}_\tau] = (q^2 - 1)(q - 1)q.$
  - $[\mathcal{G}_\tau] = (q - 1)^3 q.$
  - $[\mathfrak{M}_\tau^{\text{irr}}] = q - 2.$
  - $[R(\tau)] = q^{17} - q^{16} - 3q^{15} + 2q^{13} + 4q^{12} + 2q^{11} - 2q^{10} - 3q^9 - 3q^8 + q^7 + 2q^6$
  - $m_\kappa(\tau) = 2.$
- 

$$\xi = ((1,1),(1,1),(1,1),(1,1)), \quad \sigma_A = (\epsilon_1, \epsilon_2, \epsilon_3, \epsilon_1), \quad \sigma_B = (\epsilon_1, \epsilon_2, \epsilon_3, \epsilon_1).$$

- $[\mathcal{M}_\tau] = (q^2 - 1)(q - 1)^2.$
  - $[\mathcal{G}_\tau] = (q - 1)^4 q.$
  - $[\mathfrak{M}_\tau^{\text{irr}}] = 1.$
  - $[R(\tau)] = q^{15} + q^{14} - q^{13} - 2q^{12} - 2q^{11} + 2q^9 + 2q^8 + q^7 - q^6 - q^5$
  - $m_\kappa(\tau) = 2.$
- 

$$\xi = ((1,1),(1,1),(1,1),(1,1)), \quad \sigma_A = (\epsilon_1, \epsilon_2, \epsilon_3, \epsilon_1), \quad \sigma_B = (\epsilon_2, \epsilon_1, \epsilon_1, \epsilon_3).$$

- $[\mathcal{M}_\tau] = (q^2 - 1)(q - 1)^2 q.$
  - $[\mathcal{G}_\tau] = (q - 1)^4 q.$
  - $[\mathfrak{M}_\tau^{\text{irr}}] = 1.$
  - $[R(\tau)] = q^{16} + q^{15} - q^{14} - 2q^{13} - 2q^{12} + 2q^{10} + 2q^9 + q^8 - q^7 - q^6$
  - $m_\kappa(\tau) = 2.$
- 

$$\xi = ((1,1),(1,1),(1,1),(1,1)), \quad \sigma_A = (\epsilon_1, \epsilon_2, \epsilon_3, \epsilon_1), \quad \sigma_B = (\epsilon_2, \epsilon_1, \epsilon_3, \epsilon_1).$$

- $[\mathcal{M}_\tau] = (q - 1)^3 q.$
  - $[\mathcal{G}_\tau] = (q - 1)^4 q.$
  - $[\mathfrak{M}_\tau^{\text{irr}}] = 1.$
  - $[R(\tau)] = q^{15} - q^{13} - q^{12} - q^{11} + q^{10} + q^9 + q^8 - q^6$
  - $m_\kappa(\tau) = 4.$
- 

$$\xi = ((1,1),(1,1),(1,1),(1,1)), \quad \sigma_A = (\epsilon_2, \epsilon_1, \epsilon_1, \epsilon_3), \quad \sigma_B = (\epsilon_1, \epsilon_2, \epsilon_3, \epsilon_1).$$

- $[\mathcal{M}_\tau] = (q^2 - 1)(q - 1)^2.$
  - $[\mathcal{G}_\tau] = (q - 1)^4.$
  - $[\mathfrak{M}_\tau^{\text{irr}}] = 1.$
  - $[R(\tau)] = q^{16} + q^{15} - q^{14} - 2q^{13} - 2q^{12} + 2q^{10} + 2q^9 + q^8 - q^7 - q^6$
  - $m_\kappa(\tau) = 2.$
- 

$$\xi = ((1,1),(1,1),(1,1),(1,1)), \quad \sigma_A = (\epsilon_2, \epsilon_1, \epsilon_1, \epsilon_3), \quad \sigma_B = (\epsilon_3, \epsilon_1, \epsilon_2, \epsilon_1).$$

- $[\mathcal{M}_\tau] = (q - 1)^3 q.$
- $[\mathcal{G}_\tau] = (q - 1)^4.$
- $[\mathfrak{M}_\tau^{\text{irr}}] = 1.$
- $[R(\tau)] = q^{16} - q^{14} - q^{13} - q^{12} + q^{11} + q^{10} + q^9 - q^7$
- $m_\kappa(\tau) = 4.$

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$$\xi = ((1, 1), (2, 1), (1, 1)), \quad \sigma_A = (\epsilon_2, \epsilon_1, \epsilon_3, \epsilon_1), \quad \sigma_B = (\epsilon_1, \epsilon_2, \epsilon_1, \epsilon_3).$$

- $[\mathcal{M}_\tau] = (q^2 - q)(q - 1)q.$
  - $[\mathcal{G}_\tau] = (q - 1)^3 q.$
  - $[\mathfrak{M}_\tau^{\text{irr}}] = q - 2.$
  - $[R(\tau)] = q^{17} - 2q^{16} - q^{15} + q^{14} + q^{13} + 3q^{12} - q^{11} - q^{10} - 2q^9 - q^8 + 2q^7$
  - $m_\kappa(\tau) = 4.$
- 

$$\xi = ((1, 1), (2, 1), (1, 1)), \quad \sigma_A = (\epsilon_2, \epsilon_1, \epsilon_3, \epsilon_1), \quad \sigma_B = (\epsilon_1, \epsilon_2, \epsilon_3, \epsilon_1).$$

- $[\mathcal{M}_\tau] = (q^2 - q)(q^2 - 1).$
  - $[\mathcal{G}_\tau] = (q - 1)^3 q.$
  - $[\mathfrak{M}_\tau^{\text{irr}}] = q - 2.$
  - $[R(\tau)] = q^{17} - q^{16} - 3q^{15} + 2q^{13} + 4q^{12} + 2q^{11} - 2q^{10} - 3q^9 - 3q^8 + q^7 + 2q^6$
  - $m_\kappa(\tau) = 2.$
- 

$$\xi = ((1, 1), (1, 1), (1, 1), (1, 1)), \quad \sigma_A = (\epsilon_2, \epsilon_1, \epsilon_3, \epsilon_1), \quad \sigma_B = (\epsilon_2, \epsilon_1, \epsilon_3, \epsilon_1).$$

- $[\mathcal{M}_\tau] = (q - 1)^3 q.$
  - $[\mathcal{G}_\tau] = (q - 1)^4 q.$
  - $[\mathfrak{M}_\tau^{\text{irr}}] = 1.$
  - $[R(\tau)] = q^{15} - q^{13} - q^{12} - q^{11} + q^{10} + q^9 + q^8 - q^6$
  - $m_\kappa(\tau) = 4.$
- 

$$\xi = ((1, 1), (1, 1), (1, 1), (1, 1)), \quad \sigma_A = (\epsilon_2, \epsilon_1, \epsilon_3, \epsilon_1), \quad \sigma_B = (\epsilon_3, \epsilon_1, \epsilon_1, \epsilon_2).$$

- $[\mathcal{M}_\tau] = (q^2 - q)(q - 1)^2 q.$
  - $[\mathcal{G}_\tau] = (q - 1)^4 q.$
  - $[\mathfrak{M}_\tau^{\text{irr}}] = 1.$
  - $[R(\tau)] = q^{16} - q^{14} - q^{13} - q^{12} + q^{11} + q^{10} + q^9 - q^7$
  - $m_\kappa(\tau) = 4.$
- 

$$\xi = ((1, 1), (1, 1), (1, 1), (1, 1)), \quad \sigma_A = (\epsilon_2, \epsilon_1, \epsilon_3, \epsilon_1), \quad \sigma_B = (\epsilon_1, \epsilon_2, \epsilon_3, \epsilon_1).$$

- $[\mathcal{M}_\tau] = (q^2 - q)(q - 1)^2.$
  - $[\mathcal{G}_\tau] = (q - 1)^4 q.$
  - $[\mathfrak{M}_\tau^{\text{irr}}] = 1.$
  - $[R(\tau)] = q^{15} - q^{13} - q^{12} - q^{11} + q^{10} + q^9 + q^8 - q^6$
  - $m_\kappa(\tau) = 4.$
- 

$$\xi = ((1, 1), (1, 1), (2, 1)), \quad \sigma_A = (\epsilon_1, \epsilon_2, \epsilon_1, \epsilon_3), \quad \sigma_B = (\epsilon_1, \epsilon_2, \epsilon_1, \epsilon_3).$$

- $[\mathcal{M}_\tau] = (q^2 - 1)(q - 1)q.$
- $[\mathcal{G}_\tau] = (q - 1)^3 q.$
- $[\mathfrak{M}_\tau^{\text{irr}}] = q - 2.$
- $[R(\tau)] = q^{17} - q^{16} - 3q^{15} + 2q^{13} + 4q^{12} + 2q^{11} - 2q^{10} - 3q^9 - 3q^8 + q^7 + 2q^6$
- $m_\kappa(\tau) = 4.$

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$$\xi = ((1, 1), (1, 1), (2, 1)), \quad \sigma_A = (\epsilon_1, \epsilon_2, \epsilon_1, \epsilon_3), \quad \sigma_B = (\epsilon_2, \epsilon_1, \epsilon_3, \epsilon_1).$$

- $[\mathcal{M}_\tau] = (q - 1)^2 q^2.$
  - $[\mathcal{G}_\tau] = (q - 1)^3 q.$
  - $[\mathfrak{M}_\tau^{\text{irr}}] = q - 2.$
  - $[R(\tau)] = q^{17} - 2q^{16} - q^{15} + q^{14} + q^{13} + 3q^{12} - q^{11} - q^{10} - 2q^9 - q^8 + 2q^7$
  - $m_\kappa(\tau) = 4.$
- 

$$\xi = ((1, 1), (1, 1), (1, 1), (1, 1)), \quad \sigma_A = (\epsilon_1, \epsilon_2, \epsilon_1, \epsilon_3), \quad \sigma_B = (\epsilon_1, \epsilon_2, \epsilon_1, \epsilon_3).$$

- $[\mathcal{M}_\tau] = (q - 1)^3 q.$
  - $[\mathcal{G}_\tau] = (q - 1)^4 q.$
  - $[\mathfrak{M}_\tau^{\text{irr}}] = 1.$
  - $[R(\tau)] = q^{15} - q^{13} - q^{12} - q^{11} + q^{10} + q^9 + q^8 - q^6$
  - $m_\kappa(\tau) = 4.$
- 

$$\xi = ((1, 1), (1, 1), (1, 1), (1, 1)), \quad \sigma_A = (\epsilon_1, \epsilon_2, \epsilon_1, \epsilon_3), \quad \sigma_B = (\epsilon_1, \epsilon_3, \epsilon_2, \epsilon_1).$$

- $[\mathcal{M}_\tau] = (q - 1)^3 q.$
  - $[\mathcal{G}_\tau] = (q - 1)^4 q.$
  - $[\mathfrak{M}_\tau^{\text{irr}}] = 1.$
  - $[R(\tau)] = q^{15} - q^{13} - q^{12} - q^{11} + q^{10} + q^9 + q^8 - q^6$
  - $m_\kappa(\tau) = 4.$
- 

$$\xi = ((1, 1), (1, 1), (1, 1), (1, 1)), \quad \sigma_A = (\epsilon_1, \epsilon_2, \epsilon_1, \epsilon_3), \quad \sigma_B = (\epsilon_2, \epsilon_3, \epsilon_1, \epsilon_1).$$

- $[\mathcal{M}_\tau] = (q - 1)^3 q^2.$
  - $[\mathcal{G}_\tau] = (q - 1)^4 q.$
  - $[\mathfrak{M}_\tau^{\text{irr}}] = 1.$
  - $[R(\tau)] = q^{16} - q^{14} - q^{13} - q^{12} + q^{11} + q^{10} + q^9 - q^7$
  - $m_\kappa(\tau) = 4.$
- 

$$\xi = ((1, 1), (1, 1), (2, 1)), \quad \sigma_A = (\epsilon_2, \epsilon_1, \epsilon_1, \epsilon_3), \quad \sigma_B = (\epsilon_1, \epsilon_2, \epsilon_3, \epsilon_1).$$

- $[\mathcal{M}_\tau] = (q^2 - q)(q - 1)q.$
  - $[\mathcal{G}_\tau] = (q - 1)^3 q.$
  - $[\mathfrak{M}_\tau^{\text{irr}}] = q - 2.$
  - $[R(\tau)] = q^{17} - 2q^{16} - q^{15} + q^{14} + q^{13} + 3q^{12} - q^{11} - q^{10} - 2q^9 - q^8 + 2q^7$
  - $m_\kappa(\tau) = 4.$
- 

$$\xi = ((1, 1), (1, 1), (1, 1), (1, 1)), \quad \sigma_A = (\epsilon_2, \epsilon_3, \epsilon_1, \epsilon_1), \quad \sigma_B = (\epsilon_1, \epsilon_3, \epsilon_2, \epsilon_1).$$

- $[\mathcal{M}_\tau] = (q - 1)^3 q.$
- $[\mathcal{G}_\tau] = (q - 1)^4.$
- $[\mathfrak{M}_\tau^{\text{irr}}] = 1.$
- $[R(\tau)] = q^{16} - q^{14} - q^{13} - q^{12} + q^{11} + q^{10} + q^9 - q^7$
- $m_\kappa(\tau) = 4.$

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$$\xi = ((1,1),(1,1),(1,1),(1,1)), \quad \sigma_A = (\epsilon_1, \epsilon_2, \epsilon_1, \epsilon_3), \quad \sigma_B = (\epsilon_1, \epsilon_2, \epsilon_1, \epsilon_3).$$

- $[\mathcal{M}_\tau] = (q-1)^3 q^2.$
  - $[\mathcal{G}_\tau] = (q-1)^4 q.$
  - $[\mathfrak{M}_\tau^{\text{irr}}] = 1.$
  - $[R(\tau)] = q^{16} - q^{14} - q^{13} - q^{12} + q^{11} + q^{10} + q^9 - q^7$
  - $m_\kappa(\tau) = 4.$
- 

$$\xi = ((1,1),(1,1),(1,1),(1,1)), \quad \sigma_A = (\epsilon_1, \epsilon_2, \epsilon_1, \epsilon_3), \quad \sigma_B = (\epsilon_2, \epsilon_1, \epsilon_3, \epsilon_1).$$

- $[\mathcal{M}_\tau] = (q-1)^3 q^2.$
  - $[\mathcal{G}_\tau] = (q-1)^4 q.$
  - $[\mathfrak{M}_\tau^{\text{irr}}] = 1.$
  - $[R(\tau)] = q^{16} - q^{14} - q^{13} - q^{12} + q^{11} + q^{10} + q^9 - q^7$
  - $m_\kappa(\tau) = 4.$
- 

$$\xi = ((1,1),(1,1),(1,1),(1,1)), \quad \sigma_A = (\epsilon_1, \epsilon_2, \epsilon_1, \epsilon_3), \quad \sigma_B = (\epsilon_1, \epsilon_3, \epsilon_2, \epsilon_1).$$

- $[\mathcal{M}_\tau] = (q-1)^3 q^2.$
  - $[\mathcal{G}_\tau] = (q-1)^4 q.$
  - $[\mathfrak{M}_\tau^{\text{irr}}] = 1.$
  - $[R(\tau)] = q^{16} - q^{14} - q^{13} - q^{12} + q^{11} + q^{10} + q^9 - q^7$
  - $m_\kappa(\tau) = 4.$
- 

$$\xi = ((1,1),(1,1),(1,1),(1,1)), \quad \sigma_A = (\epsilon_1, \epsilon_2, \epsilon_3, \epsilon_1), \quad \sigma_B = (\epsilon_1, \epsilon_2, \epsilon_3, \epsilon_1).$$

- $[\mathcal{M}_\tau] = (q-1)^3 q^2.$
  - $[\mathcal{G}_\tau] = (q-1)^4 q.$
  - $[\mathfrak{M}_\tau^{\text{irr}}] = 1.$
  - $[R(\tau)] = q^{16} - q^{14} - q^{13} - q^{12} + q^{11} + q^{10} + q^9 - q^7$
  - $m_\kappa(\tau) = 4.$
- 

$$\xi = ((1,1),(1,1),(1,1),(1,1)), \quad \sigma_A = (\epsilon_1, \epsilon_2, \epsilon_3, \epsilon_1), \quad \sigma_B = (\epsilon_1, \epsilon_3, \epsilon_1, \epsilon_2).$$

- $[\mathcal{M}_\tau] = (q-1)^3 q^2.$
  - $[\mathcal{G}_\tau] = (q-1)^4 q.$
  - $[\mathfrak{M}_\tau^{\text{irr}}] = 1.$
  - $[R(\tau)] = q^{16} - q^{14} - q^{13} - q^{12} + q^{11} + q^{10} + q^9 - q^7$
  - $m_\kappa(\tau) = 4.$
- 

$$\xi = ((1,1),(1,1),(1,1),(1,1)), \quad \sigma_A = (\epsilon_1, \epsilon_2, \epsilon_3, \epsilon_1), \quad \sigma_B = (\epsilon_2, \epsilon_1, \epsilon_3, \epsilon_1).$$

- $[\mathcal{M}_\tau] = (q-1)^3 q^2.$
- $[\mathcal{G}_\tau] = (q-1)^4 q.$
- $[\mathfrak{M}_\tau^{\text{irr}}] = 1.$
- $[R(\tau)] = q^{16} - q^{14} - q^{13} - q^{12} + q^{11} + q^{10} + q^9 - q^7$
- $m_\kappa(\tau) = 4.$

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$$\xi = ((1,1),(1,1),(1,1),(1,1)), \quad \sigma_A = (\epsilon_2, \epsilon_1, \epsilon_3, \epsilon_1), \quad \sigma_B = (\epsilon_2, \epsilon_1, \epsilon_3, \epsilon_1).$$

- $[\mathcal{M}_\tau] = (q-1)^3 q^2.$
  - $[\mathcal{G}_\tau] = (q-1)^4 q.$
  - $[\mathfrak{M}_\tau^{\text{irr}}] = 1.$
  - $[R(\tau)] = q^{16} - q^{14} - q^{13} - q^{12} + q^{11} + q^{10} + q^9 - q^7$
  - $m_\kappa(\tau) = 4.$
- 

$$\xi = ((1,1),(1,1),(1,1),(1,1)), \quad \sigma_A = (\epsilon_2, \epsilon_1, \epsilon_3, \epsilon_1), \quad \sigma_B = (\epsilon_1, \epsilon_2, \epsilon_1, \epsilon_3).$$

- $[\mathcal{M}_\tau] = (q-1)^3 q^2.$
  - $[\mathcal{G}_\tau] = (q-1)^4 q.$
  - $[\mathfrak{M}_\tau^{\text{irr}}] = 1.$
  - $[R(\tau)] = q^{16} - q^{14} - q^{13} - q^{12} + q^{11} + q^{10} + q^9 - q^7$
  - $m_\kappa(\tau) = 4.$
- 

$$\xi = ((1,1),(1,1),(1,1),(1,1)), \quad \sigma_A = (\epsilon_2, \epsilon_1, \epsilon_3, \epsilon_1), \quad \sigma_B = (\epsilon_1, \epsilon_2, \epsilon_3, \epsilon_1).$$

- $[\mathcal{M}_\tau] = (q-1)^3 q^2.$
  - $[\mathcal{G}_\tau] = (q-1)^4 q.$
  - $[\mathfrak{M}_\tau^{\text{irr}}] = 1.$
  - $[R(\tau)] = q^{16} - q^{14} - q^{13} - q^{12} + q^{11} + q^{10} + q^9 - q^7$
  - $m_\kappa(\tau) = 4.$
- 

**Total count of  $\kappa = ((\epsilon_1, \epsilon_1, \epsilon_2, \epsilon_3), (\varepsilon_1, \varepsilon_1, \varepsilon_2, \varepsilon_3))$**

$$\begin{aligned} [R_\kappa^{\text{red}}] &= 2q^{19} + 21q^{18} + 14q^{17} + 8q^{16} + 41q^{15} + 29q^{14} + 27q^{13} + 6q^{12} - 17q^{11} + \\ &q^{10} - 5q^9 + 22q^8 + 10q^7 - 15q^6, \\ [R_\kappa^{\text{irr}}] &= q^{20} + 2q^{19} - 11q^{18} + 4q^{17} + 17q^{16} - 13q^{15} - 4q^{14} - 9q^{13} + 4q^{12} + 21q^{11} + \\ 5q^9 - 22q^8 - 10q^7 + 15q^6, \\ [R_\kappa] &= q^{20} + 4q^{19} + 10q^{18} + 18q^{17} + 25q^{16} + 28q^{15} + 25q^{14} + 18q^{13} + 10q^{12} + \\ 4q^{11} + q^{10}, \\ [\mathfrak{M}_\kappa] &= q^5 + 2q^4 - 10q^3 + 7q^2 + 10q - 15. \end{aligned}$$

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 7. CONFIGURATION  $\boldsymbol{\epsilon} = (\epsilon_1, \epsilon_1, \epsilon_2, \epsilon_3)$  AND  $\boldsymbol{\varepsilon} = (\varepsilon_1, \varepsilon_2, \varepsilon_3, \varepsilon_4)$ 


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$$\xi = ((3, 1), (1, 1)), \quad \sigma_A = (\epsilon_1, \epsilon_1, \epsilon_2, \epsilon_3), \quad \sigma_B = (\epsilon_1, \epsilon_2, \epsilon_3, \epsilon_4).$$

- $[\mathcal{M}_\tau] = 1.$
  - $[\mathcal{G}_\tau] = (q - 1)^2.$
  - $[\mathfrak{M}_\tau^{\text{irr}}] = q^2 - 3q + 3.$
  - $[R(\tau)] = q^{16} - 2q^{15} + 2q^{13} + q^{12} + 2q^{11} - 3q^{10} - 2q^9 - 2q^8 + 3q^6$
  - $m_\kappa(\tau) = 8.$
- 

$$\xi = ((3, 1), (1, 1)), \quad \sigma_A = (\epsilon_1, \epsilon_2, \epsilon_3, \epsilon_1), \quad \sigma_B = (\epsilon_1, \epsilon_3, \epsilon_4, \epsilon_2).$$

- $[\mathcal{M}_\tau] = 1.$
  - $[\mathcal{G}_\tau] = (q - 1)^2.$
  - $[\mathfrak{M}_\tau^{\text{irr}}] = q^4 + 4q^3 - 9q^2 - 3q + 12.$
  - $[R(\tau)] = q^{18} + 5q^{17} - 5q^{16} - 13q^{15} + 3q^{14} + 12q^{13} + 17q^{12} + 4q^{11} - 16q^{10} - 17q^9 - 12q^8 + 9q^7 + 12q^6$
  - $m_\kappa(\tau) = 4.$
- 

$$\xi = ((2, 1), (2, 1)), \quad \sigma_A = (\epsilon_1, \epsilon_2, \epsilon_1, \epsilon_3), \quad \sigma_B = (\epsilon_1, \epsilon_3, \epsilon_2, \epsilon_4).$$

- $[\mathcal{M}_\tau] = 1.$
  - $[\mathcal{G}_\tau] = (q - 1)^2.$
  - $[\mathfrak{M}_\tau^{\text{irr}}] = q^2 - 4q + 4.$
  - $[R(\tau)] = q^{16} - 3q^{15} + 3q^{13} + 2q^{12} + 3q^{11} - 4q^{10} - 3q^9 - 3q^8 + 4q^6$
  - $m_\kappa(\tau) = 6.$
- 

$$\xi = ((2, 1), (1, 1), (1, 1)), \quad \sigma_A = (\epsilon_1, \epsilon_2, \epsilon_1, \epsilon_3), \quad \sigma_B = (\epsilon_1, \epsilon_3, \epsilon_2, \epsilon_4).$$

- $[\mathcal{M}_\tau] = 1.$
  - $[\mathcal{G}_\tau] = (q - 1)^3.$
  - $[\mathfrak{M}_\tau^{\text{irr}}] = q - 2.$
  - $[R(\tau)] = q^{14} - 2q^{12} - 3q^{11} - 3q^{10} + 2q^8 + 3q^7 + 2q^6$
  - $m_\kappa(\tau) = 24.$
- 

$$\xi = ((1, 1), (1, 1), (2, 1)), \quad \sigma_A = (\epsilon_1, \epsilon_1, \epsilon_2, \epsilon_3), \quad \sigma_B = (\epsilon_1, \epsilon_2, \epsilon_3, \epsilon_4).$$

- $[\mathcal{M}_\tau] = 1.$
  - $[\mathcal{G}_\tau] = (q - 1)^3.$
  - $[\mathfrak{M}_\tau^{\text{irr}}] = q - 2.$
  - $[R(\tau)] = q^{14} - 2q^{12} - 3q^{11} - 3q^{10} + 2q^8 + 3q^7 + 2q^6$
  - $m_\kappa(\tau) = 6.$
- 

$$\xi = ((1, 1), (1, 1), (1, 1), (1, 1)), \quad \sigma_A = (\epsilon_1, \epsilon_1, \epsilon_2, \epsilon_3), \quad \sigma_B = (\epsilon_1, \epsilon_2, \epsilon_3, \epsilon_4).$$

- $[\mathcal{M}_\tau] = 1.$
- $[\mathcal{G}_\tau] = (q - 1)^4.$
- $[\mathfrak{M}_\tau^{\text{irr}}] = 1.$
- $[R(\tau)] = q^{12} + 3q^{11} + 5q^{10} + 6q^9 + 5q^8 + 3q^7 + q^6$
- $m_\kappa(\tau) = 12.$

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$$\xi = ((3, 1), (1, 1)), \quad \sigma_A = (\epsilon_1, \epsilon_1, \epsilon_2, \epsilon_3), \quad \sigma_B = (\epsilon_1, \epsilon_2, \epsilon_3, \epsilon_4).$$

- $[\mathcal{M}_\tau] = q^3 - 1.$
  - $[\mathcal{G}_\tau] = (q - 1)^2.$
  - $[\mathfrak{M}_\tau^{\text{irr}}] = q^2 - 3q + 3.$
  - $[R(\tau)] = q^{19} - 2q^{18} + q^{16} + 3q^{15} + 2q^{14} - 5q^{13} - 3q^{12} - 4q^{11} + 3q^{10} + 5q^9 + 2q^8 - 3q^6$
  - $m_\kappa(\tau) = 8.$
- 

$$\xi = ((2, 1), (1, 1), (1, 1)), \quad \sigma_A = (\epsilon_1, \epsilon_2, \epsilon_1, \epsilon_3), \quad \sigma_B = (\epsilon_1, \epsilon_3, \epsilon_2, \epsilon_4).$$

- $[\mathcal{M}_\tau] = q^3 - 1.$
  - $[\mathcal{G}_\tau] = (q - 1)^3.$
  - $[\mathfrak{M}_\tau^{\text{irr}}] = q - 2.$
  - $[R(\tau)] = q^{17} - 2q^{15} - 4q^{14} - 3q^{13} + 2q^{12} + 5q^{11} + 6q^{10} + 2q^9 - 2q^8 - 3q^7 - 2q^6$
  - $m_\kappa(\tau) = 24.$
- 

$$\xi = ((1, 1), (1, 1), (1, 1), (1, 1)), \quad \sigma_A = (\epsilon_1, \epsilon_1, \epsilon_2, \epsilon_3), \quad \sigma_B = (\epsilon_1, \epsilon_2, \epsilon_3, \epsilon_4).$$

- $[\mathcal{M}_\tau] = q^3 - 1.$
  - $[\mathcal{G}_\tau] = (q - 1)^4.$
  - $[\mathfrak{M}_\tau^{\text{irr}}] = 1.$
  - $[R(\tau)] = q^{15} + 3q^{14} + 5q^{13} + 5q^{12} + 2q^{11} - 2q^{10} - 5q^9 - 5q^8 - 3q^7 - q^6$
  - $m_\kappa(\tau) = 24.$
- 

$$\xi = ((3, 1), (1, 1)), \quad \sigma_A = (\epsilon_1, \epsilon_2, \epsilon_3, \epsilon_1), \quad \sigma_B = (\epsilon_1, \epsilon_3, \epsilon_4, \epsilon_2).$$

- $[\mathcal{M}_\tau] = q^3 - q.$
  - $[\mathcal{G}_\tau] = (q - 1)^2 q.$
  - $[\mathfrak{M}_\tau^{\text{irr}}] = q^4 + 4q^3 - 9q^2 - 3q + 12.$
  - $[R(\tau)] = q^{20} + 5q^{19} - 6q^{18} - 18q^{17} + 8q^{16} + 25q^{15} + 14q^{14} - 8q^{13} - 33q^{12} - 21q^{11} + 4q^{10} + 26q^9 + 24q^8 - 9q^7 - 12q^6$
  - $m_\kappa(\tau) = 4.$
- 

$$\xi = ((2, 1), (1, 1), (1, 1)), \quad \sigma_A = (\epsilon_1, \epsilon_2, \epsilon_3, \epsilon_1), \quad \sigma_B = (\epsilon_1, \epsilon_3, \epsilon_4, \epsilon_2).$$

- $[\mathcal{M}_\tau] = q^3 - q.$
  - $[\mathcal{G}_\tau] = (q - 1)^3 q.$
  - $[\mathfrak{M}_\tau^{\text{irr}}] = q - 2.$
  - $[R(\tau)] = q^{16} - 3q^{14} - 3q^{13} - q^{12} + 3q^{11} + 5q^{10} + 3q^9 - 3q^7 - 2q^6$
  - $m_\kappa(\tau) = 24.$
- 

$$\xi = ((1, 1), (2, 1), (1, 1)), \quad \sigma_A = (\epsilon_1, \epsilon_2, \epsilon_3, \epsilon_1), \quad \sigma_B = (\epsilon_1, \epsilon_3, \epsilon_4, \epsilon_2).$$

- $[\mathcal{M}_\tau] = q^3 - q.$
- $[\mathcal{G}_\tau] = (q - 1)^3 q.$
- $[\mathfrak{M}_\tau^{\text{irr}}] = q - 2.$
- $[R(\tau)] = q^{16} - 3q^{14} - 3q^{13} - q^{12} + 3q^{11} + 5q^{10} + 3q^9 - 3q^7 - 2q^6$
- $m_\kappa(\tau) = 12.$

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$$\xi = ((1,1),(1,1),(1,1),(1,1)), \quad \sigma_A = (\epsilon_1, \epsilon_2, \epsilon_3, \epsilon_1), \quad \sigma_B = (\epsilon_1, \epsilon_3, \epsilon_4, \epsilon_2).$$

- $[\mathcal{M}_\tau] = q^3 - q.$
  - $[\mathcal{G}_\tau] = (q-1)^4 q.$
  - $[\mathfrak{M}_\tau^{\text{irr}}] = 1.$
  - $[R(\tau)] = q^{14} + 3q^{13} + 4q^{12} + 3q^{11} - 3q^9 - 4q^8 - 3q^7 - q^6$
  - $m_\kappa(\tau) = 24.$
- 

$$\xi = ((1,1),(1,1),(2,1)), \quad \sigma_A = (\epsilon_1, \epsilon_1, \epsilon_2, \epsilon_3), \quad \sigma_B = (\epsilon_1, \epsilon_2, \epsilon_3, \epsilon_4).$$

- $[\mathcal{M}_\tau] = q^4 - 1.$
  - $[\mathcal{G}_\tau] = (q-1)^3.$
  - $[\mathfrak{M}_\tau^{\text{irr}}] = q - 2.$
  - $[R(\tau)] = q^{18} - 2q^{16} - 3q^{15} - 4q^{14} + 4q^{12} + 6q^{11} + 5q^{10} - 2q^8 - 3q^7 - 2q^6$
  - $m_\kappa(\tau) = 6.$
- 

$$\xi = ((1,1),(1,1),(1,1),(1,1)), \quad \sigma_A = (\epsilon_1, \epsilon_1, \epsilon_2, \epsilon_3), \quad \sigma_B = (\epsilon_1, \epsilon_2, \epsilon_3, \epsilon_4).$$

- $[\mathcal{M}_\tau] = (q^2 - 1)^2.$
  - $[\mathcal{G}_\tau] = (q-1)^4.$
  - $[\mathfrak{M}_\tau^{\text{irr}}] = 1.$
  - $[R(\tau)] = q^{16} + 3q^{15} + 3q^{14} - 4q^{12} - 6q^{11} - 4q^{10} + 3q^8 + 3q^7 + q^6$
  - $m_\kappa(\tau) = 12.$
- 

$$\xi = ((2,1),(2,1)), \quad \sigma_A = (\epsilon_1, \epsilon_2, \epsilon_1, \epsilon_3), \quad \sigma_B = (\epsilon_1, \epsilon_3, \epsilon_2, \epsilon_4).$$

- $[\mathcal{M}_\tau] = q^4 - q.$
  - $[\mathcal{G}_\tau] = (q-1)^2 q.$
  - $[\mathfrak{M}_\tau^{\text{irr}}] = q^2 - 4q + 4.$
  - $[R(\tau)] = q^{19} - 3q^{18} + 2q^{16} + 5q^{15} + 3q^{14} - 7q^{13} - 5q^{12} - 6q^{11} + 4q^{10} + 7q^9 + 3q^8 - 4q^6$
  - $m_\kappa(\tau) = 12.$
- 

$$\xi = ((2,1),(1,1),(1,1)), \quad \sigma_A = (\epsilon_1, \epsilon_2, \epsilon_1, \epsilon_3), \quad \sigma_B = (\epsilon_1, \epsilon_3, \epsilon_2, \epsilon_4).$$

- $[\mathcal{M}_\tau] = (q^2 - q)(q^2 - 1).$
  - $[\mathcal{G}_\tau] = (q-1)^3 q.$
  - $[\mathfrak{M}_\tau^{\text{irr}}] = q - 2.$
  - $[R(\tau)] = q^{17} - q^{16} - 3q^{15} + 2q^{13} + 4q^{12} + 2q^{11} - 2q^{10} - 3q^9 - 3q^8 + q^7 + 2q^6$
  - $m_\kappa(\tau) = 24.$
- 

$$\xi = ((1,1),(1,1),(2,1)), \quad \sigma_A = (\epsilon_1, \epsilon_2, \epsilon_1, \epsilon_3), \quad \sigma_B = (\epsilon_1, \epsilon_3, \epsilon_2, \epsilon_4).$$

- $[\mathcal{M}_\tau] = q^4 - q.$
- $[\mathcal{G}_\tau] = (q-1)^3 q.$
- $[\mathfrak{M}_\tau^{\text{irr}}] = q - 2.$
- $[R(\tau)] = q^{17} - 2q^{15} - 4q^{14} - 3q^{13} + 2q^{12} + 5q^{11} + 6q^{10} + 2q^9 - 2q^8 - 3q^7 - 2q^6$
- $m_\kappa(\tau) = 24.$

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$$\xi = ((1,1),(1,1),(1,1),(1,1)), \quad \sigma_A = (\epsilon_1, \epsilon_2, \epsilon_1, \epsilon_3), \quad \sigma_B = (\epsilon_1, \epsilon_3, \epsilon_2, \epsilon_4).$$

- $[\mathcal{M}_\tau] = (q^2 - q)(q^2 - 1)$ .
  - $[\mathcal{G}_\tau] = (q - 1)^4 q$ .
  - $[\mathfrak{M}_\tau^{\text{irr}}] = 1$ .
  - $[R(\tau)] = q^{15} + 2q^{14} + q^{13} - q^{12} - 3q^{11} - 3q^{10} - q^9 + q^8 + 2q^7 + q^6$
  - $m_\kappa(\tau) = 48$ .
- 

$$\xi = ((2,1),(1,1),(1,1)), \quad \sigma_A = (\epsilon_2, \epsilon_3, \epsilon_1, \epsilon_1), \quad \sigma_B = (\epsilon_3, \epsilon_4, \epsilon_1, \epsilon_2).$$

- $[\mathcal{M}_\tau] = (q^2 - 1)^2$ .
  - $[\mathcal{G}_\tau] = (q - 1)^3$ .
  - $[\mathfrak{M}_\tau^{\text{irr}}] = q - 2$ .
  - $[R(\tau)] = q^{18} - 4q^{16} - 3q^{15} + 2q^{14} + 6q^{13} + 6q^{12} - 5q^{10} - 6q^9 - 2q^8 + 3q^7 + 2q^6$
  - $m_\kappa(\tau) = 6$ .
- 

$$\xi = ((1,1),(1,1),(1,1),(1,1)), \quad \sigma_A = (\epsilon_2, \epsilon_3, \epsilon_1, \epsilon_1), \quad \sigma_B = (\epsilon_3, \epsilon_4, \epsilon_1, \epsilon_2).$$

- $[\mathcal{M}_\tau] = (q^2 - 1)^2$ .
  - $[\mathcal{G}_\tau] = (q - 1)^4$ .
  - $[\mathfrak{M}_\tau^{\text{irr}}] = 1$ .
  - $[R(\tau)] = q^{16} + 3q^{15} + 3q^{14} - 4q^{12} - 6q^{11} - 4q^{10} + 3q^8 + 3q^7 + q^6$
  - $m_\kappa(\tau) = 12$ .
- 

$$\xi = ((1,1),(1,1),(1,1),(1,1)), \quad \sigma_A = (\epsilon_1, \epsilon_1, \epsilon_2, \epsilon_3), \quad \sigma_B = (\epsilon_1, \epsilon_2, \epsilon_3, \epsilon_4).$$

- $[\mathcal{M}_\tau] = (q^2 - 1)(q - 1)q^2$ .
  - $[\mathcal{G}_\tau] = (q - 1)^4$ .
  - $[\mathfrak{M}_\tau^{\text{irr}}] = 1$ .
  - $[R(\tau)] = q^{17} + 2q^{16} + q^{15} - q^{14} - 3q^{13} - 3q^{12} - q^{11} + q^{10} + 2q^9 + q^8$
  - $m_\kappa(\tau) = 24$ .
- 

$$\xi = ((2,1),(1,1),(1,1)), \quad \sigma_A = (\epsilon_1, \epsilon_2, \epsilon_1, \epsilon_3), \quad \sigma_B = (\epsilon_1, \epsilon_3, \epsilon_2, \epsilon_4).$$

- $[\mathcal{M}_\tau] = (q^2 - q)(q - 1)q^2$ .
  - $[\mathcal{G}_\tau] = (q - 1)^3 q$ .
  - $[\mathfrak{M}_\tau^{\text{irr}}] = q - 2$ .
  - $[R(\tau)] = q^{18} - 2q^{17} - q^{16} + q^{15} + q^{14} + 3q^{13} - q^{12} - q^{11} - 2q^{10} - q^9 + 2q^8$
  - $m_\kappa(\tau) = 24$ .
- 

$$\xi = ((1,1),(1,1),(1,1),(1,1)), \quad \sigma_A = (\epsilon_1, \epsilon_2, \epsilon_1, \epsilon_3), \quad \sigma_B = (\epsilon_1, \epsilon_3, \epsilon_2, \epsilon_4).$$

- $[\mathcal{M}_\tau] = (q^2 - q)(q - 1)q^2$ .
- $[\mathcal{G}_\tau] = (q - 1)^4 q$ .
- $[\mathfrak{M}_\tau^{\text{irr}}] = 1$ .
- $[R(\tau)] = q^{16} + q^{15} - q^{13} - 2q^{12} - q^{11} + q^9 + q^8$
- $m_\kappa(\tau) = 48$ .

$$\xi = ((2, 1), (1, 1), (1, 1)), \quad \sigma_A = (\epsilon_1, \epsilon_2, \epsilon_3, \epsilon_1), \quad \sigma_B = (\epsilon_1, \epsilon_3, \epsilon_4, \epsilon_2).$$

- $[\mathcal{M}_\tau] = (q^2 - 1)(q - 1)q^2.$
- $[\mathcal{G}_\tau] = (q - 1)^3 q.$
- $[\mathfrak{M}_\tau^{\text{irr}}] = q - 2.$
- $[R(\tau)] = q^{18} - q^{17} - 3q^{16} + 2q^{14} + 4q^{13} + 2q^{12} - 2q^{11} - 3q^{10} - 3q^9 + q^8 + 2q^7$
- $m_\kappa(\tau) = 24.$

$$\xi = ((1, 1), (1, 1), (1, 1), (1, 1)), \quad \sigma_A = (\epsilon_1, \epsilon_2, \epsilon_3, \epsilon_1), \quad \sigma_B = (\epsilon_1, \epsilon_3, \epsilon_4, \epsilon_2).$$

- $[\mathcal{M}_\tau] = (q^2 - 1)(q - 1)q^2.$
- $[\mathcal{G}_\tau] = (q - 1)^4 q.$
- $[\mathfrak{M}_\tau^{\text{irr}}] = 1.$
- $[R(\tau)] = q^{16} + 2q^{15} + q^{14} - q^{13} - 3q^{12} - 3q^{11} - q^{10} + q^9 + 2q^8 + q^7$
- $m_\kappa(\tau) = 48.$

$$\xi = ((1, 1), (3, 1)), \quad \sigma_A = (\epsilon_1, \epsilon_1, \epsilon_2, \epsilon_3), \quad \sigma_B = (\epsilon_1, \epsilon_2, \epsilon_3, \epsilon_4).$$

- $[\mathcal{M}_\tau] = q^3 - q.$
- $[\mathcal{G}_\tau] = (q - 1)^2 q.$
- $[\mathfrak{M}_\tau^{\text{irr}}] = q^4 + 4q^3 - 9q^2 - 3q + 12.$
- $[R(\tau)] = q^{20} + 5q^{19} - 6q^{18} - 18q^{17} + 8q^{16} + 25q^{15} + 14q^{14} - 8q^{13} - 33q^{12} - 21q^{11} + 4q^{10} + 26q^9 + 24q^8 - 9q^7 - 12q^6$
- $m_\kappa(\tau) = 4.$

$$\xi = ((1, 1), (2, 1), (1, 1)), \quad \sigma_A = (\epsilon_1, \epsilon_1, \epsilon_2, \epsilon_3), \quad \sigma_B = (\epsilon_1, \epsilon_2, \epsilon_3, \epsilon_4).$$

- $[\mathcal{M}_\tau] = (q^2 - q)(q - 1).$
- $[\mathcal{G}_\tau] = (q - 1)^3 q.$
- $[\mathfrak{M}_\tau^{\text{irr}}] = q - 2.$
- $[R(\tau)] = q^{16} - 2q^{15} - q^{14} + q^{13} + q^{12} + 3q^{11} - q^{10} - q^9 - 2q^8 - q^7 + 2q^6$
- $m_\kappa(\tau) = 24.$

$$\xi = ((1, 1), (3, 1)), \quad \sigma_A = (\epsilon_2, \epsilon_1, \epsilon_1, \epsilon_3), \quad \sigma_B = (\epsilon_3, \epsilon_1, \epsilon_2, \epsilon_4).$$

- $[\mathcal{M}_\tau] = q^3 - 1.$
- $[\mathcal{G}_\tau] = (q - 1)^2.$
- $[\mathfrak{M}_\tau^{\text{irr}}] = q^2 - 3q + 3.$
- $[R(\tau)] = q^{19} - 2q^{18} + q^{16} + 3q^{15} + 2q^{14} - 5q^{13} - 3q^{12} - 4q^{11} + 3q^{10} + 5q^9 + 2q^8 - 3q^6$
- $m_\kappa(\tau) = 8.$

$$\xi = ((1, 1), (2, 1), (1, 1)), \quad \sigma_A = (\epsilon_2, \epsilon_1, \epsilon_3, \epsilon_1), \quad \sigma_B = (\epsilon_3, \epsilon_1, \epsilon_4, \epsilon_2).$$

- $[\mathcal{M}_\tau] = (q^2 - 1)(q - 1).$
- $[\mathcal{G}_\tau] = (q - 1)^3.$
- $[\mathfrak{M}_\tau^{\text{irr}}] = q - 2.$
- $[R(\tau)] = q^{17} - q^{16} - 3q^{15} + 2q^{13} + 4q^{12} + 2q^{11} - 2q^{10} - 3q^9 - 3q^8 + q^7 + 2q^6$
- $m_\kappa(\tau) = 24.$

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$$\xi = ((1,1),(1,1),(1,1),(1,1)), \quad \sigma_A = (\epsilon_2, \epsilon_1, \epsilon_1, \epsilon_3), \quad \sigma_B = (\epsilon_3, \epsilon_1, \epsilon_2, \epsilon_4).$$

- $[\mathcal{M}_\tau] = (q-1)^3.$
  - $[\mathcal{G}_\tau] = (q-1)^4.$
  - $[\mathfrak{M}_\tau^{\text{irr}}] = 1.$
  - $[R(\tau)] = q^{15} - q^{13} - q^{12} - q^{11} + q^{10} + q^9 + q^8 - q^6$
  - $m_\kappa(\tau) = 24.$
- 

$$\xi = ((1,1),(2,1),(1,1)), \quad \sigma_A = (\epsilon_1, \epsilon_1, \epsilon_2, \epsilon_3), \quad \sigma_B = (\epsilon_1, \epsilon_2, \epsilon_3, \epsilon_4).$$

- $[\mathcal{M}_\tau] = (q^2-q)(q^2-1)q.$
  - $[\mathcal{G}_\tau] = (q-1)^3q.$
  - $[\mathfrak{M}_\tau^{\text{irr}}] = q-2.$
  - $[R(\tau)] = q^{18} - q^{17} - 3q^{16} + 2q^{14} + 4q^{13} + 2q^{12} - 2q^{11} - 3q^{10} - 3q^9 + q^8 + 2q^7$
  - $m_\kappa(\tau) = 24.$
- 

$$\xi = ((1,1),(2,1),(1,1)), \quad \sigma_A = (\epsilon_1, \epsilon_2, \epsilon_3, \epsilon_1), \quad \sigma_B = (\epsilon_1, \epsilon_3, \epsilon_4, \epsilon_2).$$

- $[\mathcal{M}_\tau] = (q^2-1)^2q.$
  - $[\mathcal{G}_\tau] = (q-1)^3q.$
  - $[\mathfrak{M}_\tau^{\text{irr}}] = q-2.$
  - $[R(\tau)] = q^{18} - 4q^{16} - 3q^{15} + 2q^{14} + 6q^{13} + 6q^{12} - 5q^{10} - 6q^9 - 2q^8 + 3q^7 + 2q^6$
  - $m_\kappa(\tau) = 12.$
- 

$$\xi = ((1,1),(1,1),(1,1),(1,1)), \quad \sigma_A = (\epsilon_1, \epsilon_2, \epsilon_3, \epsilon_1), \quad \sigma_B = (\epsilon_1, \epsilon_3, \epsilon_4, \epsilon_2).$$

- $[\mathcal{M}_\tau] = (q^2-1)(q-1)^2q.$
  - $[\mathcal{G}_\tau] = (q-1)^4q.$
  - $[\mathfrak{M}_\tau^{\text{irr}}] = 1.$
  - $[R(\tau)] = q^{16} + q^{15} - q^{14} - 2q^{13} - 2q^{12} + 2q^{10} + 2q^9 + q^8 - q^7 - q^6$
  - $m_\kappa(\tau) = 24.$
- 

$$\xi = ((1,1),(1,1),(1,1),(1,1)), \quad \sigma_A = (\epsilon_2, \epsilon_1, \epsilon_1, \epsilon_3), \quad \sigma_B = (\epsilon_3, \epsilon_1, \epsilon_2, \epsilon_4).$$

- $[\mathcal{M}_\tau] = (q^2-1)(q-1)^2q.$
  - $[\mathcal{G}_\tau] = (q-1)^4.$
  - $[\mathfrak{M}_\tau^{\text{irr}}] = 1.$
  - $[R(\tau)] = q^{17} + q^{16} - q^{15} - 2q^{14} - 2q^{13} + 2q^{11} + 2q^{10} + q^9 - q^8 - q^7$
  - $m_\kappa(\tau) = 24.$
- 

$$\xi = ((1,1),(2,1),(1,1)), \quad \sigma_A = (\epsilon_2, \epsilon_1, \epsilon_3, \epsilon_1), \quad \sigma_B = (\epsilon_3, \epsilon_1, \epsilon_4, \epsilon_2).$$

- $[\mathcal{M}_\tau] = (q^2-q)(q^2-1)q.$
- $[\mathcal{G}_\tau] = (q-1)^3q.$
- $[\mathfrak{M}_\tau^{\text{irr}}] = q-2.$
- $[R(\tau)] = q^{18} - q^{17} - 3q^{16} + 2q^{14} + 4q^{13} + 2q^{12} - 2q^{11} - 3q^{10} - 3q^9 + q^8 + 2q^7$
- $m_\kappa(\tau) = 24.$

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$$\xi = ((1, 1), (1, 1), (1, 1), (1, 1)), \quad \sigma_A = (\epsilon_2, \epsilon_1, \epsilon_3, \epsilon_1), \quad \sigma_B = (\epsilon_3, \epsilon_1, \epsilon_4, \epsilon_2).$$

- $[\mathcal{M}_\tau] = (q^2 - q)(q - 1)^2 q.$
  - $[\mathcal{G}_\tau] = (q - 1)^4 q.$
  - $[\mathfrak{M}_\tau^{\text{irr}}] = 1.$
  - $[R(\tau)] = q^{16} - q^{14} - q^{13} - q^{12} + q^{11} + q^{10} + q^9 - q^7$
  - $m_\kappa(\tau) = 48.$
- 

$$\xi = ((1, 1), (1, 1), (2, 1)), \quad \sigma_A = (\epsilon_1, \epsilon_2, \epsilon_1, \epsilon_3), \quad \sigma_B = (\epsilon_1, \epsilon_3, \epsilon_2, \epsilon_4).$$

- $[\mathcal{M}_\tau] = (q^2 - 1)(q - 1)q^2.$
  - $[\mathcal{G}_\tau] = (q - 1)^3 q.$
  - $[\mathfrak{M}_\tau^{\text{irr}}] = q - 2.$
  - $[R(\tau)] = q^{18} - q^{17} - 3q^{16} + 2q^{14} + 4q^{13} + 2q^{12} - 2q^{11} - 3q^{10} - 3q^9 + q^8 + 2q^7$
  - $m_\kappa(\tau) = 24.$
- 

$$\xi = ((1, 1), (1, 1), (1, 1), (1, 1)), \quad \sigma_A = (\epsilon_1, \epsilon_2, \epsilon_1, \epsilon_3), \quad \sigma_B = (\epsilon_1, \epsilon_3, \epsilon_2, \epsilon_4).$$

- $[\mathcal{M}_\tau] = (q - 1)^3 q^2.$
  - $[\mathcal{G}_\tau] = (q - 1)^4 q.$
  - $[\mathfrak{M}_\tau^{\text{irr}}] = 1.$
  - $[R(\tau)] = q^{16} - q^{14} - q^{13} - q^{12} + q^{11} + q^{10} + q^9 - q^7$
  - $m_\kappa(\tau) = 48.$
- 

$$\xi = ((1, 1), (1, 1), (2, 1)), \quad \sigma_A = (\epsilon_2, \epsilon_1, \epsilon_1, \epsilon_3), \quad \sigma_B = (\epsilon_3, \epsilon_1, \epsilon_2, \epsilon_4).$$

- $[\mathcal{M}_\tau] = (q^2 - q)(q - 1)q^2.$
  - $[\mathcal{G}_\tau] = (q - 1)^3 q.$
  - $[\mathfrak{M}_\tau^{\text{irr}}] = q - 2.$
  - $[R(\tau)] = q^{18} - 2q^{17} - q^{16} + q^{15} + q^{14} + 3q^{13} - q^{12} - q^{11} - 2q^{10} - q^9 + 2q^8$
  - $m_\kappa(\tau) = 24.$
- 

$$\xi = ((1, 1), (1, 1), (1, 1), (1, 1)), \quad \sigma_A = (\epsilon_2, \epsilon_3, \epsilon_1, \epsilon_1), \quad \sigma_B = (\epsilon_3, \epsilon_4, \epsilon_1, \epsilon_2).$$

- $[\mathcal{M}_\tau] = (q - 1)^3 q^2.$
  - $[\mathcal{G}_\tau] = (q - 1)^4.$
  - $[\mathfrak{M}_\tau^{\text{irr}}] = 1.$
  - $[R(\tau)] = q^{17} - q^{15} - q^{14} - q^{13} + q^{12} + q^{11} + q^{10} - q^8$
  - $m_\kappa(\tau) = 24.$
- 

$$\xi = ((1, 1), (1, 1), (1, 1), (1, 1)), \quad \sigma_A = (\epsilon_1, \epsilon_2, \epsilon_1, \epsilon_3), \quad \sigma_B = (\epsilon_1, \epsilon_3, \epsilon_2, \epsilon_4).$$

- $[\mathcal{M}_\tau] = (q - 1)^3 q^3.$
- $[\mathcal{G}_\tau] = (q - 1)^4 q.$
- $[\mathfrak{M}_\tau^{\text{irr}}] = 1.$
- $[R(\tau)] = q^{17} - q^{15} - q^{14} - q^{13} + q^{12} + q^{11} + q^{10} - q^8$
- $m_\kappa(\tau) = 48.$

---


$$\xi = ((1,1),(1,1),(1,1),(1,1)), \quad \sigma_A = (\epsilon_1, \epsilon_2, \epsilon_3, \epsilon_1), \quad \sigma_B = (\epsilon_1, \epsilon_3, \epsilon_4, \epsilon_2).$$

- $[\mathcal{M}_\tau] = (q-1)^3 q^3.$
  - $[\mathcal{G}_\tau] = (q-1)^4 q.$
  - $[\mathfrak{M}_\tau^{\text{irr}}] = 1.$
  - $[R(\tau)] = q^{17} - q^{15} - q^{14} - q^{13} + q^{12} + q^{11} + q^{10} - q^8$
  - $m_\kappa(\tau) = 48.$
- 

$$\xi = ((1,1),(1,1),(1,1),(1,1)), \quad \sigma_A = (\epsilon_2, \epsilon_1, \epsilon_3, \epsilon_1), \quad \sigma_B = (\epsilon_3, \epsilon_1, \epsilon_4, \epsilon_2).$$

- $[\mathcal{M}_\tau] = (q-1)^3 q^3.$
  - $[\mathcal{G}_\tau] = (q-1)^4 q.$
  - $[\mathfrak{M}_\tau^{\text{irr}}] = 1.$
  - $[R(\tau)] = q^{17} - q^{15} - q^{14} - q^{13} + q^{12} + q^{11} + q^{10} - q^8$
  - $m_\kappa(\tau) = 48.$
- 

**Total count of  $\kappa$**   $= ((\epsilon_1, \epsilon_1, \epsilon_2, \epsilon_3), (\varepsilon_1, \varepsilon_2, \varepsilon_3, \varepsilon_4))$

$$\begin{aligned} [R_\kappa^{\text{red}}] &= 8q^{20} + 68q^{19} + 56q^{18} - 4q^{17} + 2q^{16} + 78q^{15} + 102q^{14} + 46q^{13} - 20q^{12} - \\ &\quad 92q^{11} - 38q^{10} + 30q^9 + 82q^8 + 18q^7 - 48q^6, \\ [R_\kappa^{\text{irr}}] &= q^{22} + 5q^{21} + 6q^{20} - 40q^{19} - 13q^{18} + 57q^{17} + 51q^{16} - 35q^{15} - 74q^{14} - \\ &\quad 32q^{13} + 25q^{12} + 93q^{11} + 38q^{10} - 30q^9 - 82q^8 - 18q^7 + 48q^6, \\ [R_\kappa] &= q^{22} + 5q^{21} + 14q^{20} + 28q^{19} + 43q^{18} + 53q^{17} + 53q^{16} + 43q^{15} + 28q^{14} + \\ &\quad 14q^{13} + 5q^{12} + q^{11}, \\ [\mathfrak{M}_\kappa] &= q^7 + 5q^6 + 7q^5 - 34q^4 + 34q^2 + 18q - 48. \end{aligned}$$

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8. CONFIGURATION  $\epsilon = (\epsilon_1, \epsilon_2, \epsilon_3, \epsilon_4)$  AND  $\varepsilon = (\varepsilon_1, \varepsilon_1, \varepsilon_1, \varepsilon_2)$ 


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$$\xi = ((3, 1), (1, 1)), \quad \sigma_A = (\epsilon_1, \epsilon_2, \epsilon_3, \epsilon_4), \quad \sigma_B = (\epsilon_1, \epsilon_2, \epsilon_1, \epsilon_1).$$

- $[\mathcal{M}_\tau] = 1.$
  - $[\mathcal{G}_\tau] = (q - 1)^2.$
  - $[\mathfrak{M}_\tau^{\text{irr}}] = q^2 - 3q + 3.$
  - $[R(\tau)] = q^{16} - 2q^{15} + 2q^{13} + q^{12} + 2q^{11} - 3q^{10} - 2q^9 - 2q^8 + 3q^6$
  - $m_\kappa(\tau) = 4.$
- 

$$\xi = ((2, 1), (1, 1), (1, 1)), \quad \sigma_A = (\epsilon_1, \epsilon_2, \epsilon_3, \epsilon_4), \quad \sigma_B = (\epsilon_1, \epsilon_2, \epsilon_1, \epsilon_1).$$

- $[\mathcal{M}_\tau] = 1.$
  - $[\mathcal{G}_\tau] = (q - 1)^3.$
  - $[\mathfrak{M}_\tau^{\text{irr}}] = q - 2.$
  - $[R(\tau)] = q^{14} - 2q^{12} - 3q^{11} - 3q^{10} + 2q^8 + 3q^7 + 2q^6$
  - $m_\kappa(\tau) = 6.$
- 

$$\xi = ((1, 1), (1, 1), (1, 1), (1, 1)), \quad \sigma_A = (\epsilon_1, \epsilon_2, \epsilon_3, \epsilon_4), \quad \sigma_B = (\epsilon_1, \epsilon_1, \epsilon_1, \epsilon_2).$$

- $[\mathcal{M}_\tau] = 1.$
  - $[\mathcal{G}_\tau] = (q - 1)^4.$
  - $[\mathfrak{M}_\tau^{\text{irr}}] = 1.$
  - $[R(\tau)] = q^{12} + 3q^{11} + 5q^{10} + 6q^9 + 5q^8 + 3q^7 + q^6$
  - $m_\kappa(\tau) = 4.$
- 

$$\xi = ((3, 1), (1, 1)), \quad \sigma_A = (\epsilon_1, \epsilon_2, \epsilon_3, \epsilon_4), \quad \sigma_B = (\epsilon_1, \epsilon_2, \epsilon_1, \epsilon_1).$$

- $[\mathcal{M}_\tau] = q - 1.$
  - $[\mathcal{G}_\tau] = (q - 1)^2.$
  - $[\mathfrak{M}_\tau^{\text{irr}}] = q^2 - 3q + 3.$
  - $[R(\tau)] = q^{17} - 3q^{16} + 2q^{15} + 2q^{14} - q^{13} + q^{12} - 5q^{11} + q^{10} + 2q^8 + 3q^7 - 3q^6$
  - $m_\kappa(\tau) = 4.$
- 

$$\xi = ((2, 1), (1, 1), (1, 1)), \quad \sigma_A = (\epsilon_1, \epsilon_2, \epsilon_3, \epsilon_4), \quad \sigma_B = (\epsilon_1, \epsilon_2, \epsilon_1, \epsilon_1).$$

- $[\mathcal{M}_\tau] = q - 1.$
  - $[\mathcal{G}_\tau] = (q - 1)^3.$
  - $[\mathfrak{M}_\tau^{\text{irr}}] = q - 2.$
  - $[R(\tau)] = q^{15} - q^{14} - 2q^{13} - q^{12} + 3q^{10} + 2q^9 + q^8 - q^7 - 2q^6$
  - $m_\kappa(\tau) = 12.$
- 

$$\xi = ((1, 1), (1, 1), (1, 1), (1, 1)), \quad \sigma_A = (\epsilon_1, \epsilon_2, \epsilon_3, \epsilon_4), \quad \sigma_B = (\epsilon_1, \epsilon_1, \epsilon_1, \epsilon_2).$$

- $[\mathcal{M}_\tau] = q^3 - 1.$
- $[\mathcal{G}_\tau] = (q - 1)^4.$
- $[\mathfrak{M}_\tau^{\text{irr}}] = 1.$
- $[R(\tau)] = q^{15} + 3q^{14} + 5q^{13} + 5q^{12} + 2q^{11} - 2q^{10} - 5q^9 - 5q^8 - 3q^7 - q^6$
- $m_\kappa(\tau) = 4.$

---


$$\xi = ((1, 1), (1, 1), (1, 1), (1, 1)), \quad \sigma_A = (\epsilon_1, \epsilon_2, \epsilon_3, \epsilon_4), \quad \sigma_B = (\epsilon_1, \epsilon_2, \epsilon_1, \epsilon_1).$$

- $[\mathcal{M}_\tau] = q - 1$ .
  - $[\mathcal{G}_\tau] = (q - 1)^4$ .
  - $[\mathfrak{M}_\tau^{\text{irr}}] = 1$ .
  - $[R(\tau)] = q^{13} + 2q^{12} + 2q^{11} + q^{10} - q^9 - 2q^8 - 2q^7 - q^6$
  - $m_\kappa(\tau) = 12$ .
- 

$$\xi = ((2, 1), (1, 1), (1, 1)), \quad \sigma_A = (\epsilon_1, \epsilon_2, \epsilon_3, \epsilon_4), \quad \sigma_B = (\epsilon_1, \epsilon_2, \epsilon_1, \epsilon_1).$$

- $[\mathcal{M}_\tau] = (q - 1)^2$ .
  - $[\mathcal{G}_\tau] = (q - 1)^3$ .
  - $[\mathfrak{M}_\tau^{\text{irr}}] = q - 2$ .
  - $[R(\tau)] = q^{16} - 2q^{15} - q^{14} + q^{13} + q^{12} + 3q^{11} - q^{10} - q^9 - 2q^8 - q^7 + 2q^6$
  - $m_\kappa(\tau) = 6$ .
- 

$$\xi = ((1, 1), (1, 1), (2, 1)), \quad \sigma_A = (\epsilon_1, \epsilon_2, \epsilon_3, \epsilon_4), \quad \sigma_B = (\epsilon_1, \epsilon_1, \epsilon_1, \epsilon_2).$$

- $[\mathcal{M}_\tau] = q^2 - 1$ .
  - $[\mathcal{G}_\tau] = (q - 1)^3$ .
  - $[\mathfrak{M}_\tau^{\text{irr}}] = q - 2$ .
  - $[R(\tau)] = q^{16} - 3q^{14} - 3q^{13} - q^{12} + 3q^{11} + 5q^{10} + 3q^9 - 3q^7 - 2q^6$
  - $m_\kappa(\tau) = 6$ .
- 

$$\xi = ((1, 1), (1, 1), (1, 1), (1, 1)), \quad \sigma_A = (\epsilon_1, \epsilon_2, \epsilon_3, \epsilon_4), \quad \sigma_B = (\epsilon_1, \epsilon_2, \epsilon_1, \epsilon_1).$$

- $[\mathcal{M}_\tau] = (q - 1)^2$ .
  - $[\mathcal{G}_\tau] = (q - 1)^4$ .
  - $[\mathfrak{M}_\tau^{\text{irr}}] = 1$ .
  - $[R(\tau)] = q^{14} + q^{13} - q^{11} - 2q^{10} - q^9 + q^7 + q^6$
  - $m_\kappa(\tau) = 12$ .
- 

$$\xi = ((1, 1), (1, 1), (1, 1), (1, 1)), \quad \sigma_A = (\epsilon_1, \epsilon_2, \epsilon_3, \epsilon_4), \quad \sigma_B = (\epsilon_1, \epsilon_1, \epsilon_2, \epsilon_1).$$

- $[\mathcal{M}_\tau] = (q^2 - 1)(q - 1)$ .
  - $[\mathcal{G}_\tau] = (q - 1)^4$ .
  - $[\mathfrak{M}_\tau^{\text{irr}}] = 1$ .
  - $[R(\tau)] = q^{15} + 2q^{14} + q^{13} - q^{12} - 3q^{11} - 3q^{10} - q^9 + q^8 + 2q^7 + q^6$
  - $m_\kappa(\tau) = 12$ .
- 

$$\xi = ((1, 1), (3, 1)), \quad \sigma_A = (\epsilon_1, \epsilon_2, \epsilon_3, \epsilon_4), \quad \sigma_B = (\epsilon_1, \epsilon_1, \epsilon_1, \epsilon_2).$$

- $[\mathcal{M}_\tau] = q - 1$ .
- $[\mathcal{G}_\tau] = (q - 1)^2$ .
- $[\mathfrak{M}_\tau^{\text{irr}}] = q^2 - 3q + 3$ .
- $[R(\tau)] = q^{17} - 3q^{16} + 2q^{15} + 2q^{14} - q^{13} + q^{12} - 5q^{11} + q^{10} + 2q^8 + 3q^7 - 3q^6$
- $m_\kappa(\tau) = 4$ .

$$\xi = ((1,1),(1,1),(1,1),(1,1)), \quad \sigma_A = (\epsilon_1, \epsilon_2, \epsilon_3, \epsilon_4), \quad \sigma_B = (\epsilon_2, \epsilon_1, \epsilon_1, \epsilon_1).$$

- $[\mathcal{M}_\tau] = (q-1)^3$ .
- $[\mathcal{G}_\tau] = (q-1)^4$ .
- $[\mathfrak{M}_\tau^{\text{irr}}] = 1$ .
- $[R(\tau)] = q^{15} - q^{13} - q^{12} - q^{11} + q^{10} + q^9 + q^8 - q^6$
- $m_\kappa(\tau) = 4$ .

$$\xi = ((1,1),(2,1),(1,1)), \quad \sigma_A = (\epsilon_1, \epsilon_2, \epsilon_3, \epsilon_4), \quad \sigma_B = (\epsilon_1, \epsilon_2, \epsilon_1, \epsilon_1).$$

- $[\mathcal{M}_\tau] = (q-1)^2$ .
- $[\mathcal{G}_\tau] = (q-1)^3$ .
- $[\mathfrak{M}_\tau^{\text{irr}}] = q-2$ .
- $[R(\tau)] = q^{16} - 2q^{15} - q^{14} + q^{13} + q^{12} + 3q^{11} - q^{10} - q^9 - 2q^8 - q^7 + 2q^6$
- $m_\kappa(\tau) = 12$ .

$$\xi = ((1,1),(1,1),(1,1),(1,1)), \quad \sigma_A = (\epsilon_1, \epsilon_2, \epsilon_3, \epsilon_4), \quad \sigma_B = (\epsilon_1, \epsilon_2, \epsilon_1, \epsilon_1).$$

- $[\mathcal{M}_\tau] = (q-1)^3$ .
- $[\mathcal{G}_\tau] = (q-1)^4$ .
- $[\mathfrak{M}_\tau^{\text{irr}}] = 1$ .
- $[R(\tau)] = q^{15} - q^{13} - q^{12} - q^{11} + q^{10} + q^9 + q^8 - q^6$
- $m_\kappa(\tau) = 12$ .

**Total count of  $\kappa = ((\epsilon_1, \epsilon_2, \epsilon_3, \epsilon_4), (\varepsilon_1, \varepsilon_1, \varepsilon_1, \varepsilon_2))$**

$$\begin{aligned} [R_\kappa^{\text{red}}] &= 8q^{17} + 4q^{16} + 16q^{15} + 22q^{14} + 16q^{13} + 20q^{12} + 2q^{11} + 6q^{10} + 6q^9 + 6q^7 - 4q^6, \\ [R_\kappa^{\text{irr}}] &= q^{18} - 4q^{17} + 5q^{16} - q^{15} - 3q^{14} + 3q^{13} - 5q^{12} + 7q^{11} - 2q^{10} + q^9 - 6q^7 + 4q^6, \\ [R_\kappa] &= q^{18} + 4q^{17} + 9q^{16} + 15q^{15} + 19q^{14} + 19q^{13} + 15q^{12} + 9q^{11} + 4q^{10} + q^9, \\ [\mathfrak{M}_\kappa] &= q^3 - 4q^2 + 6q - 4. \end{aligned}$$

9. CONFIGURATION  $\boldsymbol{\epsilon} = (\epsilon_1, \epsilon_2, \epsilon_3, \epsilon_4)$  AND  $\boldsymbol{\varepsilon} = (\varepsilon_1, \varepsilon_1, \varepsilon_2, \varepsilon_2)$

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$$\xi = ((3, 1), (1, 1)), \quad \sigma_A = (\epsilon_1, \epsilon_2, \epsilon_3, \epsilon_4), \quad \sigma_B = (\epsilon_1, \epsilon_1, \epsilon_2, \epsilon_2).$$

- $[\mathcal{M}_\tau] = 1.$
  - $[\mathcal{G}_\tau] = (q - 1)^2.$
  - $[\mathfrak{M}_\tau^{\text{irr}}] = q^2 - 3q + 3.$
  - $[R(\tau)] = q^{16} - 2q^{15} + 2q^{13} + q^{12} + 2q^{11} - 3q^{10} - 2q^9 - 2q^8 + 3q^6$
  - $m_\kappa(\tau) = 8.$
- 

$$\xi = ((2, 1), (2, 1)), \quad \sigma_A = (\epsilon_1, \epsilon_2, \epsilon_3, \epsilon_4), \quad \sigma_B = (\epsilon_1, \epsilon_2, \epsilon_2, \epsilon_1).$$

- $[\mathcal{M}_\tau] = 1.$
  - $[\mathcal{G}_\tau] = (q - 1)^2.$
  - $[\mathfrak{M}_\tau^{\text{irr}}] = q^2 - 4q + 4.$
  - $[R(\tau)] = q^{16} - 3q^{15} + 3q^{13} + 2q^{12} + 3q^{11} - 4q^{10} - 3q^9 - 3q^8 + 4q^6$
  - $m_\kappa(\tau) = 3.$
- 

$$\xi = ((2, 1), (1, 1), (1, 1)), \quad \sigma_A = (\epsilon_1, \epsilon_2, \epsilon_3, \epsilon_4), \quad \sigma_B = (\epsilon_1, \epsilon_2, \epsilon_2, \epsilon_1).$$

- $[\mathcal{M}_\tau] = 1.$
  - $[\mathcal{G}_\tau] = (q - 1)^3.$
  - $[\mathfrak{M}_\tau^{\text{irr}}] = q - 2.$
  - $[R(\tau)] = q^{14} - 2q^{12} - 3q^{11} - 3q^{10} + 2q^8 + 3q^7 + 2q^6$
  - $m_\kappa(\tau) = 12.$
- 

$$\xi = ((1, 1), (1, 1), (1, 1), (1, 1)), \quad \sigma_A = (\epsilon_1, \epsilon_2, \epsilon_3, \epsilon_4), \quad \sigma_B = (\epsilon_1, \epsilon_1, \epsilon_2, \epsilon_2).$$

- $[\mathcal{M}_\tau] = 1.$
  - $[\mathcal{G}_\tau] = (q - 1)^4.$
  - $[\mathfrak{M}_\tau^{\text{irr}}] = 1.$
  - $[R(\tau)] = q^{12} + 3q^{11} + 5q^{10} + 6q^9 + 5q^8 + 3q^7 + q^6$
  - $m_\kappa(\tau) = 6.$
- 

$$\xi = ((3, 1), (1, 1)), \quad \sigma_A = (\epsilon_1, \epsilon_2, \epsilon_3, \epsilon_4), \quad \sigma_B = (\epsilon_1, \epsilon_1, \epsilon_2, \epsilon_2).$$

- $[\mathcal{M}_\tau] = q^2 - 1.$
  - $[\mathcal{G}_\tau] = (q - 1)^2.$
  - $[\mathfrak{M}_\tau^{\text{irr}}] = q^2 - 3q + 3.$
  - $[R(\tau)] = q^{18} - 2q^{17} - q^{16} + 4q^{15} + q^{14} - 4q^{12} - 4q^{11} + q^{10} + 2q^9 + 5q^8 - 3q^6$
  - $m_\kappa(\tau) = 8.$
- 

$$\xi = ((2, 1), (1, 1), (1, 1)), \quad \sigma_A = (\epsilon_1, \epsilon_2, \epsilon_3, \epsilon_4), \quad \sigma_B = (\epsilon_1, \epsilon_2, \epsilon_2, \epsilon_1).$$

- $[\mathcal{M}_\tau] = q^2 - 1.$
- $[\mathcal{G}_\tau] = (q - 1)^3.$
- $[\mathfrak{M}_\tau^{\text{irr}}] = q - 2.$
- $[R(\tau)] = q^{16} - 3q^{14} - 3q^{13} - q^{12} + 3q^{11} + 5q^{10} + 3q^9 - 3q^7 - 2q^6$
- $m_\kappa(\tau) = 24.$

---


$$\xi = ((1,1),(1,1),(1,1),(1,1)), \quad \sigma_A = (\epsilon_1, \epsilon_2, \epsilon_3, \epsilon_4), \quad \sigma_B = (\epsilon_1, \epsilon_1, \epsilon_2, \epsilon_2).$$

- $[\mathcal{M}_\tau] = q^2 - 1$ .
  - $[\mathcal{G}_\tau] = (q-1)^4$ .
  - $[\mathfrak{M}_\tau^{\text{irr}}] = 1$ .
  - $[R(\tau)] = q^{14} + 3q^{13} + 4q^{12} + 3q^{11} - 3q^9 - 4q^8 - 3q^7 - q^6$
  - $m_\kappa(\tau) = 24$ .
- 

$$\xi = ((2,1),(2,1)), \quad \sigma_A = (\epsilon_1, \epsilon_2, \epsilon_3, \epsilon_4), \quad \sigma_B = (\epsilon_1, \epsilon_2, \epsilon_2, \epsilon_1).$$

- $[\mathcal{M}_\tau] = q^2 - 1$ .
  - $[\mathcal{G}_\tau] = (q-1)^2$ .
  - $[\mathfrak{M}_\tau^{\text{irr}}] = q^2 - 4q + 4$ .
  - $[R(\tau)] = q^{18} - 3q^{17} - q^{16} + 6q^{15} + 2q^{14} - 6q^{12} - 6q^{11} + q^{10} + 3q^9 + 7q^8 - 4q^6$
  - $m_\kappa(\tau) = 6$ .
- 

$$\xi = ((2,1),(1,1),(1,1)), \quad \sigma_A = (\epsilon_1, \epsilon_2, \epsilon_3, \epsilon_4), \quad \sigma_B = (\epsilon_1, \epsilon_2, \epsilon_2, \epsilon_1).$$

- $[\mathcal{M}_\tau] = (q-1)^2$ .
  - $[\mathcal{G}_\tau] = (q-1)^3$ .
  - $[\mathfrak{M}_\tau^{\text{irr}}] = q - 2$ .
  - $[R(\tau)] = q^{16} - 2q^{15} - q^{14} + q^{13} + q^{12} + 3q^{11} - q^{10} - q^9 - 2q^8 - q^7 + 2q^6$
  - $m_\kappa(\tau) = 12$ .
- 

$$\xi = ((1,1),(1,1),(2,1)), \quad \sigma_A = (\epsilon_1, \epsilon_2, \epsilon_3, \epsilon_4), \quad \sigma_B = (\epsilon_1, \epsilon_2, \epsilon_2, \epsilon_1).$$

- $[\mathcal{M}_\tau] = q^2 - 1$ .
  - $[\mathcal{G}_\tau] = (q-1)^3$ .
  - $[\mathfrak{M}_\tau^{\text{irr}}] = q - 2$ .
  - $[R(\tau)] = q^{16} - 3q^{14} - 3q^{13} - q^{12} + 3q^{11} + 5q^{10} + 3q^9 - 3q^7 - 2q^6$
  - $m_\kappa(\tau) = 12$ .
- 

$$\xi = ((1,1),(1,1),(1,1),(1,1)), \quad \sigma_A = (\epsilon_1, \epsilon_2, \epsilon_3, \epsilon_4), \quad \sigma_B = (\epsilon_1, \epsilon_1, \epsilon_2, \epsilon_2).$$

- $[\mathcal{M}_\tau] = (q^2 - 1)^2$ .
  - $[\mathcal{G}_\tau] = (q-1)^4$ .
  - $[\mathfrak{M}_\tau^{\text{irr}}] = 1$ .
  - $[R(\tau)] = q^{16} + 3q^{15} + 3q^{14} - 4q^{12} - 6q^{11} - 4q^{10} + 3q^8 + 3q^7 + q^6$
  - $m_\kappa(\tau) = 12$ .
- 

$$\xi = ((1,1),(1,1),(1,1),(1,1)), \quad \sigma_A = (\epsilon_1, \epsilon_2, \epsilon_3, \epsilon_4), \quad \sigma_B = (\epsilon_1, \epsilon_2, \epsilon_2, \epsilon_1).$$

- $[\mathcal{M}_\tau] = (q-1)^2$ .
- $[\mathcal{G}_\tau] = (q-1)^4$ .
- $[\mathfrak{M}_\tau^{\text{irr}}] = 1$ .
- $[R(\tau)] = q^{14} + q^{13} - q^{11} - 2q^{10} - q^9 + q^7 + q^6$
- $m_\kappa(\tau) = 24$ .

---


$$\xi = ((2, 1), (1, 1), (1, 1)), \quad \sigma_A = (\epsilon_1, \epsilon_2, \epsilon_3, \epsilon_4), \quad \sigma_B = (\epsilon_1, \epsilon_2, \epsilon_2, \epsilon_1).$$

- $[\mathcal{M}_\tau] = (q - 1)^2 q.$
  - $[\mathcal{G}_\tau] = (q - 1)^3.$
  - $[\mathfrak{M}_\tau^{\text{irr}}] = q - 2.$
  - $[R(\tau)] = q^{17} - 2q^{16} - q^{15} + q^{14} + q^{13} + 3q^{12} - q^{11} - q^{10} - 2q^9 - q^8 + 2q^7$
  - $m_\kappa(\tau) = 24.$
- 

$$\xi = ((1, 1), (1, 1), (1, 1), (1, 1)), \quad \sigma_A = (\epsilon_1, \epsilon_2, \epsilon_3, \epsilon_4), \quad \sigma_B = (\epsilon_1, \epsilon_2, \epsilon_2, \epsilon_1).$$

- $[\mathcal{M}_\tau] = (q - 1)^2 q.$
  - $[\mathcal{G}_\tau] = (q - 1)^4.$
  - $[\mathfrak{M}_\tau^{\text{irr}}] = 1.$
  - $[R(\tau)] = q^{15} + q^{14} - q^{12} - 2q^{11} - q^{10} + q^8 + q^7$
  - $m_\kappa(\tau) = 48.$
- 

$$\xi = ((1, 1), (3, 1)), \quad \sigma_A = (\epsilon_1, \epsilon_2, \epsilon_3, \epsilon_4), \quad \sigma_B = (\epsilon_1, \epsilon_1, \epsilon_2, \epsilon_2).$$

- $[\mathcal{M}_\tau] = q^2 - 1.$
  - $[\mathcal{G}_\tau] = (q - 1)^2.$
  - $[\mathfrak{M}_\tau^{\text{irr}}] = q^2 - 3q + 3.$
  - $[R(\tau)] = q^{18} - 2q^{17} - q^{16} + 4q^{15} + q^{14} - 4q^{12} - 4q^{11} + q^{10} + 2q^9 + 5q^8 - 3q^6$
  - $m_\kappa(\tau) = 8.$
- 

$$\xi = ((1, 1), (2, 1), (1, 1)), \quad \sigma_A = (\epsilon_1, \epsilon_2, \epsilon_3, \epsilon_4), \quad \sigma_B = (\epsilon_1, \epsilon_1, \epsilon_2, \epsilon_2).$$

- $[\mathcal{M}_\tau] = (q - 1)^2.$
  - $[\mathcal{G}_\tau] = (q - 1)^3.$
  - $[\mathfrak{M}_\tau^{\text{irr}}] = q - 2.$
  - $[R(\tau)] = q^{16} - 2q^{15} - q^{14} + q^{13} + q^{12} + 3q^{11} - q^{10} - q^9 - 2q^8 - q^7 + 2q^6$
  - $m_\kappa(\tau) = 24.$
- 

$$\xi = ((1, 1), (2, 1), (1, 1)), \quad \sigma_A = (\epsilon_1, \epsilon_2, \epsilon_3, \epsilon_4), \quad \sigma_B = (\epsilon_1, \epsilon_1, \epsilon_2, \epsilon_2).$$

- $[\mathcal{M}_\tau] = (q - 1)^2 q.$
  - $[\mathcal{G}_\tau] = (q - 1)^3.$
  - $[\mathfrak{M}_\tau^{\text{irr}}] = q - 2.$
  - $[R(\tau)] = q^{17} - 2q^{16} - q^{15} + q^{14} + q^{13} + 3q^{12} - q^{11} - q^{10} - 2q^9 - q^8 + 2q^7$
  - $m_\kappa(\tau) = 24.$
- 

$$\xi = ((1, 1), (1, 1), (1, 1), (1, 1)), \quad \sigma_A = (\epsilon_1, \epsilon_2, \epsilon_3, \epsilon_4), \quad \sigma_B = (\epsilon_1, \epsilon_2, \epsilon_2, \epsilon_1).$$

- $[\mathcal{M}_\tau] = (q^2 - 1)(q - 1)^2.$
- $[\mathcal{G}_\tau] = (q - 1)^4.$
- $[\mathfrak{M}_\tau^{\text{irr}}] = 1.$
- $[R(\tau)] = q^{16} + q^{15} - q^{14} - 2q^{13} - 2q^{12} + 2q^{10} + 2q^9 + q^8 - q^7 - q^6$
- $m_\kappa(\tau) = 24.$

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$$\xi = ((1,1), (1,1), (2,1)), \quad \sigma_A = (\epsilon_1, \epsilon_2, \epsilon_3, \epsilon_4), \quad \sigma_B = (\epsilon_1, \epsilon_2, \epsilon_2, \epsilon_1).$$

- $[\mathcal{M}_\tau] = (q-1)^2 q.$
  - $[\mathcal{G}_\tau] = (q-1)^3.$
  - $[\mathfrak{M}_\tau^{\text{irr}}] = q-2.$
  - $[R(\tau)] = q^{17} - 2q^{16} - q^{15} + q^{14} + q^{13} + 3q^{12} - q^{11} - q^{10} - 2q^9 - q^8 + 2q^7$
  - $m_\kappa(\tau) = 24.$
- 

$$\xi = ((1,1), (1,1), (1,1), (1,1)), \quad \sigma_A = (\epsilon_1, \epsilon_2, \epsilon_3, \epsilon_4), \quad \sigma_B = (\epsilon_1, \epsilon_2, \epsilon_1, \epsilon_2).$$

- $[\mathcal{M}_\tau] = (q-1)^3 q.$
  - $[\mathcal{G}_\tau] = (q-1)^4.$
  - $[\mathfrak{M}_\tau^{\text{irr}}] = 1.$
  - $[R(\tau)] = q^{16} - q^{14} - q^{13} - q^{12} + q^{11} + q^{10} + q^9 - q^7$
  - $m_\kappa(\tau) = 48.$
- 

**Total count of  $\kappa = ((\epsilon_1, \epsilon_2, \epsilon_3, \epsilon_4), (\varepsilon_1, \varepsilon_1, \varepsilon_2, \varepsilon_2))$**

$$\begin{aligned} [R_\kappa^{\text{red}}] &= 22q^{18} + 22q^{17} + q^{16} + 39q^{15} + 28q^{14} + 25q^{13} + 16q^{12} - 21q^{11} + 4q^{10} - \\ &11q^9 + 19q^8 + 18q^7 - 18q^6, \\ [R_\kappa^{\text{irr}}] &= q^{20} + 4q^{19} - 12q^{18} - 4q^{17} + 24q^{16} - 11q^{15} - 3q^{14} - 7q^{13} - 6q^{12} + 25q^{11} - \\ 3q^{10} + 11q^9 - 19q^8 - 18q^7 + 18q^6, \\ [R_\kappa] &= q^{20} + 4q^{19} + 10q^{18} + 18q^{17} + 25q^{16} + 28q^{15} + 25q^{14} + 18q^{13} + 10q^{12} + \\ 4q^{11} + q^{10}, \\ [\mathfrak{M}_\kappa] &= q^5 + 4q^4 - 11q^3 + q^2 + 18q - 18. \end{aligned}$$

10. CONFIGURATION  $\boldsymbol{\epsilon} = (\epsilon_1, \epsilon_2, \epsilon_3, \epsilon_4)$  AND  $\boldsymbol{\varepsilon} = (\varepsilon_1, \varepsilon_1, \varepsilon_2, \varepsilon_3)$ 

$$\xi = ((3, 1), (1, 1)), \quad \sigma_A = (\epsilon_1, \epsilon_2, \epsilon_3, \epsilon_4), \quad \sigma_B = (\epsilon_1, \epsilon_1, \epsilon_2, \epsilon_3).$$

- $[\mathcal{M}_\tau] = 1.$
- $[\mathcal{G}_\tau] = (q - 1)^2.$
- $[\mathfrak{M}_\tau^{\text{irr}}] = q^2 - 3q + 3.$
- $[R(\tau)] = q^{16} - 2q^{15} + 2q^{13} + q^{12} + 2q^{11} - 3q^{10} - 2q^9 - 2q^8 + 3q^6$
- $m_\kappa(\tau) = 8.$

$$\xi = ((3, 1), (1, 1)), \quad \sigma_A = (\epsilon_1, \epsilon_2, \epsilon_3, \epsilon_4), \quad \sigma_B = (\epsilon_2, \epsilon_3, \epsilon_1, \epsilon_1).$$

- $[\mathcal{M}_\tau] = 1.$
- $[\mathcal{G}_\tau] = (q - 1)^2.$
- $[\mathfrak{M}_\tau^{\text{irr}}] = q^4 + 4q^3 - 9q^2 - 3q + 12.$
- $[R(\tau)] = q^{18} + 5q^{17} - 5q^{16} - 13q^{15} + 3q^{14} + 12q^{13} + 17q^{12} + 4q^{11} - 16q^{10} - 17q^9 - 12q^8 + 9q^7 + 12q^6$
- $m_\kappa(\tau) = 4.$

$$\xi = ((2, 1), (2, 1)), \quad \sigma_A = (\epsilon_1, \epsilon_2, \epsilon_3, \epsilon_4), \quad \sigma_B = (\epsilon_1, \epsilon_2, \epsilon_3, \epsilon_1).$$

- $[\mathcal{M}_\tau] = 1.$
- $[\mathcal{G}_\tau] = (q - 1)^2.$
- $[\mathfrak{M}_\tau^{\text{irr}}] = q^2 - 4q + 4.$
- $[R(\tau)] = q^{16} - 3q^{15} + 3q^{13} + 2q^{12} + 3q^{11} - 4q^{10} - 3q^9 - 3q^8 + 4q^6$
- $m_\kappa(\tau) = 6.$

$$\xi = ((2, 1), (1, 1), (1, 1)), \quad \sigma_A = (\epsilon_1, \epsilon_2, \epsilon_3, \epsilon_4), \quad \sigma_B = (\epsilon_2, \epsilon_3, \epsilon_1, \epsilon_1).$$

- $[\mathcal{M}_\tau] = 1.$
- $[\mathcal{G}_\tau] = (q - 1)^3.$
- $[\mathfrak{M}_\tau^{\text{irr}}] = q - 2.$
- $[R(\tau)] = q^{14} - 2q^{12} - 3q^{11} - 3q^{10} + 2q^8 + 3q^7 + 2q^6$
- $m_\kappa(\tau) = 6.$

$$\xi = ((2, 1), (1, 1), (1, 1)), \quad \sigma_A = (\epsilon_1, \epsilon_2, \epsilon_3, \epsilon_4), \quad \sigma_B = (\epsilon_1, \epsilon_2, \epsilon_3, \epsilon_1).$$

- $[\mathcal{M}_\tau] = 1.$
- $[\mathcal{G}_\tau] = (q - 1)^3.$
- $[\mathfrak{M}_\tau^{\text{irr}}] = q - 2.$
- $[R(\tau)] = q^{14} - 2q^{12} - 3q^{11} - 3q^{10} + 2q^8 + 3q^7 + 2q^6$
- $m_\kappa(\tau) = 24.$

$$\xi = ((1, 1), (1, 1), (1, 1), (1, 1)), \quad \sigma_A = (\epsilon_1, \epsilon_2, \epsilon_3, \epsilon_4), \quad \sigma_B = (\epsilon_1, \epsilon_1, \epsilon_2, \epsilon_3).$$

- $[\mathcal{M}_\tau] = 1.$
- $[\mathcal{G}_\tau] = (q - 1)^4.$
- $[\mathfrak{M}_\tau^{\text{irr}}] = 1.$
- $[R(\tau)] = q^{12} + 3q^{11} + 5q^{10} + 6q^9 + 5q^8 + 3q^7 + q^6$
- $m_\kappa(\tau) = 12.$

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$$\xi = ((3, 1), (1, 1)), \quad \sigma_A = (\epsilon_1, \epsilon_2, \epsilon_3, \epsilon_4), \quad \sigma_B = (\epsilon_1, \epsilon_1, \epsilon_2, \epsilon_3).$$

- $[\mathcal{M}_\tau] = q^3 - 1.$
  - $[\mathcal{G}_\tau] = (q - 1)^2.$
  - $[\mathfrak{M}_\tau^{\text{irr}}] = q^2 - 3q + 3.$
  - $[R(\tau)] = q^{19} - 2q^{18} + q^{16} + 3q^{15} + 2q^{14} - 5q^{13} - 3q^{12} - 4q^{11} + 3q^{10} + 5q^9 + 2q^8 - 3q^6$
  - $m_\kappa(\tau) = 8.$
- 

$$\xi = ((3, 1), (1, 1)), \quad \sigma_A = (\epsilon_1, \epsilon_2, \epsilon_3, \epsilon_4), \quad \sigma_B = (\epsilon_2, \epsilon_3, \epsilon_1, \epsilon_1).$$

- $[\mathcal{M}_\tau] = q^2 - 1.$
  - $[\mathcal{G}_\tau] = (q - 1)^2.$
  - $[\mathfrak{M}_\tau^{\text{irr}}] = q^4 + 4q^3 - 9q^2 - 3q + 12.$
  - $[R(\tau)] = q^{20} + 5q^{19} - 6q^{18} - 18q^{17} + 8q^{16} + 25q^{15} + 14q^{14} - 8q^{13} - 33q^{12} - 21q^{11} + 4q^{10} + 26q^9 + 24q^8 - 9q^7 - 12q^6$
  - $m_\kappa(\tau) = 4.$
- 

$$\xi = ((2, 1), (1, 1), (1, 1)), \quad \sigma_A = (\epsilon_1, \epsilon_2, \epsilon_3, \epsilon_4), \quad \sigma_B = (\epsilon_2, \epsilon_3, \epsilon_1, \epsilon_1).$$

- $[\mathcal{M}_\tau] = q^2 - 1.$
  - $[\mathcal{G}_\tau] = (q - 1)^3.$
  - $[\mathfrak{M}_\tau^{\text{irr}}] = q - 2.$
  - $[R(\tau)] = q^{16} - 3q^{14} - 3q^{13} - q^{12} + 3q^{11} + 5q^{10} + 3q^9 - 3q^7 - 2q^6$
  - $m_\kappa(\tau) = 12.$
- 

$$\xi = ((2, 1), (1, 1), (1, 1)), \quad \sigma_A = (\epsilon_1, \epsilon_2, \epsilon_3, \epsilon_4), \quad \sigma_B = (\epsilon_1, \epsilon_2, \epsilon_3, \epsilon_1).$$

- $[\mathcal{M}_\tau] = q^2 - 1.$
  - $[\mathcal{G}_\tau] = (q - 1)^3.$
  - $[\mathfrak{M}_\tau^{\text{irr}}] = q - 2.$
  - $[R(\tau)] = q^{16} - 3q^{14} - 3q^{13} - q^{12} + 3q^{11} + 5q^{10} + 3q^9 - 3q^7 - 2q^6$
  - $m_\kappa(\tau) = 24.$
- 

$$\xi = ((2, 1), (1, 1), (1, 1)), \quad \sigma_A = (\epsilon_1, \epsilon_2, \epsilon_3, \epsilon_4), \quad \sigma_B = (\epsilon_2, \epsilon_1, \epsilon_1, \epsilon_3).$$

- $[\mathcal{M}_\tau] = q^3 - 1.$
  - $[\mathcal{G}_\tau] = (q - 1)^3.$
  - $[\mathfrak{M}_\tau^{\text{irr}}] = q - 2.$
  - $[R(\tau)] = q^{17} - 2q^{15} - 4q^{14} - 3q^{13} + 2q^{12} + 5q^{11} + 6q^{10} + 2q^9 - 2q^8 - 3q^7 - 2q^6$
  - $m_\kappa(\tau) = 24.$
- 

$$\xi = ((1, 1), (1, 1), (1, 1), (1, 1)), \quad \sigma_A = (\epsilon_1, \epsilon_2, \epsilon_3, \epsilon_4), \quad \sigma_B = (\epsilon_1, \epsilon_1, \epsilon_2, \epsilon_3).$$

- $[\mathcal{M}_\tau] = q^3 - 1.$
- $[\mathcal{G}_\tau] = (q - 1)^4.$
- $[\mathfrak{M}_\tau^{\text{irr}}] = 1.$
- $[R(\tau)] = q^{15} + 3q^{14} + 5q^{13} + 5q^{12} + 2q^{11} - 2q^{10} - 5q^9 - 5q^8 - 3q^7 - q^6$
- $m_\kappa(\tau) = 24.$

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$$\xi = ((1,1),(1,1),(1,1),(1,1)), \quad \sigma_A = (\epsilon_1, \epsilon_2, \epsilon_3, \epsilon_4), \quad \sigma_B = (\epsilon_2, \epsilon_3, \epsilon_1, \epsilon_1).$$

- $[\mathcal{M}_\tau] = q^2 - 1.$
  - $[\mathcal{G}_\tau] = (q - 1)^4.$
  - $[\mathfrak{M}_\tau^{\text{irr}}] = 1.$
  - $[R(\tau)] = q^{14} + 3q^{13} + 4q^{12} + 3q^{11} - 3q^9 - 4q^8 - 3q^7 - q^6$
  - $m_\kappa(\tau) = 24.$
- 

$$\xi = ((2,1),(2,1)), \quad \sigma_A = (\epsilon_1, \epsilon_2, \epsilon_3, \epsilon_4), \quad \sigma_B = (\epsilon_1, \epsilon_2, \epsilon_3, \epsilon_1).$$

- $[\mathcal{M}_\tau] = q^3 - 1.$
  - $[\mathcal{G}_\tau] = (q - 1)^2.$
  - $[\mathfrak{M}_\tau^{\text{irr}}] = q^2 - 4q + 4.$
  - $[R(\tau)] = q^{19} - 3q^{18} + 2q^{16} + 5q^{15} + 3q^{14} - 7q^{13} - 5q^{12} - 6q^{11} + 4q^{10} + 7q^9 + 3q^8 - 4q^6$
  - $m_\kappa(\tau) = 12.$
- 

$$\xi = ((2,1),(1,1),(1,1)), \quad \sigma_A = (\epsilon_1, \epsilon_2, \epsilon_3, \epsilon_4), \quad \sigma_B = (\epsilon_2, \epsilon_3, \epsilon_1, \epsilon_1).$$

- $[\mathcal{M}_\tau] = (q^2 - 1)^2.$
  - $[\mathcal{G}_\tau] = (q - 1)^3.$
  - $[\mathfrak{M}_\tau^{\text{irr}}] = q - 2.$
  - $[R(\tau)] = q^{18} - 4q^{16} - 3q^{15} + 2q^{14} + 6q^{13} + 6q^{12} - 5q^{10} - 6q^9 - 2q^8 + 3q^7 + 2q^6$
  - $m_\kappa(\tau) = 6.$
- 

$$\xi = ((2,1),(1,1),(1,1)), \quad \sigma_A = (\epsilon_1, \epsilon_2, \epsilon_3, \epsilon_4), \quad \sigma_B = (\epsilon_1, \epsilon_2, \epsilon_3, \epsilon_1).$$

- $[\mathcal{M}_\tau] = (q^2 - 1)(q - 1).$
  - $[\mathcal{G}_\tau] = (q - 1)^3.$
  - $[\mathfrak{M}_\tau^{\text{irr}}] = q - 2.$
  - $[R(\tau)] = q^{17} - q^{16} - 3q^{15} + 2q^{13} + 4q^{12} + 2q^{11} - 2q^{10} - 3q^9 - 3q^8 + q^7 + 2q^6$
  - $m_\kappa(\tau) = 24.$
- 

$$\xi = ((1,1),(1,1),(2,1)), \quad \sigma_A = (\epsilon_1, \epsilon_2, \epsilon_3, \epsilon_4), \quad \sigma_B = (\epsilon_1, \epsilon_1, \epsilon_2, \epsilon_3).$$

- $[\mathcal{M}_\tau] = q^4 - 1.$
  - $[\mathcal{G}_\tau] = (q - 1)^3.$
  - $[\mathfrak{M}_\tau^{\text{irr}}] = q - 2.$
  - $[R(\tau)] = q^{18} - 2q^{16} - 3q^{15} - 4q^{14} + 4q^{12} + 6q^{11} + 5q^{10} - 2q^8 - 3q^7 - 2q^6$
  - $m_\kappa(\tau) = 6.$
- 

$$\xi = ((1,1),(1,1),(2,1)), \quad \sigma_A = (\epsilon_1, \epsilon_2, \epsilon_3, \epsilon_4), \quad \sigma_B = (\epsilon_1, \epsilon_2, \epsilon_3, \epsilon_1).$$

- $[\mathcal{M}_\tau] = q^3 - 1.$
- $[\mathcal{G}_\tau] = (q - 1)^3.$
- $[\mathfrak{M}_\tau^{\text{irr}}] = q - 2.$
- $[R(\tau)] = q^{17} - 2q^{15} - 4q^{14} - 3q^{13} + 2q^{12} + 5q^{11} + 6q^{10} + 2q^9 - 2q^8 - 3q^7 - 2q^6$
- $m_\kappa(\tau) = 24.$

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$$\xi = ((1,1),(1,1),(1,1),(1,1)), \quad \sigma_A = (\epsilon_1, \epsilon_2, \epsilon_3, \epsilon_4), \quad \sigma_B = (\epsilon_1, \epsilon_1, \epsilon_2, \epsilon_3).$$

- $[\mathcal{M}_\tau] = (q^2 - 1)^2.$
  - $[\mathcal{G}_\tau] = (q - 1)^4.$
  - $[\mathfrak{M}_\tau^{\text{irr}}] = 1.$
  - $[R(\tau)] = q^{16} + 3q^{15} + 3q^{14} - 4q^{12} - 6q^{11} - 4q^{10} + 3q^8 + 3q^7 + q^6$
  - $m_\kappa(\tau) = 12.$
- 

$$\xi = ((1,1),(1,1),(1,1),(1,1)), \quad \sigma_A = (\epsilon_1, \epsilon_2, \epsilon_3, \epsilon_4), \quad \sigma_B = (\epsilon_2, \epsilon_3, \epsilon_1, \epsilon_1).$$

- $[\mathcal{M}_\tau] = (q^2 - 1)^2.$
  - $[\mathcal{G}_\tau] = (q - 1)^4.$
  - $[\mathfrak{M}_\tau^{\text{irr}}] = 1.$
  - $[R(\tau)] = q^{16} + 3q^{15} + 3q^{14} - 4q^{12} - 6q^{11} - 4q^{10} + 3q^8 + 3q^7 + q^6$
  - $m_\kappa(\tau) = 12.$
- 

$$\xi = ((1,1),(1,1),(1,1),(1,1)), \quad \sigma_A = (\epsilon_1, \epsilon_2, \epsilon_3, \epsilon_4), \quad \sigma_B = (\epsilon_1, \epsilon_2, \epsilon_3, \epsilon_1).$$

- $[\mathcal{M}_\tau] = (q^2 - 1)(q - 1).$
  - $[\mathcal{G}_\tau] = (q - 1)^4.$
  - $[\mathfrak{M}_\tau^{\text{irr}}] = 1.$
  - $[R(\tau)] = q^{15} + 2q^{14} + q^{13} - q^{12} - 3q^{11} - 3q^{10} - q^9 + q^8 + 2q^7 + q^6$
  - $m_\kappa(\tau) = 48.$
- 

$$\xi = ((2,1),(1,1),(1,1)), \quad \sigma_A = (\epsilon_1, \epsilon_2, \epsilon_3, \epsilon_4), \quad \sigma_B = (\epsilon_1, \epsilon_2, \epsilon_3, \epsilon_1).$$

- $[\mathcal{M}_\tau] = (q^2 - 1)(q - 1)q.$
  - $[\mathcal{G}_\tau] = (q - 1)^3.$
  - $[\mathfrak{M}_\tau^{\text{irr}}] = q - 2.$
  - $[R(\tau)] = q^{18} - q^{17} - 3q^{16} + 2q^{14} + 4q^{13} + 2q^{12} - 2q^{11} - 3q^{10} - 3q^9 + q^8 + 2q^7$
  - $m_\kappa(\tau) = 24.$
- 

$$\xi = ((2,1),(1,1),(1,1)), \quad \sigma_A = (\epsilon_1, \epsilon_2, \epsilon_3, \epsilon_4), \quad \sigma_B = (\epsilon_2, \epsilon_1, \epsilon_1, \epsilon_3).$$

- $[\mathcal{M}_\tau] = (q - 1)^2 q^2.$
  - $[\mathcal{G}_\tau] = (q - 1)^3.$
  - $[\mathfrak{M}_\tau^{\text{irr}}] = q - 2.$
  - $[R(\tau)] = q^{18} - 2q^{17} - q^{16} + q^{15} + q^{14} + 3q^{13} - q^{12} - q^{11} - 2q^{10} - q^9 + 2q^8$
  - $m_\kappa(\tau) = 24.$
- 

$$\xi = ((1,1),(1,1),(1,1),(1,1)), \quad \sigma_A = (\epsilon_1, \epsilon_2, \epsilon_3, \epsilon_4), \quad \sigma_B = (\epsilon_1, \epsilon_1, \epsilon_2, \epsilon_3).$$

- $[\mathcal{M}_\tau] = (q^2 - 1)(q - 1)q^2.$
- $[\mathcal{G}_\tau] = (q - 1)^4.$
- $[\mathfrak{M}_\tau^{\text{irr}}] = 1.$
- $[R(\tau)] = q^{17} + 2q^{16} + q^{15} - q^{14} - 3q^{13} - 3q^{12} - q^{11} + q^{10} + 2q^9 + q^8$
- $m_\kappa(\tau) = 24.$

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$$\xi = ((1,1),(1,1),(1,1),(1,1)), \quad \sigma_A = (\epsilon_1, \epsilon_2, \epsilon_3, \epsilon_4), \quad \sigma_B = (\epsilon_1, \epsilon_2, \epsilon_3, \epsilon_1).$$

- $[\mathcal{M}_\tau] = (q^2 - 1)(q - 1)q.$
  - $[\mathcal{G}_\tau] = (q - 1)^4.$
  - $[\mathfrak{M}_\tau^{\text{irr}}] = 1.$
  - $[R(\tau)] = q^{16} + 2q^{15} + q^{14} - q^{13} - 3q^{12} - 3q^{11} - q^{10} + q^9 + 2q^8 + q^7$
  - $m_\kappa(\tau) = 48.$
- 

$$\xi = ((1,1),(1,1),(1,1),(1,1)), \quad \sigma_A = (\epsilon_1, \epsilon_2, \epsilon_3, \epsilon_4), \quad \sigma_B = (\epsilon_2, \epsilon_1, \epsilon_1, \epsilon_3).$$

- $[\mathcal{M}_\tau] = (q - 1)^2 q^2.$
  - $[\mathcal{G}_\tau] = (q - 1)^4.$
  - $[\mathfrak{M}_\tau^{\text{irr}}] = 1.$
  - $[R(\tau)] = q^{16} + q^{15} - q^{13} - 2q^{12} - q^{11} + q^9 + q^8$
  - $m_\kappa(\tau) = 48.$
- 

$$\xi = ((1,1),(3,1)), \quad \sigma_A = (\epsilon_1, \epsilon_2, \epsilon_3, \epsilon_4), \quad \sigma_B = (\epsilon_1, \epsilon_1, \epsilon_2, \epsilon_3).$$

- $[\mathcal{M}_\tau] = q^2 - 1.$
  - $[\mathcal{G}_\tau] = (q - 1)^2.$
  - $[\mathfrak{M}_\tau^{\text{irr}}] = q^4 + 4q^3 - 9q^2 - 3q + 12.$
  - $[R(\tau)] = q^{20} + 5q^{19} - 6q^{18} - 18q^{17} + 8q^{16} + 25q^{15} + 14q^{14} - 8q^{13} - 33q^{12} - 21q^{11} + 4q^{10} + 26q^9 + 24q^8 - 9q^7 - 12q^6$
  - $m_\kappa(\tau) = 4.$
- 

$$\xi = ((1,1),(3,1)), \quad \sigma_A = (\epsilon_1, \epsilon_2, \epsilon_3, \epsilon_4), \quad \sigma_B = (\epsilon_2, \epsilon_3, \epsilon_1, \epsilon_1).$$

- $[\mathcal{M}_\tau] = q^3 - 1.$
  - $[\mathcal{G}_\tau] = (q - 1)^2.$
  - $[\mathfrak{M}_\tau^{\text{irr}}] = q^2 - 3q + 3.$
  - $[R(\tau)] = q^{19} - 2q^{18} + q^{16} + 3q^{15} + 2q^{14} - 5q^{13} - 3q^{12} - 4q^{11} + 3q^{10} + 5q^9 + 2q^8 - 3q^6$
  - $m_\kappa(\tau) = 8.$
- 

$$\xi = ((1,1),(2,1),(1,1)), \quad \sigma_A = (\epsilon_1, \epsilon_2, \epsilon_3, \epsilon_4), \quad \sigma_B = (\epsilon_1, \epsilon_1, \epsilon_2, \epsilon_3).$$

- $[\mathcal{M}_\tau] = (q - 1)^2.$
  - $[\mathcal{G}_\tau] = (q - 1)^3.$
  - $[\mathfrak{M}_\tau^{\text{irr}}] = q - 2.$
  - $[R(\tau)] = q^{16} - 2q^{15} - q^{14} + q^{13} + q^{12} + 3q^{11} - q^{10} - q^9 - 2q^8 - q^7 + 2q^6$
  - $m_\kappa(\tau) = 24.$
- 

$$\xi = ((1,1),(2,1),(1,1)), \quad \sigma_A = (\epsilon_1, \epsilon_2, \epsilon_3, \epsilon_4), \quad \sigma_B = (\epsilon_2, \epsilon_3, \epsilon_1, \epsilon_1).$$

- $[\mathcal{M}_\tau] = (q^2 - 1)(q - 1).$
- $[\mathcal{G}_\tau] = (q - 1)^3.$
- $[\mathfrak{M}_\tau^{\text{irr}}] = q - 2.$
- $[R(\tau)] = q^{17} - q^{16} - 3q^{15} + 2q^{13} + 4q^{12} + 2q^{11} - 2q^{10} - 3q^9 - 3q^8 + q^7 + 2q^6$
- $m_\kappa(\tau) = 24.$

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$$\xi = ((1, 1), (1, 1), (1, 1), (1, 1)), \quad \sigma_A = (\epsilon_1, \epsilon_2, \epsilon_3, \epsilon_4), \quad \sigma_B = (\epsilon_2, \epsilon_3, \epsilon_1, \epsilon_1).$$

- $[\mathcal{M}_\tau] = (q - 1)^3$ .
  - $[\mathcal{G}_\tau] = (q - 1)^4$ .
  - $[\mathfrak{M}_\tau^{\text{irr}}] = 1$ .
  - $[R(\tau)] = q^{15} - q^{13} - q^{12} - q^{11} + q^{10} + q^9 + q^8 - q^6$
  - $m_\kappa(\tau) = 24$ .
- 

$$\xi = ((1, 1), (2, 1), (1, 1)), \quad \sigma_A = (\epsilon_1, \epsilon_2, \epsilon_3, \epsilon_4), \quad \sigma_B = (\epsilon_1, \epsilon_1, \epsilon_2, \epsilon_3).$$

- $[\mathcal{M}_\tau] = (q^2 - 1)(q - 1)q$ .
  - $[\mathcal{G}_\tau] = (q - 1)^3$ .
  - $[\mathfrak{M}_\tau^{\text{irr}}] = q - 2$ .
  - $[R(\tau)] = q^{18} - q^{17} - 3q^{16} + 2q^{14} + 4q^{13} + 2q^{12} - 2q^{11} - 3q^{10} - 3q^9 + q^8 + 2q^7$
  - $m_\kappa(\tau) = 24$ .
- 

$$\xi = ((1, 1), (2, 1), (1, 1)), \quad \sigma_A = (\epsilon_1, \epsilon_2, \epsilon_3, \epsilon_4), \quad \sigma_B = (\epsilon_2, \epsilon_3, \epsilon_1, \epsilon_1).$$

- $[\mathcal{M}_\tau] = (q^2 - 1)(q - 1)q$ .
  - $[\mathcal{G}_\tau] = (q - 1)^3$ .
  - $[\mathfrak{M}_\tau^{\text{irr}}] = q - 2$ .
  - $[R(\tau)] = q^{18} - q^{17} - 3q^{16} + 2q^{14} + 4q^{13} + 2q^{12} - 2q^{11} - 3q^{10} - 3q^9 + q^8 + 2q^7$
  - $m_\kappa(\tau) = 24$ .
- 

$$\xi = ((1, 1), (2, 1), (1, 1)), \quad \sigma_A = (\epsilon_1, \epsilon_2, \epsilon_3, \epsilon_4), \quad \sigma_B = (\epsilon_1, \epsilon_2, \epsilon_3, \epsilon_1).$$

- $[\mathcal{M}_\tau] = (q^2 - 1)^2$ .
  - $[\mathcal{G}_\tau] = (q - 1)^3$ .
  - $[\mathfrak{M}_\tau^{\text{irr}}] = q - 2$ .
  - $[R(\tau)] = q^{18} - 4q^{16} - 3q^{15} + 2q^{14} + 6q^{13} + 6q^{12} - 5q^{10} - 6q^9 - 2q^8 + 3q^7 + 2q^6$
  - $m_\kappa(\tau) = 12$ .
- 

$$\xi = ((1, 1), (1, 1), (1, 1), (1, 1)), \quad \sigma_A = (\epsilon_1, \epsilon_2, \epsilon_3, \epsilon_4), \quad \sigma_B = (\epsilon_2, \epsilon_3, \epsilon_1, \epsilon_1).$$

- $[\mathcal{M}_\tau] = (q - 1)^3q$ .
  - $[\mathcal{G}_\tau] = (q - 1)^4$ .
  - $[\mathfrak{M}_\tau^{\text{irr}}] = 1$ .
  - $[R(\tau)] = q^{16} - q^{14} - q^{13} - q^{12} + q^{11} + q^{10} + q^9 - q^7$
  - $m_\kappa(\tau) = 48$ .
- 

$$\xi = ((1, 1), (1, 1), (1, 1), (1, 1)), \quad \sigma_A = (\epsilon_1, \epsilon_2, \epsilon_3, \epsilon_4), \quad \sigma_B = (\epsilon_1, \epsilon_2, \epsilon_3, \epsilon_1).$$

- $[\mathcal{M}_\tau] = (q^2 - 1)(q - 1)^2$ .
- $[\mathcal{G}_\tau] = (q - 1)^4$ .
- $[\mathfrak{M}_\tau^{\text{irr}}] = 1$ .
- $[R(\tau)] = q^{16} + q^{15} - q^{14} - 2q^{13} - 2q^{12} + 2q^{10} + 2q^9 + q^8 - q^7 - q^6$
- $m_\kappa(\tau) = 24$ .

---


$$\xi = ((1,1),(1,1),(1,1),(1,1)), \quad \sigma_A = (\epsilon_1, \epsilon_2, \epsilon_3, \epsilon_4), \quad \sigma_B = (\epsilon_2, \epsilon_1, \epsilon_1, \epsilon_3).$$

- $[\mathcal{M}_\tau] = (q^2 - 1)(q - 1)^2 q.$
  - $[\mathcal{G}_\tau] = (q - 1)^4.$
  - $[\mathfrak{M}_\tau^{\text{irr}}] = 1.$
  - $[R(\tau)] = q^{17} + q^{16} - q^{15} - 2q^{14} - 2q^{13} + 2q^{11} + 2q^{10} + q^9 - q^8 - q^7$
  - $m_\kappa(\tau) = 24.$
- 

$$\xi = ((1,1),(1,1),(2,1)), \quad \sigma_A = (\epsilon_1, \epsilon_2, \epsilon_3, \epsilon_4), \quad \sigma_B = (\epsilon_1, \epsilon_2, \epsilon_3, \epsilon_1).$$

- $[\mathcal{M}_\tau] = (q^2 - 1)(q - 1)q.$
  - $[\mathcal{G}_\tau] = (q - 1)^3.$
  - $[\mathfrak{M}_\tau^{\text{irr}}] = q - 2.$
  - $[R(\tau)] = q^{18} - q^{17} - 3q^{16} + 2q^{14} + 4q^{13} + 2q^{12} - 2q^{11} - 3q^{10} - 3q^9 + q^8 + 2q^7$
  - $m_\kappa(\tau) = 24.$
- 

$$\xi = ((1,1),(1,1),(2,1)), \quad \sigma_A = (\epsilon_1, \epsilon_2, \epsilon_3, \epsilon_4), \quad \sigma_B = (\epsilon_2, \epsilon_1, \epsilon_1, \epsilon_3).$$

- $[\mathcal{M}_\tau] = (q - 1)^2 q^2.$
  - $[\mathcal{G}_\tau] = (q - 1)^3.$
  - $[\mathfrak{M}_\tau^{\text{irr}}] = q - 2.$
  - $[R(\tau)] = q^{18} - 2q^{17} - q^{16} + q^{15} + q^{14} + 3q^{13} - q^{12} - q^{11} - 2q^{10} - q^9 + 2q^8$
  - $m_\kappa(\tau) = 24.$
- 

$$\xi = ((1,1),(1,1),(1,1),(1,1)), \quad \sigma_A = (\epsilon_1, \epsilon_2, \epsilon_3, \epsilon_4), \quad \sigma_B = (\epsilon_2, \epsilon_3, \epsilon_1, \epsilon_1).$$

- $[\mathcal{M}_\tau] = (q - 1)^3 q^2.$
  - $[\mathcal{G}_\tau] = (q - 1)^4.$
  - $[\mathfrak{M}_\tau^{\text{irr}}] = 1.$
  - $[R(\tau)] = q^{17} - q^{15} - q^{14} - q^{13} + q^{12} + q^{11} + q^{10} - q^8$
  - $m_\kappa(\tau) = 24.$
- 

$$\xi = ((1,1),(1,1),(1,1),(1,1)), \quad \sigma_A = (\epsilon_1, \epsilon_2, \epsilon_3, \epsilon_4), \quad \sigma_B = (\epsilon_1, \epsilon_2, \epsilon_3, \epsilon_1).$$

- $[\mathcal{M}_\tau] = (q - 1)^3 q.$
  - $[\mathcal{G}_\tau] = (q - 1)^4.$
  - $[\mathfrak{M}_\tau^{\text{irr}}] = 1.$
  - $[R(\tau)] = q^{16} - q^{14} - q^{13} - q^{12} + q^{11} + q^{10} + q^9 - q^7$
  - $m_\kappa(\tau) = 48.$
- 

$$\xi = ((1,1),(1,1),(1,1),(1,1)), \quad \sigma_A = (\epsilon_1, \epsilon_2, \epsilon_3, \epsilon_4), \quad \sigma_B = (\epsilon_1, \epsilon_2, \epsilon_3, \epsilon_1).$$

- $[\mathcal{M}_\tau] = (q - 1)^3 q^2.$
- $[\mathcal{G}_\tau] = (q - 1)^4.$
- $[\mathfrak{M}_\tau^{\text{irr}}] = 1.$
- $[R(\tau)] = q^{17} - q^{15} - q^{14} - q^{13} + q^{12} + q^{11} + q^{10} - q^8$
- $m_\kappa(\tau) = 48.$

---


$$\xi = ((1,1),(1,1),(1,1),(1,1)), \quad \sigma_A = (\epsilon_1, \epsilon_2, \epsilon_3, \epsilon_4), \quad \sigma_B = (\epsilon_1, \epsilon_3, \epsilon_1, \epsilon_2).$$

- $[\mathcal{M}_\tau] = (q-1)^3 q^2.$
  - $[\mathcal{G}_\tau] = (q-1)^4.$
  - $[\mathfrak{M}_\tau^{\text{irr}}] = 1.$
  - $[R(\tau)] = q^{17} - q^{15} - q^{14} - q^{13} + q^{12} + q^{11} + q^{10} - q^8$
  - $m_\kappa(\tau) = 48.$
- 

$$\xi = ((1,1),(1,1),(1,1),(1,1)), \quad \sigma_A = (\epsilon_1, \epsilon_2, \epsilon_3, \epsilon_4), \quad \sigma_B = (\epsilon_2, \epsilon_1, \epsilon_3, \epsilon_1).$$

- $[\mathcal{M}_\tau] = (q-1)^3 q^2.$
  - $[\mathcal{G}_\tau] = (q-1)^4.$
  - $[\mathfrak{M}_\tau^{\text{irr}}] = 1.$
  - $[R(\tau)] = q^{17} - q^{15} - q^{14} - q^{13} + q^{12} + q^{11} + q^{10} - q^8$
  - $m_\kappa(\tau) = 48.$
- 

**Total count of  $\kappa$**   $= ((\epsilon_1, \epsilon_2, \epsilon_3, \epsilon_4), (\varepsilon_1, \varepsilon_1, \varepsilon_2, \varepsilon_3))$

$$\begin{aligned} [R_\kappa^{\text{red}}] &= 8q^{20} + 68q^{19} + 56q^{18} - 4q^{17} + 2q^{16} + 78q^{15} + 102q^{14} + 46q^{13} - 20q^{12} - \\ &\quad 92q^{11} - 38q^{10} + 30q^9 + 82q^8 + 18q^7 - 48q^6, \\ [R_\kappa^{\text{irr}}] &= q^{22} + 5q^{21} + 6q^{20} - 40q^{19} - 13q^{18} + 57q^{17} + 51q^{16} - 35q^{15} - 74q^{14} - \\ &\quad 32q^{13} + 25q^{12} + 93q^{11} + 38q^{10} - 30q^9 - 82q^8 - 18q^7 + 48q^6, \\ [R_\kappa] &= q^{22} + 5q^{21} + 14q^{20} + 28q^{19} + 43q^{18} + 53q^{17} + 53q^{16} + 43q^{15} + 28q^{14} + \\ &\quad 14q^{13} + 5q^{12} + q^{11}, \\ [\mathfrak{M}_\kappa] &= q^7 + 5q^6 + 7q^5 - 34q^4 + 34q^2 + 18q - 48. \end{aligned}$$

11. CONFIGURATION  $\boldsymbol{\epsilon} = (\epsilon_1, \epsilon_2, \epsilon_3, \epsilon_4)$  AND  $\boldsymbol{\varepsilon} = (\varepsilon_1, \varepsilon_2, \varepsilon_3, \varepsilon_4)$

---

$$\xi = ((3, 1), (1, 1)), \quad \sigma_A = (\epsilon_1, \epsilon_2, \epsilon_3, \epsilon_4), \quad \sigma_B = (\epsilon_1, \epsilon_2, \epsilon_3, \epsilon_4).$$

- $[\mathcal{M}_\tau] = 1.$
  - $[\mathcal{G}_\tau] = (q - 1)^2.$
  - $[\mathfrak{M}_\tau^{\text{irr}}] = q^4 + 4q^3 - 9q^2 - 3q + 12.$
  - $[R(\tau)] = q^{18} + 5q^{17} - 5q^{16} - 13q^{15} + 3q^{14} + 12q^{13} + 17q^{12} + 4q^{11} - 16q^{10} - 17q^9 - 12q^8 + 9q^7 + 12q^6$
  - $m_\kappa(\tau) = 16.$
- 

$$\xi = ((2, 1), (2, 1)), \quad \sigma_A = (\epsilon_1, \epsilon_2, \epsilon_3, \epsilon_4), \quad \sigma_B = (\epsilon_1, \epsilon_2, \epsilon_3, \epsilon_4).$$

- $[\mathcal{M}_\tau] = 1.$
  - $[\mathcal{G}_\tau] = (q - 1)^2.$
  - $[\mathfrak{M}_\tau^{\text{irr}}] = q^2 - 4q + 4.$
  - $[R(\tau)] = q^{16} - 3q^{15} + 3q^{13} + 2q^{12} + 3q^{11} - 4q^{10} - 3q^9 - 3q^8 + 4q^6$
  - $m_\kappa(\tau) = 18.$
- 

$$\xi = ((2, 1), (1, 1), (1, 1)), \quad \sigma_A = (\epsilon_1, \epsilon_2, \epsilon_3, \epsilon_4), \quad \sigma_B = (\epsilon_1, \epsilon_2, \epsilon_3, \epsilon_4).$$

- $[\mathcal{M}_\tau] = 1.$
  - $[\mathcal{G}_\tau] = (q - 1)^3.$
  - $[\mathfrak{M}_\tau^{\text{irr}}] = q - 2.$
  - $[R(\tau)] = q^{14} - 2q^{12} - 3q^{11} - 3q^{10} + 2q^8 + 3q^7 + 2q^6$
  - $m_\kappa(\tau) = 72.$
- 

$$\xi = ((1, 1), (1, 1), (1, 1), (1, 1)), \quad \sigma_A = (\epsilon_1, \epsilon_2, \epsilon_3, \epsilon_4), \quad \sigma_B = (\epsilon_1, \epsilon_2, \epsilon_3, \epsilon_4).$$

- $[\mathcal{M}_\tau] = 1.$
  - $[\mathcal{G}_\tau] = (q - 1)^4.$
  - $[\mathfrak{M}_\tau^{\text{irr}}] = 1.$
  - $[R(\tau)] = q^{12} + 3q^{11} + 5q^{10} + 6q^9 + 5q^8 + 3q^7 + q^6$
  - $m_\kappa(\tau) = 24.$
- 

$$\xi = ((3, 1), (1, 1)), \quad \sigma_A = (\epsilon_1, \epsilon_2, \epsilon_3, \epsilon_4), \quad \sigma_B = (\epsilon_1, \epsilon_2, \epsilon_3, \epsilon_4).$$

- $[\mathcal{M}_\tau] = q^3 - 1.$
  - $[\mathcal{G}_\tau] = (q - 1)^2.$
  - $[\mathfrak{M}_\tau^{\text{irr}}] = q^4 + 4q^3 - 9q^2 - 3q + 12.$
  - $[R(\tau)] = q^{21} + 5q^{20} - 5q^{19} - 14q^{18} - 2q^{17} + 17q^{16} + 30q^{15} + q^{14} - 28q^{13} - 34q^{12} - 16q^{11} + 25q^{10} + 29q^9 + 12q^8 - 9q^7 - 12q^6$
  - $m_\kappa(\tau) = 16.$
- 

$$\xi = ((2, 1), (1, 1), (1, 1)), \quad \sigma_A = (\epsilon_1, \epsilon_2, \epsilon_3, \epsilon_4), \quad \sigma_B = (\epsilon_1, \epsilon_2, \epsilon_3, \epsilon_4).$$

- $[\mathcal{M}_\tau] = q^3 - 1.$
- $[\mathcal{G}_\tau] = (q - 1)^3.$
- $[\mathfrak{M}_\tau^{\text{irr}}] = q - 2.$
- $[R(\tau)] = q^{17} - 2q^{15} - 4q^{14} - 3q^{13} + 2q^{12} + 5q^{11} + 6q^{10} + 2q^9 - 2q^8 - 3q^7 - 2q^6$

- $m_\kappa(\tau) = 144$ .
- 

$$\xi = ((1, 1), (1, 1), (1, 1), (1, 1)), \quad \sigma_A = (\epsilon_1, \epsilon_2, \epsilon_3, \epsilon_4), \quad \sigma_B = (\epsilon_1, \epsilon_2, \epsilon_3, \epsilon_4).$$

- $[\mathcal{M}_\tau] = q^3 - 1$ .
  - $[\mathcal{G}_\tau] = (q - 1)^4$ .
  - $[\mathfrak{M}_\tau^{\text{irr}}] = 1$ .
  - $[R(\tau)] = q^{15} + 3q^{14} + 5q^{13} + 5q^{12} + 2q^{11} - 2q^{10} - 5q^9 - 5q^8 - 3q^7 - q^6$
  - $m_\kappa(\tau) = 96$ .
- 

$$\xi = ((2, 1), (2, 1)), \quad \sigma_A = (\epsilon_1, \epsilon_2, \epsilon_3, \epsilon_4), \quad \sigma_B = (\epsilon_1, \epsilon_2, \epsilon_3, \epsilon_4).$$

- $[\mathcal{M}_\tau] = q^4 - 1$ .
  - $[\mathcal{G}_\tau] = (q - 1)^2$ .
  - $[\mathfrak{M}_\tau^{\text{irr}}] = q^2 - 4q + 4$ .
  - $[R(\tau)] = q^{20} - 3q^{19} + 3q^{17} + q^{16} + 6q^{15} - 4q^{14} - 6q^{13} - 5q^{12} - 3q^{11} + 8q^{10} + 3q^9 + 3q^8 - 4q^6$
  - $m_\kappa(\tau) = 36$ .
- 

$$\xi = ((2, 1), (1, 1), (1, 1)), \quad \sigma_A = (\epsilon_1, \epsilon_2, \epsilon_3, \epsilon_4), \quad \sigma_B = (\epsilon_1, \epsilon_2, \epsilon_3, \epsilon_4).$$

- $[\mathcal{M}_\tau] = (q^2 - 1)^2$ .
  - $[\mathcal{G}_\tau] = (q - 1)^3$ .
  - $[\mathfrak{M}_\tau^{\text{irr}}] = q - 2$ .
  - $[R(\tau)] = q^{18} - 4q^{16} - 3q^{15} + 2q^{14} + 6q^{13} + 6q^{12} - 5q^{10} - 6q^9 - 2q^8 + 3q^7 + 2q^6$
  - $m_\kappa(\tau) = 72$ .
- 

$$\xi = ((1, 1), (1, 1), (2, 1)), \quad \sigma_A = (\epsilon_1, \epsilon_2, \epsilon_3, \epsilon_4), \quad \sigma_B = (\epsilon_1, \epsilon_2, \epsilon_3, \epsilon_4).$$

- $[\mathcal{M}_\tau] = q^4 - 1$ .
  - $[\mathcal{G}_\tau] = (q - 1)^3$ .
  - $[\mathfrak{M}_\tau^{\text{irr}}] = q - 2$ .
  - $[R(\tau)] = q^{18} - 2q^{16} - 3q^{15} - 4q^{14} + 4q^{12} + 6q^{11} + 5q^{10} - 2q^8 - 3q^7 - 2q^6$
  - $m_\kappa(\tau) = 72$ .
- 

$$\xi = ((1, 1), (1, 1), (1, 1), (1, 1)), \quad \sigma_A = (\epsilon_1, \epsilon_2, \epsilon_3, \epsilon_4), \quad \sigma_B = (\epsilon_1, \epsilon_2, \epsilon_3, \epsilon_4).$$

- $[\mathcal{M}_\tau] = (q^2 - 1)^2$ .
  - $[\mathcal{G}_\tau] = (q - 1)^4$ .
  - $[\mathfrak{M}_\tau^{\text{irr}}] = 1$ .
  - $[R(\tau)] = q^{16} + 3q^{15} + 3q^{14} - 4q^{12} - 6q^{11} - 4q^{10} + 3q^8 + 3q^7 + q^6$
  - $m_\kappa(\tau) = 144$ .
- 

$$\xi = ((2, 1), (1, 1), (1, 1)), \quad \sigma_A = (\epsilon_1, \epsilon_2, \epsilon_3, \epsilon_4), \quad \sigma_B = (\epsilon_1, \epsilon_2, \epsilon_3, \epsilon_4).$$

- $[\mathcal{M}_\tau] = (q^2 - 1)(q - 1)q^2$ .
- $[\mathcal{G}_\tau] = (q - 1)^3$ .
- $[\mathfrak{M}_\tau^{\text{irr}}] = q - 2$ .
- $[R(\tau)] = q^{19} - q^{18} - 3q^{17} + 2q^{15} + 4q^{14} + 2q^{13} - 2q^{12} - 3q^{11} - 3q^{10} + q^9 + 2q^8$
- $m_\kappa(\tau) = 144$ .

---


$$\xi = ((1,1),(1,1),(1,1),(1,1)), \quad \sigma_A = (\epsilon_1, \epsilon_2, \epsilon_3, \epsilon_4), \quad \sigma_B = (\epsilon_1, \epsilon_2, \epsilon_3, \epsilon_4).$$

- $[\mathcal{M}_\tau] = (q^2 - 1)(q - 1)q^2.$
  - $[\mathcal{G}_\tau] = (q - 1)^4.$
  - $[\mathfrak{M}_\tau^{\text{irr}}] = 1.$
  - $[R(\tau)] = q^{17} + 2q^{16} + q^{15} - q^{14} - 3q^{13} - 3q^{12} - q^{11} + q^{10} + 2q^9 + q^8$
  - $m_\kappa(\tau) = 288.$
- 

$$\xi = ((1,1),(3,1)), \quad \sigma_A = (\epsilon_1, \epsilon_2, \epsilon_3, \epsilon_4), \quad \sigma_B = (\epsilon_1, \epsilon_2, \epsilon_3, \epsilon_4).$$

- $[\mathcal{M}_\tau] = q^3 - 1.$
  - $[\mathcal{G}_\tau] = (q - 1)^2.$
  - $[\mathfrak{M}_\tau^{\text{irr}}] = q^4 + 4q^3 - 9q^2 - 3q + 12.$
  - $[R(\tau)] = q^{21} + 5q^{20} - 5q^{19} - 14q^{18} - 2q^{17} + 17q^{16} + 30q^{15} + q^{14} - 28q^{13} - 34q^{12} - 16q^{11} + 25q^{10} + 29q^9 + 12q^8 - 9q^7 - 12q^6$
  - $m_\kappa(\tau) = 16.$
- 

$$\xi = ((1,1),(2,1),(1,1)), \quad \sigma_A = (\epsilon_1, \epsilon_2, \epsilon_3, \epsilon_4), \quad \sigma_B = (\epsilon_1, \epsilon_2, \epsilon_3, \epsilon_4).$$

- $[\mathcal{M}_\tau] = (q^2 - 1)(q - 1).$
  - $[\mathcal{G}_\tau] = (q - 1)^3.$
  - $[\mathfrak{M}_\tau^{\text{irr}}] = q - 2.$
  - $[R(\tau)] = q^{17} - q^{16} - 3q^{15} + 2q^{13} + 4q^{12} + 2q^{11} - 2q^{10} - 3q^9 - 3q^8 + q^7 + 2q^6$
  - $m_\kappa(\tau) = 144.$
- 

$$\xi = ((1,1),(1,1),(1,1),(1,1)), \quad \sigma_A = (\epsilon_1, \epsilon_2, \epsilon_3, \epsilon_4), \quad \sigma_B = (\epsilon_1, \epsilon_2, \epsilon_3, \epsilon_4).$$

- $[\mathcal{M}_\tau] = (q - 1)^3.$
  - $[\mathcal{G}_\tau] = (q - 1)^4.$
  - $[\mathfrak{M}_\tau^{\text{irr}}] = 1.$
  - $[R(\tau)] = q^{15} - q^{13} - q^{12} - q^{11} + q^{10} + q^9 + q^8 - q^6$
  - $m_\kappa(\tau) = 96.$
- 

$$\xi = ((1,1),(2,1),(1,1)), \quad \sigma_A = (\epsilon_1, \epsilon_2, \epsilon_3, \epsilon_4), \quad \sigma_B = (\epsilon_1, \epsilon_2, \epsilon_3, \epsilon_4).$$

- $[\mathcal{M}_\tau] = (q^2 - 1)^2q.$
  - $[\mathcal{G}_\tau] = (q - 1)^3.$
  - $[\mathfrak{M}_\tau^{\text{irr}}] = q - 2.$
  - $[R(\tau)] = q^{19} - 4q^{17} - 3q^{16} + 2q^{15} + 6q^{14} + 6q^{13} - 5q^{11} - 6q^{10} - 2q^9 + 3q^8 + 2q^7$
  - $m_\kappa(\tau) = 144.$
- 

$$\xi = ((1,1),(1,1),(1,1),(1,1)), \quad \sigma_A = (\epsilon_1, \epsilon_2, \epsilon_3, \epsilon_4), \quad \sigma_B = (\epsilon_1, \epsilon_2, \epsilon_3, \epsilon_4).$$

- $[\mathcal{M}_\tau] = (q^2 - 1)(q - 1)^2q.$
- $[\mathcal{G}_\tau] = (q - 1)^4.$
- $[\mathfrak{M}_\tau^{\text{irr}}] = 1.$
- $[R(\tau)] = q^{17} + q^{16} - q^{15} - 2q^{14} - 2q^{13} + 2q^{11} + 2q^{10} + q^9 - q^8 - q^7$
- $m_\kappa(\tau) = 288.$

- 
- $\xi = ((1,1),(1,1),(2,1)), \quad \sigma_A = (\epsilon_1, \epsilon_2, \epsilon_3, \epsilon_4), \quad \sigma_B = (\epsilon_1, \epsilon_2, \epsilon_3, \epsilon_4).$
- $[\mathcal{M}_\tau] = (q^2 - 1)(q - 1)q^2.$
  - $[\mathcal{G}_\tau] = (q - 1)^3.$
  - $[\mathfrak{M}_\tau^{\text{irr}}] = q - 2.$
  - $[R(\tau)] = q^{19} - q^{18} - 3q^{17} + 2q^{15} + 4q^{14} + 2q^{13} - 2q^{12} - 3q^{11} - 3q^{10} + q^9 + 2q^8$
  - $m_\kappa(\tau) = 144.$
- 

- $\xi = ((1,1),(1,1),(1,1),(1,1)), \quad \sigma_A = (\epsilon_1, \epsilon_2, \epsilon_3, \epsilon_4), \quad \sigma_B = (\epsilon_1, \epsilon_2, \epsilon_3, \epsilon_4).$
- $[\mathcal{M}_\tau] = (q - 1)^3q^2.$
  - $[\mathcal{G}_\tau] = (q - 1)^4.$
  - $[\mathfrak{M}_\tau^{\text{irr}}] = 1.$
  - $[R(\tau)] = q^{17} - q^{15} - q^{14} - q^{13} + q^{12} + q^{11} + q^{10} - q^8$
  - $m_\kappa(\tau) = 288.$
- 

- $\xi = ((1,1),(1,1),(1,1),(1,1)), \quad \sigma_A = (\epsilon_1, \epsilon_2, \epsilon_3, \epsilon_4), \quad \sigma_B = (\epsilon_1, \epsilon_2, \epsilon_3, \epsilon_4).$
- $[\mathcal{M}_\tau] = (q - 1)^3q^3.$
  - $[\mathcal{G}_\tau] = (q - 1)^4.$
  - $[\mathfrak{M}_\tau^{\text{irr}}] = 1.$
  - $[R(\tau)] = q^{18} - q^{16} - q^{15} - q^{14} + q^{13} + q^{12} + q^{11} - q^9$
  - $m_\kappa(\tau) = 576.$
- 

**Total count of  $\kappa = ((\epsilon_1, \epsilon_2, \epsilon_3, \epsilon_4), (\varepsilon_1, \varepsilon_2, \varepsilon_3, \varepsilon_4))$**

$$\begin{aligned}
 [R_\kappa^{\text{red}}] &= 32q^{21} + 196q^{20} + 164q^{19} - 164q^{17} - 58q^{16} + 386q^{15} + 296q^{14} + 94q^{13} - \\
 &\quad 264q^{12} - 406q^{11} - 8q^{10} + 182q^9 + 270q^8 - 144q^6, \\
 [R_\kappa^{\text{irr}}] &= q^{24} + 6q^{23} + 19q^{22} + 10q^{21} - 125q^{20} - 68q^{19} + 106q^{18} + 260q^{17} + 129q^{16} - \\
 &\quad 344q^{15} - 277q^{14} - 88q^{13} + 265q^{12} + 406q^{11} + 8q^{10} - 182q^9 - 270q^8 + 144q^6, \\
 [R_\kappa] &= q^{24} + 6q^{23} + 19q^{22} + 42q^{21} + 71q^{20} + 96q^{19} + 106q^{18} + 96q^{17} + 71q^{16} + \\
 &\quad 42q^{15} + 19q^{14} + 6q^{13} + q^{12}, \\
 [\mathfrak{M}_\kappa] &= q^9 + 6q^8 + 20q^7 + 17q^6 - 98q^5 - 26q^4 + 38q^3 + 126q^2 - 144.
 \end{aligned}$$

## SUMMARY

$$\begin{aligned}
[R_{(\epsilon_1, \epsilon_1, \epsilon_1, \epsilon_2), (\epsilon_1, \epsilon_2, \epsilon_3, \epsilon_4)}^{\text{irr}}] &= q^{18} - 4q^{17} + 5q^{16} - q^{15} - 3q^{14} + 3q^{13} - 5q^{12} + 7q^{11} - \\
&\quad 2q^{10} + q^9 - 6q^7 + 4q^6. \\
[R_{(\epsilon_1, \epsilon_1, \epsilon_2, \epsilon_2), (\epsilon_1, \epsilon_1, \epsilon_2, \epsilon_2)}^{\text{irr}}] &= 0. \\
[R_{(\epsilon_1, \epsilon_1, \epsilon_2, \epsilon_2), (\epsilon_1, \epsilon_1, \epsilon_2, \epsilon_3)}^{\text{irr}}] &= q^{18} - 3q^{17} + 4q^{16} - 2q^{15} - 3q^{14} + 3q^{13} - 3q^{12} + 7q^{11} - \\
&\quad 2q^{10} - q^8 - 5q^7 + 4q^6. \\
[R_{(\epsilon_1, \epsilon_1, \epsilon_2, \epsilon_2), (\epsilon_1, \epsilon_2, \epsilon_3, \epsilon_4)}^{\text{irr}}] &= q^{20} + 4q^{19} - 12q^{18} - 4q^{17} + 24q^{16} - 11q^{15} - 3q^{14} - \\
&\quad 7q^{13} - 6q^{12} + 25q^{11} - 3q^{10} + 11q^9 - 19q^8 - 18q^7 + 18q^6. \\
[R_{(\epsilon_1, \epsilon_1, \epsilon_2, \epsilon_3), (\epsilon_1, \epsilon_1, \epsilon_2, \epsilon_2)}^{\text{irr}}] &= q^{18} - 3q^{17} + 4q^{16} - 2q^{15} - 3q^{14} + 3q^{13} - 3q^{12} + 7q^{11} - \\
&\quad 2q^{10} - q^8 - 5q^7 + 4q^6. \\
[R_{(\epsilon_1, \epsilon_1, \epsilon_2, \epsilon_3), (\epsilon_1, \epsilon_1, \epsilon_2, \epsilon_3)}^{\text{irr}}] &= q^{20} + 2q^{19} - 11q^{18} + 4q^{17} + 17q^{16} - 13q^{15} - 4q^{14} - \\
&\quad 9q^{13} + 4q^{12} + 21q^{11} + 5q^9 - 22q^8 - 10q^7 + 15q^6. \\
[R_{(\epsilon_1, \epsilon_1, \epsilon_2, \epsilon_3), (\epsilon_1, \epsilon_2, \epsilon_3, \epsilon_4)}^{\text{irr}}] &= q^{22} + 5q^{21} + 6q^{20} - 40q^{19} - 13q^{18} + 57q^{17} + 51q^{16} - \\
&\quad 35q^{15} - 74q^{14} - 32q^{13} + 25q^{12} + 93q^{11} + 38q^{10} - 30q^9 - 82q^8 - 18q^7 + 48q^6. \\
[R_{(\epsilon_1, \epsilon_2, \epsilon_3, \epsilon_4), (\epsilon_1, \epsilon_1, \epsilon_1, \epsilon_2)}^{\text{irr}}] &= q^{18} - 4q^{17} + 5q^{16} - q^{15} - 3q^{14} + 3q^{13} - 5q^{12} + 7q^{11} - \\
&\quad 2q^{10} + q^9 - 6q^7 + 4q^6. \\
[R_{(\epsilon_1, \epsilon_2, \epsilon_3, \epsilon_4), (\epsilon_1, \epsilon_1, \epsilon_2, \epsilon_2)}^{\text{irr}}] &= q^{20} + 4q^{19} - 12q^{18} - 4q^{17} + 24q^{16} - 11q^{15} - 3q^{14} - \\
&\quad 7q^{13} - 6q^{12} + 25q^{11} - 3q^{10} + 11q^9 - 19q^8 - 18q^7 + 18q^6. \\
[R_{(\epsilon_1, \epsilon_2, \epsilon_3, \epsilon_4), (\epsilon_1, \epsilon_1, \epsilon_2, \epsilon_3)}^{\text{irr}}] &= q^{22} + 5q^{21} + 6q^{20} - 40q^{19} - 13q^{18} + 57q^{17} + 51q^{16} - \\
&\quad 35q^{15} - 74q^{14} - 32q^{13} + 25q^{12} + 93q^{11} + 38q^{10} - 30q^9 - 82q^8 - 18q^7 + 48q^6. \\
[R_{(\epsilon_1, \epsilon_2, \epsilon_3, \epsilon_4), (\epsilon_1, \epsilon_2, \epsilon_3, \epsilon_4)}^{\text{irr}}] &= q^{24} + 6q^{23} + 19q^{22} + 10q^{21} - 125q^{20} - 68q^{19} + 106q^{18} + \\
&\quad 260q^{17} + 129q^{16} - 344q^{15} - 277q^{14} - 88q^{13} + 265q^{12} + 406q^{11} + 8q^{10} - 182q^9 - 270q^8 + 144q^6)C_{(1,1,1,1),(1,1,1,2)} + (q^{18} - 3q^{17} + 4q^{16} - 2q^{15} - 3q^{14} + \\
&\quad 3q^{13} - 3q^{12} + 7q^{11} - 2q^{10} - q^8 - 5q^7 + 4q^6)C_{(2,2),(1,1,2)} + (q^{18} - 3q^{17} + 4q^{16} - 2q^{15} - 3q^{14} + \\
&\quad 2q^{13} - 3q^{12} - 3q^{11} - 2q^{10} - q^8 - 5q^7 + 4q^6)C_{(1,1,2),(2,2)} + (q^{20} + 4q^{19} - 12q^{18} - 4q^{17} + 24q^{16} - 11q^{15} - 3q^{14} - 7q^{13} - 6q^{12} + 25q^{11} - 3q^{10} + 11q^9 - \\
&\quad 19q^8 - 18q^7 + 18q^6)C_{(2,2),(1,1,1,1)} + (q^{18} - 4q^{17} + 5q^{16} - q^{15} - 3q^{14} + 3q^{13} - 5q^{12} + 7q^{11} - 2q^{10} + q^9 - 6q^7 + 4q^6)C_{(1,3),(1,1,1,1)} + (q^{20} + 2q^{19} - 11q^{18} + 4q^{17} + 17q^{16} - \\
&\quad 13q^{15} - 4q^{14} - 9q^{13} + 4q^{12} + 21q^{11} + 5q^9 - 22q^8 - 10q^7 + 15q^6)C_{(1,1,2),(1,1,2)}.
\end{aligned}$$

## Final result representations.

$$\begin{aligned}
[R_4^{\text{irr}}] &= (q^{20} + 4q^{19} - 12q^{18} - 4q^{17} + 24q^{16} - 11q^{15} - 3q^{14} - 7q^{13} - 6q^{12} + \\
&\quad 25q^{11} - 3q^{10} + 11q^9 - 19q^8 - 18q^7 + 18q^6)C_{(1,1,1,1),(2,2)} + (q^{18} - 4q^{17} + 5q^{16} - \\
&\quad q^{15} - 3q^{14} + 3q^{13} - 5q^{12} + 7q^{11} - 2q^{10} + q^9 - 6q^7 + 4q^6)C_{(1,1,1,1),(1,3)} + (q^{22} + \\
&\quad 5q^{21} + 6q^{20} - 40q^{19} - 13q^{18} + 57q^{17} + 51q^{16} - 35q^{15} - 74q^{14} - 32q^{13} + 25q^{12} + \\
&\quad 93q^{11} + 38q^{10} - 30q^9 - 82q^8 - 18q^7 + 48q^6)C_{(1,1,2),(1,1,1,1)} + (q^{22} + 5q^{21} + 6q^{20} - \\
&\quad 40q^{19} - 13q^{18} + 57q^{17} + 51q^{16} - 35q^{15} - 74q^{14} - 32q^{13} + 25q^{12} + 93q^{11} + 38q^{10} - \\
&\quad 30q^9 - 82q^8 - 18q^7 + 48q^6)C_{(1,1,1,1),(1,1,2)} + (q^{24} + 6q^{23} + 19q^{22} + 10q^{21} - 125q^{20} - \\
&\quad 68q^{19} + 106q^{18} + 260q^{17} + 129q^{16} - 344q^{15} - 277q^{14} - 88q^{13} + 265q^{12} + 406q^{11} + \\
&\quad 8q^{10} - 182q^9 - 270q^8 + 144q^6)C_{(1,1,1,1),(1,1,1,1)} + (q^{18} - 3q^{17} + 4q^{16} - 2q^{15} - 3q^{14} + \\
&\quad 3q^{13} - 3q^{12} + 7q^{11} - 2q^{10} - q^8 - 5q^7 + 4q^6)C_{(2,2),(1,1,2)} + (q^{18} - 3q^{17} + 4q^{16} - \\
&\quad 2q^{15} - 3q^{14} + 3q^{13} - 3q^{12} + 7q^{11} - 2q^{10} - q^8 - 5q^7 + 4q^6)C_{(1,1,2),(2,2)} + (q^{20} + \\
&\quad 4q^{19} - 12q^{18} - 4q^{17} + 24q^{16} - 11q^{15} - 3q^{14} - 7q^{13} - 6q^{12} + 25q^{11} - 3q^{10} + 11q^9 - \\
&\quad 19q^8 - 18q^7 + 18q^6)C_{(2,2),(1,1,1,1)} + (q^{18} - 4q^{17} + 5q^{16} - q^{15} - 3q^{14} + 3q^{13} - 5q^{12} + \\
&\quad 7q^{11} - 2q^{10} + q^9 - 6q^7 + 4q^6)C_{(1,3),(1,1,1,1)} + (q^{20} + 2q^{19} - 11q^{18} + 4q^{17} + 17q^{16} - \\
&\quad 13q^{15} - 4q^{14} - 9q^{13} + 4q^{12} + 21q^{11} + 5q^9 - 22q^8 - 10q^7 + 15q^6)C_{(1,1,2),(1,1,2)}.
\end{aligned}$$

## Final result characters.

$$\begin{aligned}
[\mathfrak{M}_4^{\text{irr}}] &= (q^5 + 4q^4 - 11q^3 + q^2 + 18q - 18)C_{(1,1,1,1),(2,2)} + (q^3 - 4q^2 + 6q - \\
&\quad 4)C_{(1,1,1,1),(1,3)} + (q^7 + 5q^6 + 7q^5 - 34q^4 + 34q^2 + 18q - 48)C_{(1,1,2),(1,1,1,1)} + (q^7 + \\
&\quad 5q^6 + 7q^5 - 34q^4 + 34q^2 + 18q - 48)C_{(1,1,1,1),(1,1,2)} + (q^9 + 6q^8 + 20q^7 + 17q^6 - \\
&\quad 98q^5 - 26q^4 + 38q^3 + 126q^2 - 144)C_{(1,1,1,1),(1,1,1,1)} + (q^3 - 3q^2 + 5q - 4)C_{(2,2),(1,1,2)} + \\
&\quad (q^3 - 3q^2 + 5q - 4)C_{(1,1,2),(2,2)} + (q^5 + 4q^4 - 11q^3 + q^2 + 18q - 18)C_{(2,2),(1,1,1,1)} + \\
&\quad (q^3 - 4q^2 + 6q - 4)C_{(1,3),(1,1,1,1)} + (q^5 + 2q^4 - 10q^3 + 7q^2 + 10q - 15)C_{(1,1,2),(1,1,2)}.
\end{aligned}$$

## REFERENCES

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