

# *¿Qué podemos aprender de los datos acerca de las relaciones económicas?*

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Mayo 2013

## *Esquema*

1. Deficiencias en la aplicación de métodos estadísticos en Economía
  2. Significación estadística y precisión
  3. Significación estadística y capacidad explicativa/contenido informativo
  4. ¿Dónde está la función de potencia?
  5. Interpretación de coeficientes individuales en regresiones múltiples: colinealidad, sesgo de variables omitidas
  6. Tratamiento de la colinealidad
  7. Sugerencias
    - Evitar un excesivo resumen de la información muestral
    - Enfoque alternativo para el contraste de hipótesis conceptuales
    - Cómo evaluar contenido informativo
    - Evaluar restricciones mediante su efecto sobre la cuestión objeto de análisis
- 
- Comentarios aplicables a modelos y métodos sofisticados
  - Implicaciones para el modo en que enseñamos Estadística y Econometría

# 1. Deficiencias debido a la aplicación mecánica de métodos estadísticos en Economía

- Tratándose de una ciencia no experimental
  - Una única muestra (relevancia de la ausencia de sesgo?)
  - Colinealidad (diseño no experimental)
  - Variabilidad paramétrica
- Excesivo resumen de la información muestral en unos pocos estadísticos, a pesar de lo cual, a menudo se leen conclusiones excesivamente enfáticas:
  - “we have *shown* that...”
  - “we have obtained *conclusive evidence* on the relevance of variable X to explain the behavior of variable Y ...”
- Pretensión: pronunciarnos sobre la verdad o falsedad de una teoría, en vez de corroborar si los datos son consistentes con una determinada teoría: *falsacionismo* vs. *corroboración*.
- Insistencia en contrastación de hipótesis paramétricas
- No encontrar evidencia en contra de la hipótesis nula suele interpretarse como haber probado que dicha hipótesis es cierta.

## 2. Significación estadística y precisión

### **Algunas aparentes paradojas :**

El BCE quiere reducir la inflación un punto porcentual elevando los tipos de interés ¿en cuánto debe hacerlo? ¿basta un alza de 100 puntos básicos o debe ser una elevación superior?

Modelo:  $\pi_t = \alpha + \beta r_t + u_t$

H0:  $\beta=1$  versus: H1:  $\beta<1$

- **Paradoja 1:** Estimación:  $\beta = .65$  (.25)      No rechazamos H0
- **Paradoja 2:** Estimación:  $\beta = .95$  (.01)      Rechazamos H0
- **Paradoja 3:** Estimación:  $\beta = 1.45$  (.10)      No rechazamos H0
  
- **Paradoja 4:**  $volatility_t = 0.487 + 3.275 inflation_t + u_t$   
 $p - value = 0.24$

## 2. Significación estadística y precisión

- Un estadístico  $t$  es el producto de:
    - Grado de incumplimiento muestral de  $H_0$
    - Precisión en la estimación
- $$t = \frac{\hat{\beta} - \beta_0}{DT(\hat{\beta})} = \frac{\hat{\beta} - \beta_0}{\sqrt{\sigma_u^2 / \sum_1^n (x_i - \bar{x})^2}}$$
- En la significación estadística de un coeficiente, la precisión en la estimación juega un papel fundamental
  - Un estadístico  $t$  puede ser reducido porque:
    - ✓  $H_0$  se cumple, aproximadamente, en los datos  $\Rightarrow$  no hay problema, pero examinemos la función de potencia
    - ✓ O porque los coeficientes involucrados en la hipótesis se estiman con precisión reducida (incluso si la hipótesis no se satisface)
  - Un estadístico  $t$  puede ser elevado incluso si el grado de incumplimiento muestral de  $H_0$  es muy reducido
  - Abuso del estadístico  $t$ -Student

### Precisión y $t$ -Student

|           |          | Grado de incumplimiento de $H_0$ |                                 |
|-----------|----------|----------------------------------|---------------------------------|
|           |          | Alto                             | Bajo                            |
| Precisión | Elevada  | Rechazar $H_0$<br>t elevado      | ?<br>t?                         |
|           | Reducida | ?<br>t?                          | No rechazar $H_0$<br>t reducido |

## Paradojas ?

- **Paradoja 1:** Estimación:  $\beta = .65$  (.25)      No rechazamos H0 (!!!) [reducida precisión]
  - *Cuestión clave: Relación entre precisión en la estimación y potencia en el contraste*
  - *No deberíamos contrastar*
- **Paradoja 2:** Estimación:  $\beta = .95$  (.01)      Rechazamos H0 [“excesiva” precisión?]
- **Paradoja 3:** Estimación:  $\beta = 1.45$  (.10)
  - No rechazamos H0 (!!!) [Solo se cumple una de las 2 condiciones precisas para rechazar]
  - *No tiene sentido contrastar*

## Testing the Expectations Hypothesis of the term structure of interest rates: Error tipo II

### *Future spot interest rate projected on lagged forward rate*

Model:  $r_t^3 = \alpha + \beta f_{t-3}^{3,6} + u_t$ ,  $f_t^{3,6} = 2r_t^6 - r_t^3$

H0:  $\beta=1$  versus: H1:  $\beta<1$

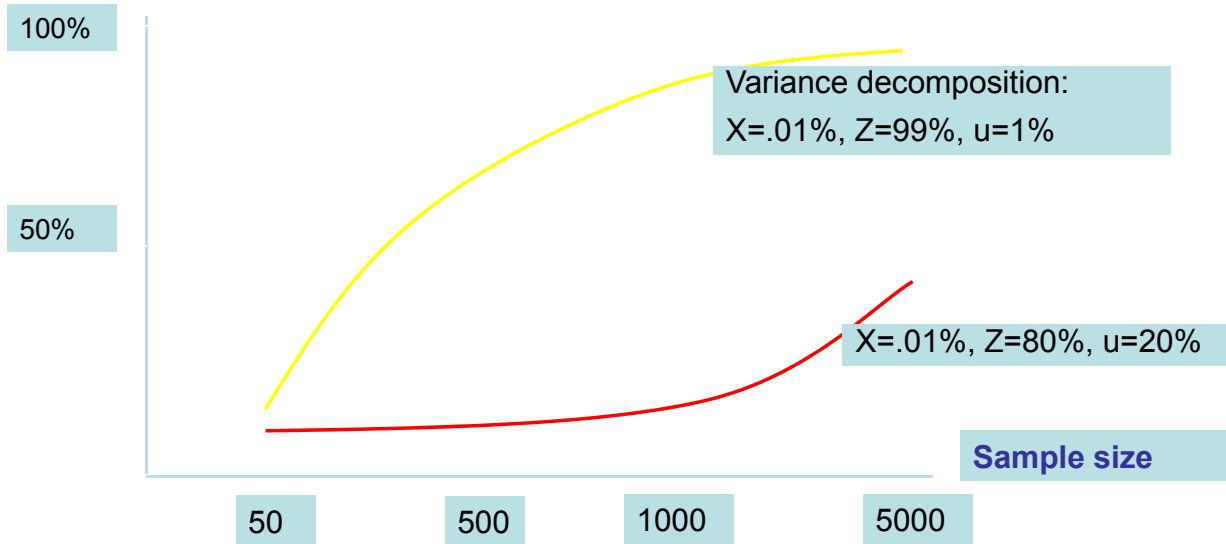
| Maturity | Beta | Standard dev. | R2   | t stat<br>H0: Beta = 1 |
|----------|------|---------------|------|------------------------|
| 1 month  | 0,96 | 0,04          | 0,54 | -1,00                  |
| 3 months | 0,93 | 0,06          | 0,42 | -1,17                  |
| 6 months | 1,10 | 0,15          | 0,32 | 0,67                   |
| 1 year   | 1,40 | 0,24          | 0,22 | 1,67                   |
| 3 years  | 1,63 | 0,47          | 0,15 | 1,34                   |
| 5 years  | 2,40 | 0,85          | 0,04 | 1,65                   |

# Test size and sample size: Error tipo I

- Simulation experiment

$$y = \beta_1 x + \beta_2 z + u, \text{Corr}(x, z) = \text{Corr}(x, u) = \text{Corr}(z, u) = 0$$

- How the frequency of rejection of  $H_0: \beta_x = 0$  changes with T



### 3. Una lamentable confusión: significación estadística versus capacidad explicativa o contenido informativo

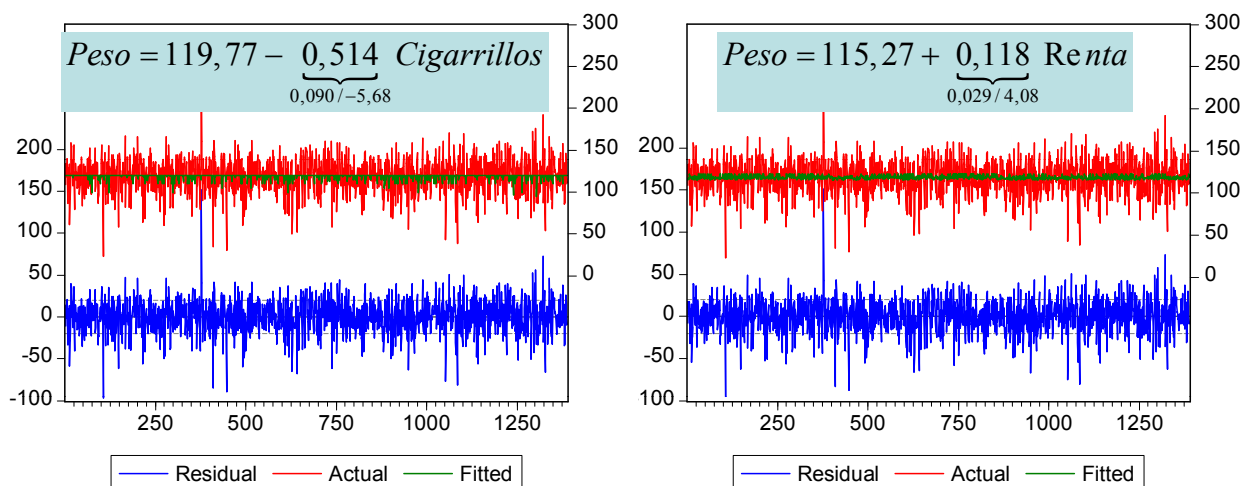
#### Consecuencias de una confusión

- Errónea identificación de dos conceptos: significación estadística de un coeficiente y capacidad explicativa o contenido informativo de la variable asociada
- El concepto de variable significativa no existe
- Abuso del estadístico t-Student
- Leading to serious fallacies and misinterpretations of estimation results
  - ✓ Qualitatively: X explains Y iff its associated coefficient is statistically different from zero
  - ✓ Quantitatively: explanatory power  $\Leftrightarrow$  high absolute value of Student's  $t$
  - ✓ Sign econometrics
  - ✓ Asterisk econometrics
- Inappropriately comparing *relative* explanatory power
  - ✓ Comparing estimated coefficients: *The more important variable to explain Y is Z.*
  - ✓ Comparing values of  $t$  - statistics for different variables: *The more significant variable in the estimated model is Z*
  - ✓ Or for the same variable between different subsamples: *Variable X has become more significant after 1998*

It is relatively easy to find evidence contrary to  $H_0$ : lack of statistical significance of  $\beta$  with a large sample even though the associated variable has little information content. **Type I error (?)**.

$$t = \frac{\hat{\beta} - \beta_0}{DT(\hat{\beta})} = \frac{\hat{\beta} - \beta_0}{\sqrt{\sigma_u^2 / \sum_1^n (x_i - \bar{x})^2}}$$

Example (Wooldridge 2003): Explain child birth weight in terms of: cigarettes smoked by the mother per day during pregnancy, family income, education of father and mother, birth order of the child among siblings.



Dependent Variable: PESO  
Sample: 1 1388 IF EDUCM <> NA AND EDUCM <> NA  
Included observations: 1191

| Variable | Coefficient | Std. Error | t-Statistic | Prob. |
|----------|-------------|------------|-------------|-------|
| C        | 114.5       | 3.728      | 30.71       | 0.00  |
| CIGS     | -0.595      | 0.110      | -5.40       | 0.00  |
| EDUCP    | 0.472       | 0.282      | 1.67        | 0.09  |
| EDUCM    | -0.370      | 0.319      | -1.15       | 0.24  |
| FAMINC   | 0.056       | 0.036      | 1.53        | 0.12  |
| ORDENAC  | 1.787       | 0.659      | 2.71        | 0.00  |

R-squared 0.038 Mean dependent var 119.5  
Adjusted R-squared 0.034 S.D. dependent var 20.14  
S.E. of regression 19.78 Akaike info criterion 8.813

**EDUCP: father's education level**  
**EDUCM: mother's education**  
**CIGS: cigarettes/day smoked by mother**  
**FAMINC: family income**  
**ORDENAC: order among siblings**

**Sample: 1388**

**Smokers among mothers : 212 (15,2%)**

Dependent Variable: PESO  
Sample: 1 1388 IF EDUCM <> NA AND EDUCP <> NA  
Included observations: 1191

| Variable | Coefficient | Std. Error | t-Statistic | Prob. |
|----------|-------------|------------|-------------|-------|
| C        | 117.8       | 1.21       | 96.98       | 0.00  |
| CIGS     | -0.632      | 0.107      | -5.87       | 0.00  |
| ORDENAC  | 1.763       | 0.657      | 2.68        | 0.00  |

R-squared 0.032 Mean dependent var 119.52  
Adjusted R-squared 0.031 S.D. dependent var 20.14  
S.E. of regression 19.82 Akaike info criterion 8.81

Dependent Variable: PESO  
 Sample: 1 1388  
 Included observations: 1191  
 Excluded observations: 197

| Variable           | Coefficient | Std. Error            | t-Statistic | Prob.  |
|--------------------|-------------|-----------------------|-------------|--------|
| C                  | 109.0       | 3.937                 | 27.68       | 0.00   |
| CIGS               | -0.598      | 0.109                 | -5.450      | 0.00   |
| ORDENAC            | 1.915       | 0.655                 | 2.923       | 0.00   |
| RENTA              | 0.043       | 0.036                 | 1.183       | 0.23   |
| EDUCM              | -0.328      | 0.317                 | -1.033      | 0.30   |
| EDUCP              | 0.411       | 0.281                 | 1.463       | 0.14   |
| MALE               | 3.795       | 1.142                 | 3.321       | 0.00   |
| WHITE              | 4.713       | 1.607                 | 2.931       | 0.00   |
| R-squared          | 0.054       | Mean dependent var    |             | 119.52 |
| Adjusted R-squared | 0.048       | S.D. dependent var    |             | 20.141 |
| S.E. of regression | 19.64       | Akaike info criterion |             | 8.800  |

**F-statistic: 9.67 , p-value=0**

Dependent Variable: PESO  
 Sample: 1 1388 IF EDUCM<>NA AND EDUCP<>NA  
 Included observations: 1191

| Variable           | Coefficient | Std. Error            | t-Statistic | Prob.    |
|--------------------|-------------|-----------------------|-------------|----------|
| C                  | 111.0       | 1.942                 | 57.1        | 0.00     |
| CIGS               | -0.627      | 0.106                 | -5.87       | 0.00     |
| ORDENAC            | 1.913       | 0.653                 | 2.92        | 0.00     |
| WHITE              | 5.364       | 1.572                 | 3.41        | 0.00     |
| MALE               | 3.738       | 1.141                 | 3.27        | 0.00     |
| R-squared          | 0.050       | Mean dependent var    |             | 119.5298 |
| Adjusted R-squared | 0.047       | S.D. dependent var    |             | 20.14    |
| S.E. of regression | 19.66       | Akaike info criterion |             | 8.799    |

**¿What kind of information do we really get out of the t - statistic?**

**Linear correlation coefficients between dependent variable (weight) and residuals from alternative models**

|                  | PESO  | R1    | R2    | R3    | R4    | R5    | R6    | R7    | R8  |
|------------------|-------|-------|-------|-------|-------|-------|-------|-------|-----|
| PESO             | 1.0   |       |       |       |       |       |       |       |     |
| PESO_CIGS        | 0.990 | 1.0   |       |       |       |       |       |       |     |
| PESO_RENTA       | 0.994 | 0.987 | 1.0   |       |       |       |       |       |     |
| PESO_CIGSRENTA   | 0.987 | 0.996 | 0.992 | 1.0   |       |       |       |       |     |
| PESO_CIGSEDCUP   | 0.984 | 0.998 | 0.984 | 0.996 | 1.0   |       |       |       |     |
| PESO_CIGSEDCUPM  | 0.984 | 0.997 | 0.983 | 0.995 | 0.999 | 1.0   |       |       |     |
| PESO_TODAS       | 0.980 | 0.993 | 0.983 | 0.994 | 0.995 | 0.996 | 1.0   |       |     |
| PESO_TODAS_FIC   | 0.972 | 0.985 | 0.975 | 0.986 | 0.987 | 0.988 | 0.992 | 1.0   |     |
| PESO_TODAS_NOORD | 0.976 | 0.989 | 0.978 | 0.990 | 0.991 | 0.991 | 0.989 | 0.996 | 1.0 |

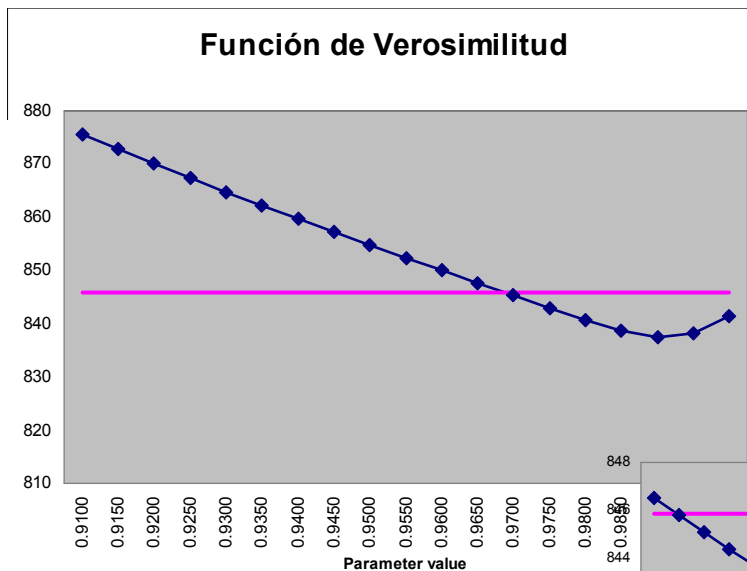
**In spite of which there is sample evidence on the fact that smoking during pregnancy affects child birth weight: *difference in median weights ...***

**... that boys weight more than girls and white babys weight more than comparable non-white babys**



## 4. Where is the power function?

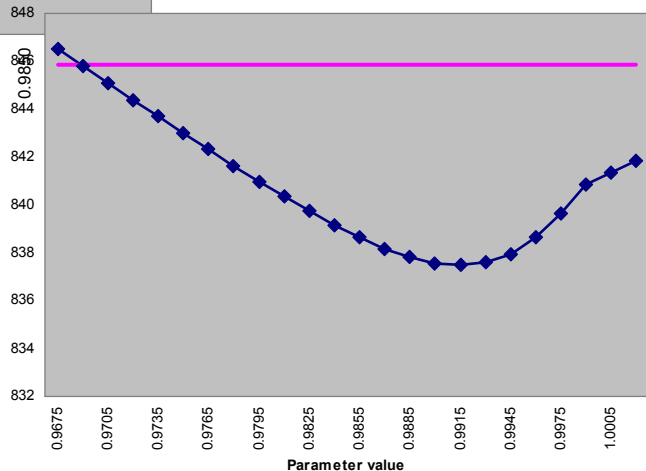
- Lack of rejection of the null hypothesis is usually identified with having shown that the hypothesis is true,
  - ✓ As a consequence of completely ignoring the power function of the test
  - ✓ And forgetting about the fact that rejecting the null hypothesis requires sample evidence in favor of the alternative hypothesis
  - ✓ Surprisingly low frequency of one-sided tests
- Providing  $p$  - values is not enough
- And they usually get the wrong interpretation:  $P [ H_0 / \text{muestra} ]$  versus  $P [ \text{muestra} / H_0 ]$
- **Much better** : graph displaying changes in an appropriate objective function under changes in parameter values: *What is the question? What is the associated loss function?*



Objective: To characterize how the VaR of a portfolio (SP500/TSE) changes with its composition.

The correlation model depends on a single parameter

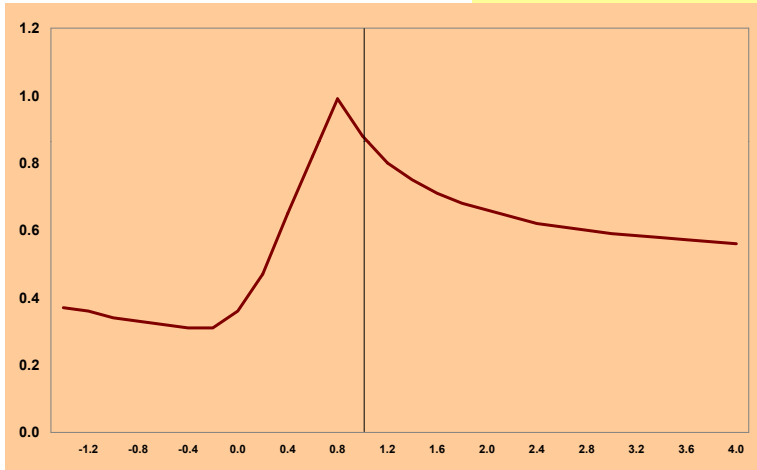
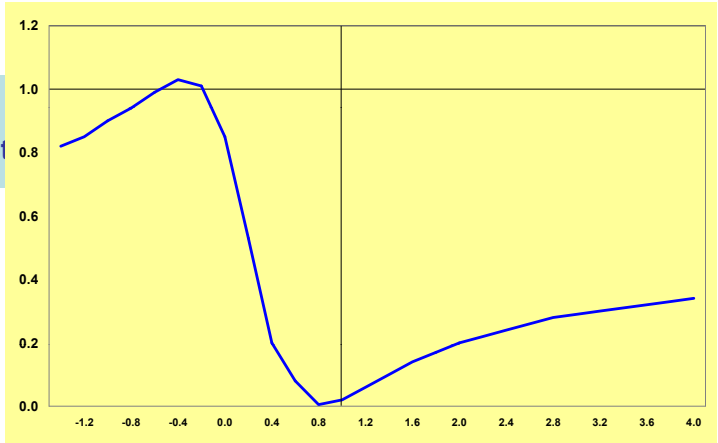
**Función de Verosimilitud**



Standard analysis: VaR is a single function of the portfolio weights

Values of LRT statistic  
H0: a given income elasticity

Testing for a unit  
elasticity of income in  
the demand for money  
function



*p-values for LRT  
statistic for income  
elasticity values*

## 5. *Interpretación de coeficientes individuales en regresiones múltiples*

### *Main difficulties when interpreting individual coefficients as individual effects*

- Taking proper account of sample variability in explanatory variables
  - ✓ Effect on Y of changes in the value of X from min(X) to Max(X), or from the 10% to the 90% percentile of X (that ignores colinearity, anyway)
  - ✓  $100\beta R(x)/R(y)$       $100\beta DT(x)/DT(y)$
- The explanatory power of X on Y is not an absolute characteristic of the two variables but rather, it is **conditional** on the model specification (the explanatory variables already included in the model, besides the sample used, the data frequency, ...)
- But we sometimes even compare statistical significance of a given variable across different models !!!

# Estrategias de diversificación en las exportaciones manufactureras – REA 2003

|                             | Indice de dispersión geográfica de exportaciones | Empleo <50 | Empleo (50,100) | Empleo (100,200) | Empleo >200     | Segundas líneas productos | Participación capital extranjero | Ratio importador | Concent. industrial | I+D/Ventas      | Publicidad/ Ventas | Concent. provincial |
|-----------------------------|--|------------|-----------------|------------------|-----------------|---------------------------|----------------------------------|------------------|---------------------|-----------------|--------------------|---------------------|
| <b>Medias muestrales</b>    |  |            |                 |                  |                 |                           |                                  |                  |                     |                 |                    |                     |
| Media                       | 0,243  | 0,203      | 0,349           | 0,221            | 0,226           | 4,375                     | 0,094                            | 0,114            | 0,185               | 0,005           | 0,009              | 0,175               |
| Beta                        |  |            | 0,026<br>(4,29) | 0,057<br>(7,25)  | 0,099<br>(13,2) | 0,004<br>(2,56)           | 0,047<br>(6,53)                  | -0,015<br>(1,96) | -0,006<br>(1,54)    | 0,051<br>(2,35) | 1,302<br>(6,44)    | 0,087<br>(6,79)     |
| Producto                    |  |            |                 |                  |                 | 0,018                     |                                  | -0,002           | -0,001              | 0,000           | 0,012              | 0,015               |
| Mínimo                      | 0  | 0          | 0               | 0                | 0               | 0                         | 0                                | 0                | 0,036               | 0,001           | 0,001              | 0,052               |
| Máximo                      | 0,560  | 1          | 1               | 1                | 1               | 82                        | 1                                | 0,724            | 0,810               | 0,083           | 0,086              | 0,745               |
| Producto                    |  |            | 0,026           | 0,057            | 0,099           | 0,328                     | 0,047                            | -0,011           | -0,005              | 0,004           | 0,111              | 0,060               |
| <b>Desviaciones típicas</b> |  |            |                 |                  |                 |                           |                                  |                  |                     |                 |                    |                     |
|                             | 0,170  |            |                 |                  |                 | 5,480                     |                                  | 0,200            | 0,140               | 0,010           | 0,060              | 0,180               |
|                             |  |            |                 |                  |                 | 0,022                     |                                  | -0,003           | -0,001              | 0,001           | 0,078              | 0,016               |

## Ejemplo 1: Taking into account sample variation

Positive size effect. ✓

Positive effect from the number of products (✓) and from foreign capital participation (≠).

Negative effect from import coefficient (≠)

No effect from market concentration (✓)

Positive effect from the other two product differentiation variables: Advertising (✓) and R&D expenditures (≠).

## Explanatory power/information content are conditional concepts

- We cannot test for the information content or the explanatory power of a given regressor in a multiple regression model.
  - ✓ For that, we would have to use a single regression model approach
  - ✓ In a multiple regression model, we can just test for the amount of information a given variable **adds** to those already included in the model
- Colinearity is central in this evaluation (as it is in the interpretation of individual coefficients)
- Collinearity
  - ✓ Requires some structural interpretation. Cholesky decomposition as an example
  - ✓ What type of questions can we give an answer to?
- Omitted variable bias (Are we getting it right?)

## Omitted variable bias

$$Ventas_t = 247,6 + 2,204 Pub_t - 1,464 P_t$$

(0,545)                      (0,649)

$$Ventas_t = 96,0 + 3,224 Pub_t$$

(0,375)

An increase of 6.200 euros in advertising = 1 standard deviation

Corr(Pub,P) = -0,829  $\Rightarrow$  decrease of -0,829 standard deviations in price = 4,327 euros.

Total effect on sales: (6,200)(2,204) + (1,464)(4,327) = 20,0 thousand euros

Single variable model: (3,224) (6,200) = 20,0 thousand euros

- The simple linear regression measures the *global effect (direct+indirect)* on Y of a change in either one of the X
  - It is a biased estimation of the *ceteris paribus individual effect (indirect)*, which is seldom interesting
  - But it is an unbiased estimate of the global effect, the one on which we are usually interested
- While the multiple regression provides a biased estimation of that global effect, because of collinearity
- What is the question ?

## 6. Tratamiento de la colinealidad

Dependent Variable: RENTA  
 Sample: 1 83  
 Included observations: 58  
 Excluded observations: 25

**T1**

| Variable           | Coefficient | Std. Error            | t-Statistic | Prob. |
|--------------------|-------------|-----------------------|-------------|-------|
| C                  | 7.699       | 0.168                 | 45.74       | 0.00  |
| OIL                | 1.130       | 0.246                 | 4.59        | 0.00  |
| INTER              | -0.434      | 0.446                 | -0.97       | 0.33  |
| PREM               | -0.344      | 0.339                 | -1.01       | 0.31  |
| INFLAC             | 0.032       | 0.370                 | 0.08        | 0.93  |
| OVER               | -0.143      | 0.287                 | -0.49       | 0.61  |
| DEMOC              | 0.218       | 0.180                 | 1.21        | 0.23  |
| ESTAB              | -0.258      | 0.204                 | -1.26       | 0.21  |
| EFICA              | 0.158       | 0.308                 | 0.51        | 0.61  |
| REGULA             | 0.632       | 0.207                 | 3.04        | 0.00  |
| LEYES              | 0.273       | 0.235                 | 1.16        | 0.25  |
| CONTROL            | 0.353       | 0.297                 | 1.18        | 0.24  |
| R-squared          | 0.674       | Mean dependent var    |             | 7.577 |
| Adjusted R-squared | 0.596       | S.D. dependent var    |             | 0.896 |
| S.E. of regression | 0.569       | Akaike info criterion |             | 1.894 |

**Cleaning “non-significant variables” and re-estimating the model**

|        | RES_T1 | RES_T4 | RES_T5 |
|--------|--------|--------|--------|
| RES_T1 | 1.00   |        |        |
| RES_T4 | 0.949  | 1.00   |        |
| RES_T5 | 0.768  | 0.801  | 1.00   |

Dependent Variable: RENTA  
 Sample: 1 83  
 Included observations: 70  
 Excluded observations: 13

**T4**

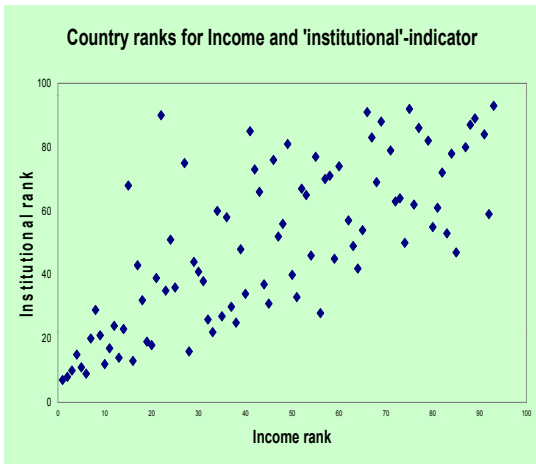
| Variable           | Coefficient | Std. Error            | t-Statistic | Prob. |
|--------------------|-------------|-----------------------|-------------|-------|
| C                  | 7.652       | 0.111                 | 68.79       | 0.00  |
| OIL                | 1.093       | 0.204                 | 5.34        | 0.00  |
| INTER              | -0.748      | 0.338                 | -2.21       | 0.03  |
| REGULA             | 0.717       | 0.133                 | 5.36        | 0.00  |
| CONTROL            | 0.677       | 0.126                 | 5.34        | 0.00  |
| R-squared          | 0.656       | Mean dependent var    |             | 7.544 |
| Adjusted R-squared | 0.635       | S.D. dependent var    |             | 0.923 |
| S.E. of regression | 0.557       | Akaike info criterion |             | 1.737 |

Dependent Variable: RENTA  
 Sample: 1 83  
 Included observations: 82  
 Excluded observations: 1

**T5**

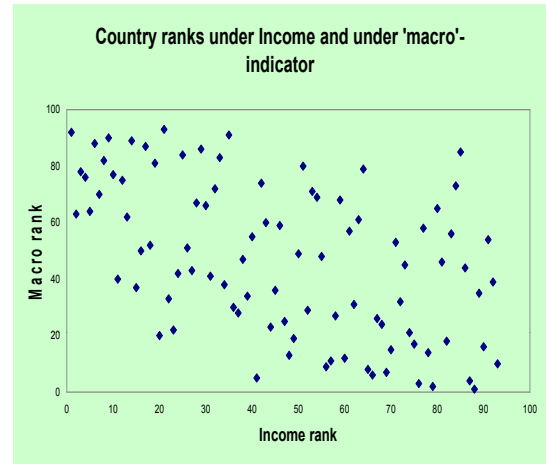
| Variable           | Coefficient | Std. Error            | t-Statistic | Prob. |
|--------------------|-------------|-----------------------|-------------|-------|
| C                  | 7.376       | 0.081                 | 90.56       | 0.00  |
| OIL                | 0.700       | 0.233                 | 2.99        | 0.00  |
| REGULA             | 0.946       | 0.116                 | 8.15        | 0.00  |
| R-squared          | 0.477       | Mean dependent var    |             | 7.470 |
| Adjusted R-squared | 0.464       | S.D. dependent var    |             | 0.943 |
| S.E. of regression | 0.690       | Akaike info criterion |             | 2.133 |

# Factores económicos vs. Factores institucionales como determinantes del crecimiento



Rank corr: .71 (9.2)

Utilizando institutions\macro:  
Rank corr: .50 (4.9)



Rank corr: -.51 (-5.7)

Utilizando macro\institutions:  
Rank corr: -.11 (-1.0)

Dependent Variable: RENTA. Method: Least Squares  
Sample: 1 93. Included observations: 87 Excluded observations: 6

| Variable           | Coefficient | Std. Error | t-Statistic | Prob. |
|--------------------|-------------|------------|-------------|-------|
| C                  | 7.734       | 0.072      | 108.48      | 0.00  |
| INSTITUTIONS       | 1.826       | 0.166      | 10.98       | 0.00  |
| MACRO_INSTITUTIONS | -0.211      | 0.144      | -1.46       | 0.15  |

|                    |        |                       |       |
|--------------------|--------|-----------------------|-------|
| R-squared          | 0.594  | Mean dependent var    | 7.688 |
| Adjusted R-squared | 0.584  | S.D. dependent var    | 1.029 |
| S.E. of regression | 0.664  | Akaike info criterion | 2.052 |
| Sum squared resid  | 37.018 | Schwarz criterion     | 2.137 |
| Log likelihood     | -86.28 | F-statistic           | 61.35 |
| Durbin-Watson stat | 2.25   | Prob(F-statistic)     | 0.000 |

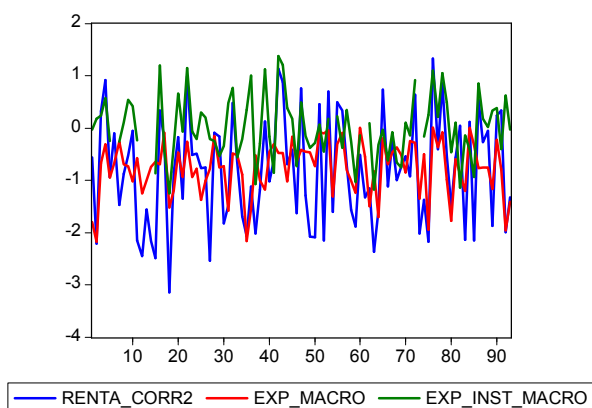
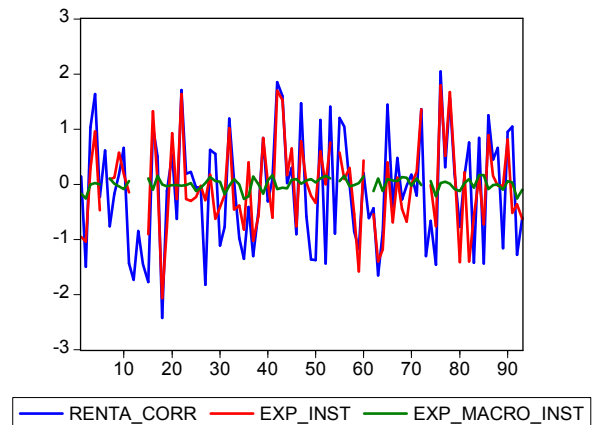
## Orthogonalize explanatory variables

Dependent Variable: RENTA. Method: Least Squares  
Sample: 1 93. Included observations: 87 Excluded observations: 6

| Variable           | Coefficient | Std. Error | t-Statistic | Prob. |
|--------------------|-------------|------------|-------------|-------|
| C                  | 8.446       | 0.125      | 67.285      | 0.000 |
| MACRO              | -0.879      | 0.119      | -7.329      | 0.000 |
| INSTITUTIONS_MACRO | 1.663       | 0.200      | 8.307       | 0.000 |

|                    |        |                       |       |
|--------------------|--------|-----------------------|-------|
| R-squared          | 0.594  | Mean dependent var    | 7.688 |
| Adjusted R-squared | 0.584  | S.D. dependent var    | 1.029 |
| S.E. of regression | 0.664  | Akaike info criterion | 2.052 |
| Sum squared resid  | 37.018 | Schwarz criterion     | 2.137 |
| Log likelihood     | -86.28 | F-statistic           | 61.35 |
| Durbin-Watson stat | 2.25   | Prob(F-statistic)     | 0.000 |



## 7. Sugerencias

### Excessive summary of sample information

El modelo más general, modelo ARCH-Poisson-Gaussiano se especifica como sigue:

$$\Delta r_t = \mu_t + \sigma_t \Delta z_t + J_t \Delta n_t; \quad \Delta z_t \sim N(0, 1); \quad J_t \sim N(\theta_t, \psi^2); \quad \Delta z_t \text{ y } J_t \text{ son}$$

independientes;  $\sigma_t^2 = \omega_0 + \omega_1 [\Delta r_{t-1} - E_{t-1}(\Delta r_{t-1})]^2$ ;  $\mu_t$  y  $\theta_t$  están definidos en la siguiente tabla.

|                      | $\mu_t = \alpha(r_{t-1} - r_{t-1}^*)$ |   | $\mu_t = \alpha_1(r_{t-1} - r_{t-1}^*) + \alpha_2(r_{t-1} - r_{t-1}^*)^2$ |   |
|----------------------|---------------------------------------|---|---|---|
| Parámetros           | Modelo i<br>$\theta_t = \theta$       | Modelo ii<br>$\theta_t = \gamma(r_{t-1} - r_{t-1}^*)$ | Modelo iii<br>$\theta_t = \theta$   | Modelo iv<br>$\theta_t = \gamma(r_{t-1} - r_{t-1}^*)$ |
| $\alpha$             | -0.046<br>(-6.601)                    | -0.0344<br>(-6.365)                                   | -----   | -----   |
| $\alpha_1$           | -----                                 | -----   | -0.0465<br>(-6.244)   | -0.0388<br>(-7.832)                                   |
| $\alpha_2$           | -----                                 | -----   | -1.0928<br>(-263.81)  | -0.9943<br>(-61.837)                                  |
| $\omega_0$           | 0.00003<br>(5.123)                    | 0.00003<br>(7.189)                                    | 0.0004<br>(10.127)  | 0.0004<br>(12.833)                                    |
| $\omega_1$           | 0.6240<br>(5.922)                     | 0.6092<br>(5.542)                                     | 0.6651<br>(6.338)   | 0.6482<br>(6.053)                                     |
| $\theta$ or $\gamma$ | -0.0087<br>(-1.196)                   | -0.4152<br>(-8.179)                                   | -0.009<br>(-1.170)  | -0.2758<br>(-4.406)                                   |
| $\psi$               | 0.2101<br>(12.939)                    | 0.1903<br>(14.249)                                    | 0.2003<br>(12.294)  | 0.1930<br>(13.035)                                    |
| $\delta_0$           | 0.1209<br>(7.841)                     | 0.1128<br>(6.917)                                     | 0.1025<br>(7.005)   | 0.1023<br>(7.209)                                     |
| $\delta_1$           | 0.5260<br>(10.201)                    | 0.5271<br>(11.546)                                    | 0.5500<br>(10.714)  | 0.5347<br>(10.431)                                    |
| $\delta_2$           | 0.5257<br>(8.838)                     | 0.5076<br>(9.830)                                     | 0.5233<br>(8.486)   | 0.5306<br>(8.460)                                     |
| $\delta_3$           | 0.1421<br>(3.582)                     | 0.1309<br>(4.239)                                     | 0.1344<br>(3.493)   | 0.1476<br>(3.568)                                     |
| $\delta_4$           | 0.8307<br>(10.343)                    | 0.8060<br>(10.055)                                    | 0.8763<br>(10.372)  | 0.8847<br>(10.998)                                    |
| $\delta_5$           | 0.3896<br>(2.741)                     | 0.3569<br>(3.080)                                     | 0.4368<br>(2.843)   | 0.4373<br>(3.367)                                     |
| Log-L<br>[SIC]       | 2186.46<br>[2147.01]                  | 2222.14<br>[2182.69]                                  | 2237.55<br>[2194.51]  | 2256.05<br>[2218.01]                                  |

Resultados de la estimación por máxima verosimilitud con desviaciones típicas robustas de Bollerslev y Wooldridge (1992). Estadístico t entre paréntesis. Log-L es el logaritmo de la función de verosimilitud. Los coeficientes  $\delta_0, \delta_1, \delta_2, \delta_3, \delta_4, \delta_5$  destacan respectivamente las probabilidades de salto (0) en los

1. Models with the same measure of fit: R2, log-likelihood. Do they explain the same?

2. What is the difference between models with statistically significant differences in their log-likelihood values?

3. What is the final question? How does the answer to that changes across alternative models?

- volatilidad
- saltos
- VaR



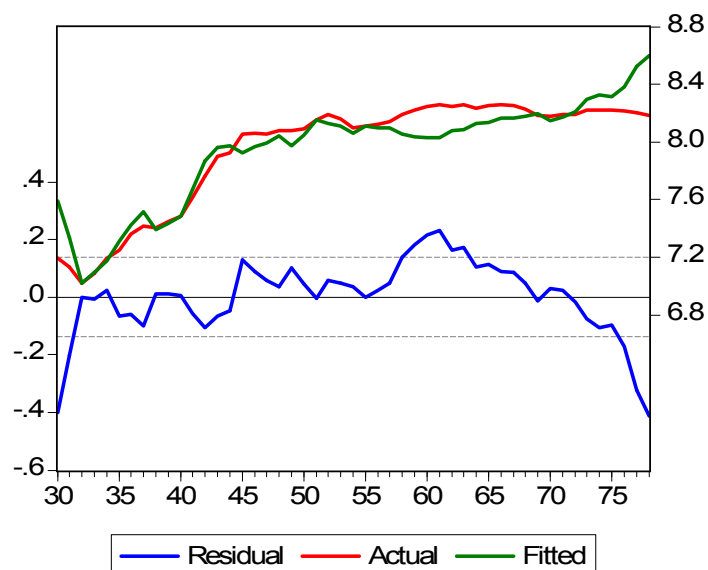
## S1. Avoid an excessive summary of sample information

### Examine the residuals in detail

- ¿When do two alternative models have “the same” explanatory power?
- Graphical representations of actual data, fitted data and residuals
  - They contain complete information on the estimated model
  - Avoiding too much information reduction
  - Search for local information content: a specific but short period of time, a particular set of observations in cross-section data sharing some common characteristic: omitted variables.
- Discover subsamples of poor model fitting
- How to compare alternative models:
  - How much similarity between sets of residuals should we expect to find?
  - What is explained by a model which is not explained by others?

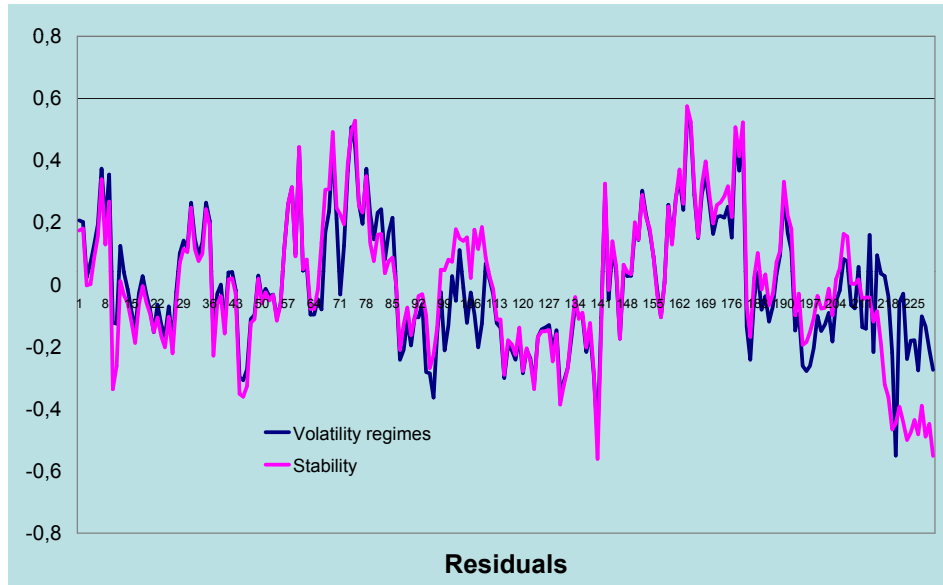
### Subsamples of model deterioration

#### *Consumo de tabaco explicado por la renta y el precio*



What is explained by a model which is not explained by competing models?

*Explaining credit spreads by regime switching models*



## *S2. Alternative approach to testing parametric constraints*

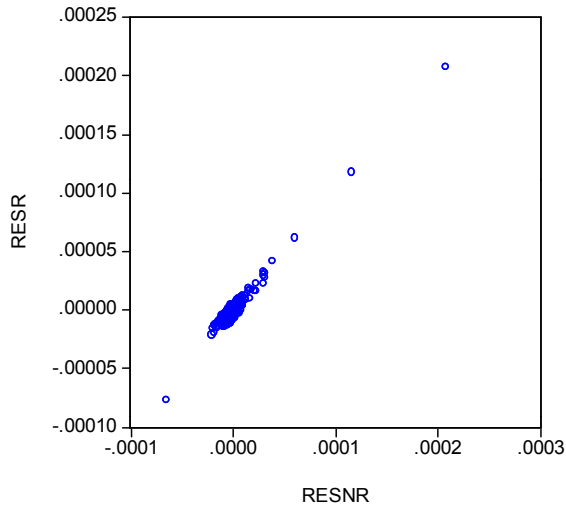
- *The constraints being tested cannot be rejected on the basis of the sample evidence if and only if the residuals of the restricted and unrestricted models contain the same information regarding the question which is the ultimate object of research*
- What matters is not so much the test, but the detailed comparison between the two sets of residuals.
- Different approaches to testing for equality of residuals:
  - Nonparametric point-to-point tests for equality of residual sets
  - Tests for reduction in absolute size and in variance in subsamples of largest residuals or in the whole sample.
  - Any appropriate test?

Dependent Variable: VAAA Sample (adjusted): 1997M02 2012M01  
 Included observations: 180 after adjustments

|          | Coefficient | Std. Error | t-Statistic | Prob.  |
|----------|-------------|------------|-------------|--------|
| C        | 7.37E-06    | 2.84E-06   | 2.596229    | 0.0102 |
| VAAA(-1) | 0.290072    | 0.073017   | 3.972664    | 0.0001 |
| TERM     | 0.000365    | 0.000137   | 2.669464    | 0.0083 |

|                    |          |                       |           |
|--------------------|----------|-----------------------|-----------|
| R-squared          | 0.159143 | Mean dependent var    | 1.94E-05  |
| Adjusted R-squared | 0.149642 | S.D. dependent var    | 2.33E-05  |
| S.E. of regression | 2.15E-05 | Akaike info criterion | -18.64311 |
| Sum squared resid  | 8.16E-08 | Schwarz criterion     | -18.58990 |
| Log likelihood     | 1680.880 | Hannan-Quinn criter.  | -18.62154 |
| F-statistic        | 16.74978 | Durbin-Watson stat    | 2.029103  |
| Prob(F-statistic)  | 0.000000 |                       |           |

Residuos restringidos versus residuos sin restringir



Dependent Variable: VAAA Sample (adjusted): 1997M02 2012M01  
 Included observations: 180 after adjustments

|          | Coefficient | Std. Error | t-Statistic | Prob.  |
|----------|-------------|------------|-------------|--------|
| C        | 1.25E-05    | 2.12E-06   | 5.897115    | 0.0000 |
| VAAA(-1) | 0.354143    | 0.070136   | 5.049362    | 0.0000 |

|                    |          |                       |           |
|--------------------|----------|-----------------------|-----------|
| R-squared          | 0.125290 | Mean dependent var    | 1.94E-05  |
| Adjusted R-squared | 0.120376 | S.D. dependent var    | 2.33E-05  |
| S.E. of regression | 2.18E-05 | Akaike info criterion | -18.61475 |
| Sum squared resid  | 8.49E-08 | Schwarz criterion     | -18.57928 |
| Log likelihood     | 1677.328 | Hannan-Quinn criter.  | -18.60037 |
| F-statistic        | 25.49606 | Durbin-Watson stat    | 2.091023  |
| Prob(F-statistic)  | 0.000001 |                       |           |

### S3. How can we decide on information content?

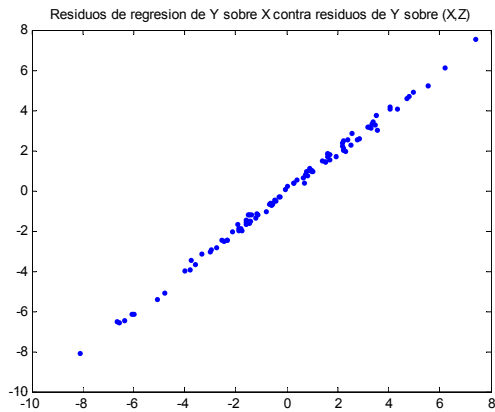
- Variable  $x_t$  adds information to vector  $z_t$  to explain  $y_t$  iff the residuals of the model that explains  $y_t$  by vector  $z_t$  are significantly different from those of the model that explains  $y_t$  by  $(z_t, x_t)$ .
- We move from testing for statistical significance to testing for equality of sets of residuals
- Questions that are often asked:
  - Does Z add any information to X to explain Y ?
  - Is it X or Z that contains more information on Y?
    - Look at residuals from single variable projections
    - Orthogonalize using different orderings
    - Are we interpreting correctly the *omitted variable bias*?

## Testing for additional information content by comparing residuals from restricted and unrestricted models

### Irrelevant Z-variable

Correlations:

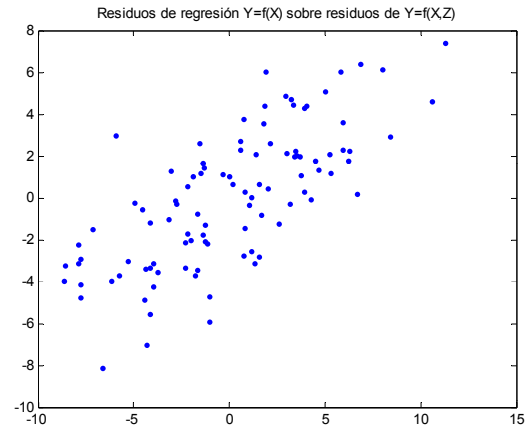
|   | Y     | X     | Z     | u     |
|---|-------|-------|-------|-------|
| Y | 1.00  | 0.85  | -0.01 | 0.49  |
| X | 0.85  | 1.00  | 0.02  | -0.04 |
| Z | -0.01 | 0.02  | 1.00  | -0.05 |
| u | 0.49  | -0.04 | -0.05 | 1.00  |



### Relevant Z-variable

Correlations:

|   | Y    | X    | Z    | u    |
|---|------|------|------|------|
| Y | 1.00 | 0.79 | 0.49 | 0.58 |
| X | 0.79 | 1.00 | 0.09 | 0.11 |
| Z | 0.49 | 0.09 | 1.00 | 0.12 |
| u | 0.58 | 0.11 | 0.12 | 1.00 |



## S4. Evaluate restrictions on the basis of their implications for the issue being analyzed

- What a difference does it make a given restriction for the final question under analysis? What implications do alternative models have for the final question?
- Compare alternative models using loss functions defined on the value of the final objective function under each model: predicción, estimación de una volatilidad o una correlación, gestión de carteras, ...
- **What is the final question?**
  - what is the implication of asymmetric effects on conditional variance on VaR calculations?
  - is there any forecasting improvement from imposing long-run cointegration relationships?
  - Is time between trades weakly exogenous with respect to volume?

# *Pero ¿no es esto lo que ya venimos haciendo?*

## *Lo que NO debe hacerse:*

1. *No identificar significación estadística y contenido informativo/capacidad explicativa*
2. *No contrastar la significación estadística de un coeficiente*
  - *Evaluar el contenido informativo en una variable.*
  - *Considerar el contenido informativo en una variable explicativa como un concepto condicional, y evaluarlo de modo apropiado.*
3. *No resumir excesivamente la información muestral*
4. *No apoyarse exclusivamente en estadístico tipo  $t$  y  $F$  al evaluar restricciones paramétricas o al comparar modelos alternativos*
5. *No comparar el contenido informativo de distintas variables examinando sus coeficientes o sus estadísticos  $t$* 
  - *No practicar econometría de signos o de asteriscos*
6. *No poner mucho énfasis en coeficientes individuales estimados en regresiones múltiples*
7. *Tratar la colinealidad y tener en cuenta la variabilidad muestral de cada variable*
8. *No contrastar demasiado...*
  - *... y si se contrasta, no olvidar analizar la potencia del contraste*

## *Pautas que deben seguirse:*

1. *Comenzar definiendo con claridad la (única) cuestión objeto de análisis. No perder dicha referencia a lo largo del trabajo empírico*
2. *Analizar los datos desde distintos puntos de vista, utilizando una variedad de procedimientos estadísticos*
  - *Describiendo en detalle las características de los datos : rango muestral, histogramas, diagramas stem and leaf, evaluación no paramétrica de asociación entre variables*
  - *Diseño de contrastes paramétricos y no paramétricos acerca de:*
    - ✓ *características que deberían observarse si la hipótesis en estudio fuese correcta*
    - ✓ *características que **no** deberían observarse en los datos si la hipótesis en estudio **no** fuese correcta*
  - *Contrastar hipótesis paramétricas mediante comparación punto a punto de residuos de la regresión restringida y sin restringir*
3. *Comparar modelos (evaluar restricciones) desde el punto de vista de su impacto sobre la cuestión que se analiza: predicción, medición de riesgo, gestión de carteras...*
  - *Qué explica un modelo que no es explicado por otros modelos?*
  - *Cómo de distintos son dos modelos alternativos?*
  - *Simulación de modelos*
4. *Proporcionar evidencia acerca de variabilidad paramétrica*

*FIN (por ahora)*

## *Significación estadística frente a contenido informativo: Algunas aparentes paradojas*

**Problema:** El BCE quiere reducir la inflación un punto porcentual elevando los tipos de interés ¿en cuánto debe hacerlo?

Modelo:  $\pi_t = \alpha + \beta r_t + u_t$

H0:  $\beta=1$  versus: H1:  $\beta<1$

- **Paradoja 1:** Estimación:  $\beta = .65$  (.25)      No rechazamos H0 (!!!) [reducida precisión]
  - *Cuestión clave: Relación entre precisión en la estimación y potencia en el contraste*
  - *No deberíamos contrastar*
- **Paradoja 2:** Estimación:  $\beta = .95$  (.05)      Rechazamos H0 [“excesiva” precisión?]
- **Paradoja 2:** Estimación:  $\beta = 1.45$  (.10)
  - No rechazamos H0 (!!!) [Solo se cumple una de las 2 condiciones precisas para rechazar]
  - *No tiene sentido contrastar*