

# Seminario de Geometría y Topología



## Scale Structures and $C^*$ -algebras

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### Resumen:

The purpose of this talk is to investigate the duality between large scale and small scale. It is done by creating a connection between  $C^*$ -algebras and scale structures. In the commutative case we consider  $C^*$ -subalgebras of  $C^b(X)$ , the  $C^*$ -algebra of bounded complex-valued functions on  $X$ . Namely, each  $C^*$ -subalgebra  $\mathscr{C}$  of  $C^b(X)$  induces both a small scale structure on  $X$  and a large scale structure on  $X$ . The small scale structure induced on  $X$  corresponds (or is analogous) to the restriction of  $C^b(h(X))$  to  $X$ , where  $h(X)$  is the Higson compactification of  $X$ . The large scale structure induced on  $X$  is a generalization of the  $C_0$ -coarse structure of N.Wright. Conversely, each small scale structure on  $X$  induces a  $C^*$ -subalgebra of  $C^b(X)$  and each large scale structure on  $X$  induces a  $C^*$ -subalgebra of  $C^b(X)$ . To accomplish the full correspondence between scale structures on  $X$  and  $C^*$ -subalgebras of  $C^b(X)$  we need to enhance the scale structures to what we call hybrid structures. In the noncommutative case we consider  $C^*$ -subalgebras of bounded operators  $B(l_2(X))$ .

Joint work with Kyle Austin and Michael Holloway.

**Lugar:** Universidad Complutense de Madrid  
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